

# ECE 2EI4 Lab Test (Section 1)

Use the following formulae in your solutions

## NMOS Transistor Mathematical Model

Cut off region  $i_{DS}=0$  for  $v_{GS} < V_{TN}$

Linear region  $i_{DS} = K_n (v_{GS} - V_{TN} - 0.5 v_{DS}) v_{DS}$  for  $v_{GS} - V_{TN} \geq v_{DS} \geq 0$

Saturation region  $i_{DS} = \frac{K_n}{2} (v_{GS} - V_{TN})^2 (1 + \lambda v_{DS})$  for  $v_{DS} \geq v_{GS} - V_{TN} \geq 0$

## PMOS Transistor Mathematical Model

Cut off region  $i_{SD}=0$  for  $v_{SG} < -V_{TP}$

Linear region  $i_{SD} = K_p (v_{SG} + V_{TP} - 0.5 v_{SD}) v_{SD}$  for  $v_{SG} + V_{TP} \geq v_{SD} \geq 0$

Saturation region  $i_{SD} = \frac{K_p}{2} (v_{SG} + V_{TP})^2 (1 + \lambda v_{SD})$  for  $v_{SD} \geq v_{SG} + V_{TP} \geq 0$

## Small signal Model Parameter of NMOS Transistors

$$g_m = \sqrt{2 K_n I_{DS} (1 + \lambda V_{DS})}$$

$$r_o = \frac{\frac{1}{\lambda} + V_{DS}}{I_{DS}}$$

## Propagation delays for reference CMOS inverter with $V_{DD}=5V$ , $V_{TN}=1V$ and $V_{TP}=-1V$

$$\tau_{PHL} = 0.322 \frac{C}{K_n}$$

$$\tau_{PLH} = 0.322 \frac{C}{K_p}$$

**Mathematical Model of the pn junction**

$$I = I_s(\exp(V_D / V_T) - 1)$$

**Full Transport Model of npn transistors**

$$i_C = I_s \left[ \exp\left(\frac{V_{BE}}{V_T}\right) - \exp\left(\frac{V_{BC}}{V_T}\right) \right] - \frac{I_s}{\beta_R} \left[ \exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right]$$

$$i_E = I_s \left[ \exp\left(\frac{V_{BE}}{V_T}\right) - \exp\left(\frac{V_{BC}}{V_T}\right) \right] + \frac{I_s}{\beta_F} \left[ \exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right]$$

$$i_B = \frac{I_s}{\beta_F} \left[ \exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right] + \frac{I_s}{\beta_R} \left[ \exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right]$$

**Simplifications of the Transport Model of npn Transistors**

Forward active region:  $i_C = I_s \exp\left(\frac{V_{BE}}{V_T}\right)$ ,  $i_B = \frac{i_C}{\beta_F}$  and  $i_E = \frac{i_C}{\alpha_F}$

Saturation Region:  $v_{CESAT}=0.2 \text{ V}$

Cut-off region:  $i_B = i_C = i_E = 0$

**Full Transport Model of pnp transistors**

$$i_C = I_s \left[ \exp\left(\frac{V_{EB}}{V_T}\right) - \exp\left(\frac{V_{CB}}{V_T}\right) \right] - \frac{I_s}{\beta_R} \left[ \exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right]$$

$$i_E = I_s \left[ \exp\left(\frac{V_{EB}}{V_T}\right) - \exp\left(\frac{V_{CB}}{V_T}\right) \right] + \frac{I_s}{\beta_F} \left[ \exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right]$$

$$i_B = \frac{I_s}{\beta_F} \left[ \exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right] + \frac{I_s}{\beta_R} \left[ \exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right]$$

**Simplifications of the Transport Model of pnp Transistors**

Forward active region:  $i_C = I_s \exp\left(\frac{V_{EB}}{V_T}\right)$ ,  $i_B = \frac{i_C}{\beta_F}$  and  $i_E = \frac{i_C}{\alpha_F}$

Saturation Region:  $v_{ECSAT}=0.2 \text{ V}$

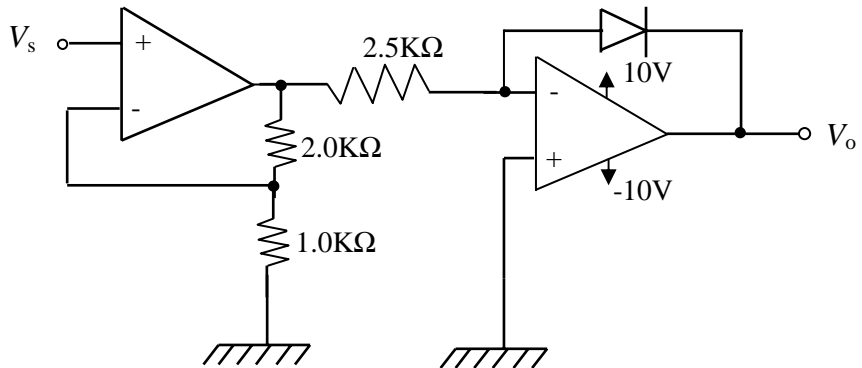
Cut-off region:  $i_B = i_C = i_E = 0$

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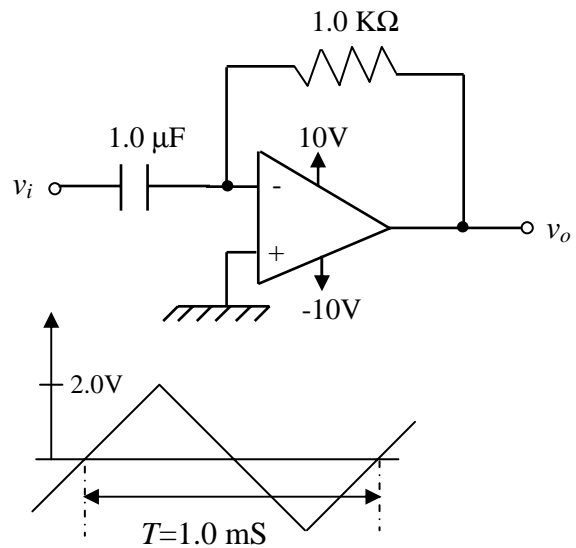
1) For the shown circuit the diode reverse saturation current is  $I_s = 10^{-15}$  A. If  $V_s = 1.0$  V,  $V_o$  is

- a) 0.6852 V
- b) -0.6852 V
- c) 0.755 V
- d) -0.755V
- e) -10V



2) The input to the shown circuit is a triangular waveform with amplitude of 2.0 V. The output  $v_o$  as observed on the scope is

- a) a triangular waveform with amplitude 10V and frequency 1.0 KHz.
- b) a square waveform with amplitude 10 V and frequency 1.0 KHz.
- c) a square waveform with amplitude 8 V and frequency 1.0 KHz.
- d) a triangular waveform with amplitude 8V and frequency 1.0 KHz.
- e) a square waveform with amplitude 8 V and frequency 2.0 KHz.

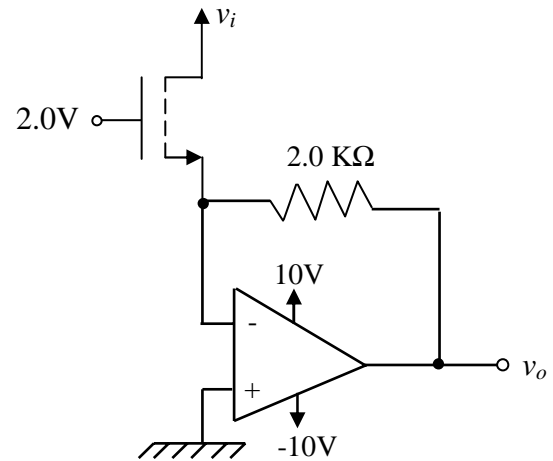


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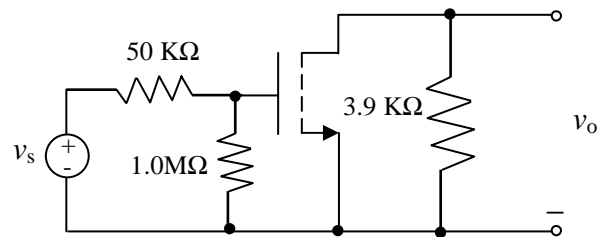
3) The enhancement NMOS transistor in the shown circuit has  $K_n=1.0 \text{ mA/V}^2$ ,  $V_{TN}= 1.0 \text{ V}$  and  $\lambda = 0 \text{ V}^{-1}$ . If the voltage  $v_i$  changes from 1.0 V to 2.0 V, which one of the following statements will be correct?

- a) The output voltage changes from -1.0 V to -2.0 V.
- b) The output voltage changes from -2.0 V to -4.0 V.
- c) The transistor changes state from saturation region to linear region.
- d) The transistor is in the cut-off region.
- e) The output voltage does not change.



4) The figure to the right shows the ac equivalent circuit of an NMOS amplifier with  $K_n=1.0 \text{ mA/V}^2$ ,  $V_{TN}=1.0 \text{ V}$  and  $\lambda=0 \text{ V}^{-1}$ . The operating point is  $(I_{DS}, V_{DS})=(2.0 \text{ mA}, 7.5 \text{ V})$ . If the ac source is  $v_s=0.1 \sin(2\pi \times 10^3 t) \text{ V}$ , the maximum and minimum values of the total drain-to-source voltage  $v_{DS}$  are approximately

- a) 8.24 V, 6.76 V
- b) 0.74 V, -0.74 V
- c) 8.24 V, 7.76 V
- d) 7.76 V, 6.76 V
- e) None of the above

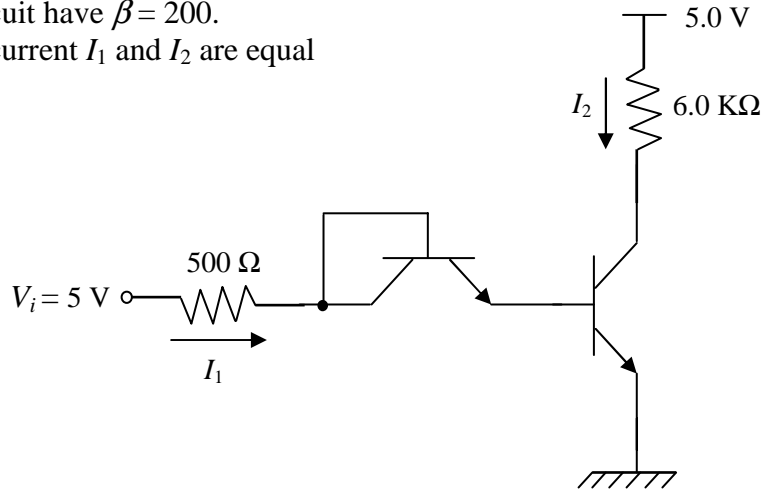


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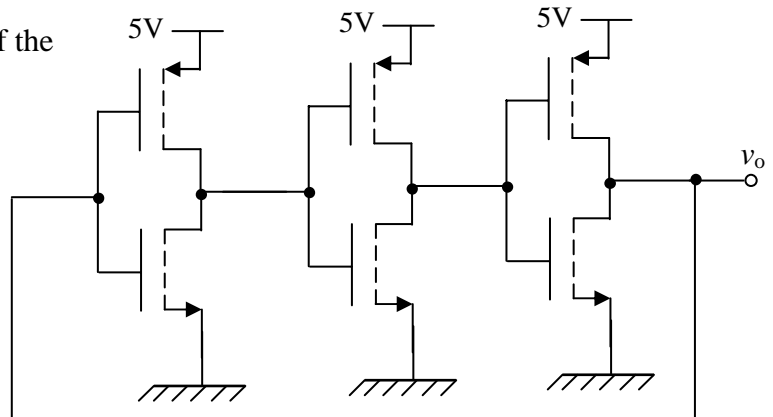
5) Both transistors in the shown circuit have  $\beta = 200$ .  
For an input voltage  $V_i = 5.0 \text{ V}$ , the current  $I_1$  and  $I_2$  are equal to, respectively,

- a) 7.2 mA, 0.8 mA
- b) 7.2 mA, 1.44 A
- c) 8.6 mA, 0.8 mA
- d) 8.6 mA, 1.72 A
- e) None of the above



6) The propagation delay in each one of the inverter stages in the shown circuit is  $t_p = 2.0 \text{ nSec}$ . The frequency of this ring oscillator is

- a) 375 MHz
- b) 166 MHz
- c) 250 MHz
- d) 83 MHz
- e) None of the above

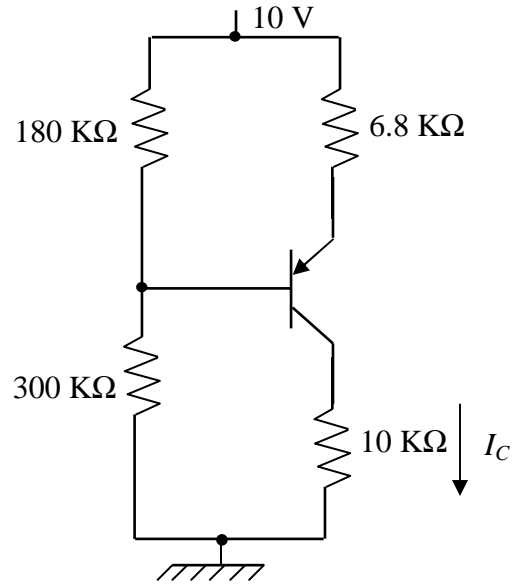


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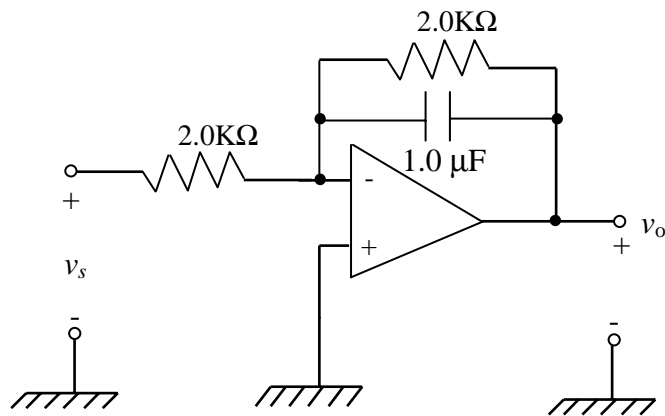
7) The pnp transistor in the shown circuit has  $\beta = 100$ .  
The operating point ( $V_{EC}$ ,  $I_C$ ) is

- a) -3.5649 V, 0.3816 mA
- b) 3.2152 V, 0.527 mA
- c) 3.5649 V, 0.3816 mA
- d) 4.2354 V, -0.4321 mA
- e) None of the above



8) If the input to the shown circuit is  $v_s = 2.0 \sin(500t)$ , the output  $v_o$  is

- a)  $\sqrt{2} \sin(500t - 0.75\pi)$
- b)  $2.0 \sin(500t + 0.75\pi)$
- c)  $-2.0 \sin(500t + 0.75\pi)$
- d)  $\sqrt{2} \sin(500t + 0.75\pi)$
- e)  $2.0 \sin(500t - 0.75\pi)$

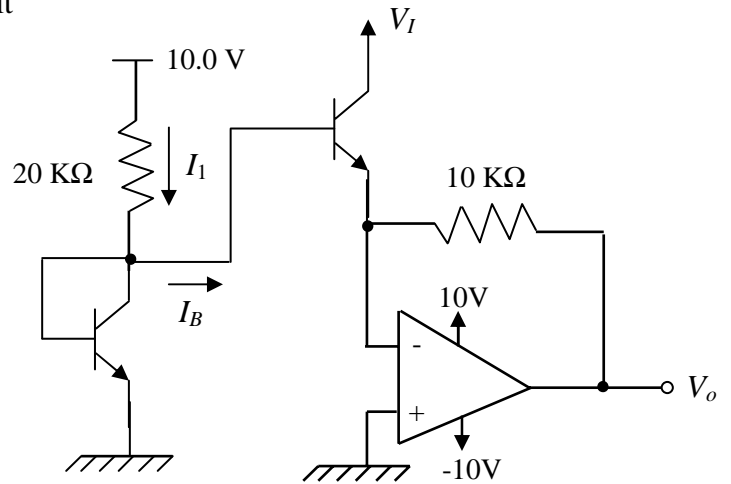


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9) The two npn transistors in the shown circuit are matched with  $\beta = 100$ . The currents  $I_1$  and  $I_B$  are, respectively,

- a) 0.490 mA, 4.8  $\mu$ A
- b) 0.465 mA, 4.55  $\mu$ A
- c) 0.50 mA, 4.9  $\mu$ A
- d) 0.465 mA, 10.0  $\mu$ A
- e) 0.490 mA, 10  $\mu$ A



10) In problem (9), if  $V_I = 5.0$  V,  $V_o$  is

- a) -4.7 V
- b) -4.89 V
- c) -3.65 V
- d) -5.0 V
- e) -4.59 V