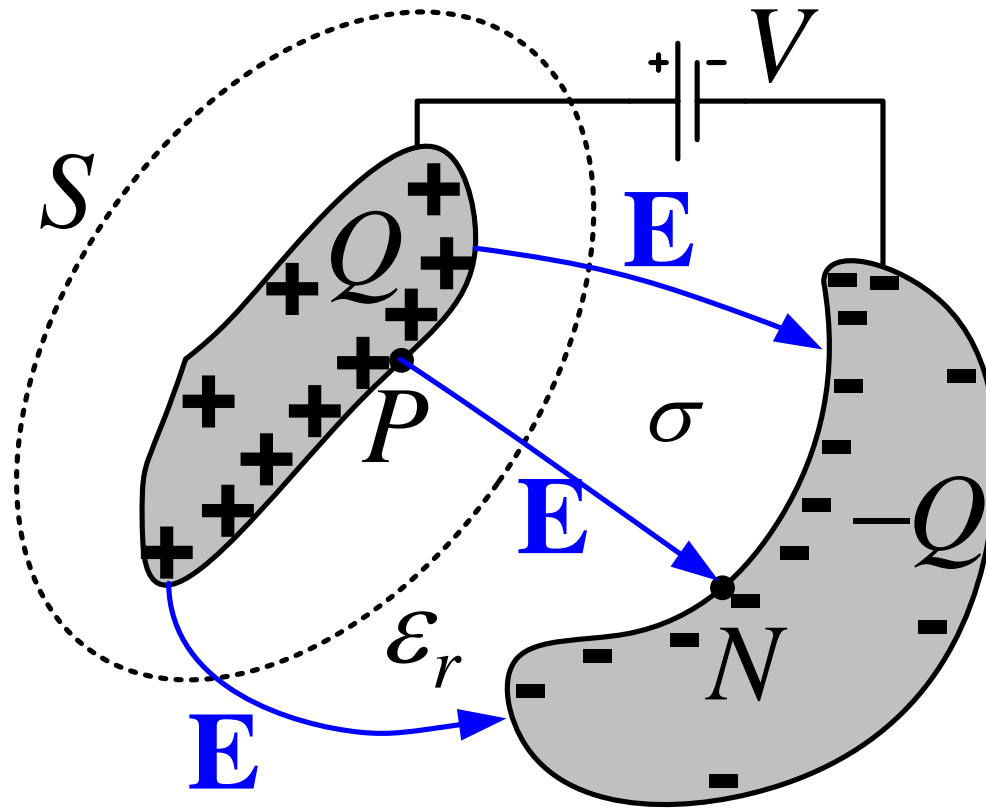


Lecture 16: Electrostatics

Resistance and Capacitance, Chapter 6, pages
239-256

Two Conductors



Evaluating Resistance between Two Conductor

start with Poisson's or Laplace's equations to determine $V(\mathbf{r})$

evaluate electric field using $\mathbf{E} = -\nabla V$

evaluate current density using $\mathbf{J} = \sigma \mathbf{E}$

evaluate current flowing between the two conductors using

$$I = \oiint_S \mathbf{J} \cdot d\mathbf{S}$$

conductance is given by $G = \frac{I}{V_a - V_b}$

Evaluating Capacitance (V-method)

start with Poisson's or Laplace's equations to determine $V(\mathbf{r})$

evaluate electric field using $\mathbf{E} = -\nabla V$

evaluate \mathbf{D} using $\mathbf{D} = \epsilon \mathbf{E}$

evaluate electric flux diverging from the positive conductor using

$$Q = \psi = \oiint \mathbf{D} \cdot d\mathbf{S}$$

capacitance is given by $C = \frac{Q}{V_a - V_b}$

Evaluating Capacitance (Q-method)

start by assuming a charge Q on one of the positive conductor

apply Gauss Law to solve for \mathbf{D}

evaluate \mathbf{E} using $\mathbf{E}=\mathbf{D}/\epsilon$

evaluate potential difference between the two conductors using

$$V_a - V_b = \int_a^b \mathbf{E} \cdot d\mathbf{L}$$

capacitance is given by $C = \frac{Q}{V_a - V_b}$