

# **Low-Frequency Noise in SiGeC-Based pMOSFETs**

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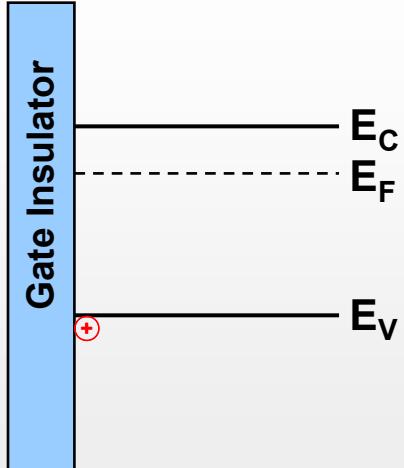
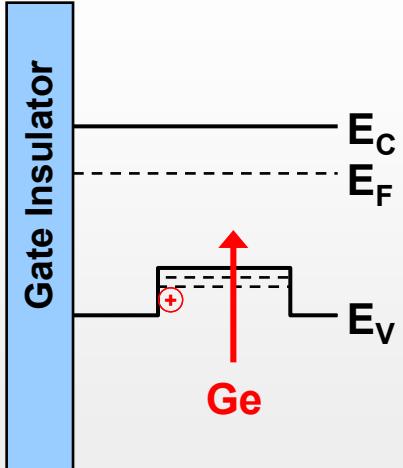
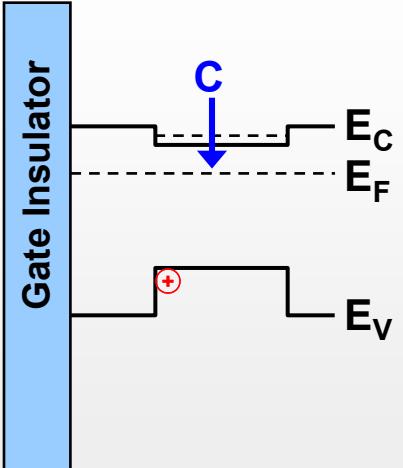
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**(Thursday 27 May 2004)**

# Outline

- **Performance of SiGeC MOSFETs**
  - ✿ Comparison Si : SiGe : SiGeC
- **Experimental results**
  - ✿ DC and LFN experiments
  - ✿ Trends, variations, modeling
- **Discussion on LFN behavior**
  - ✿ Noise scaling
  - ✿  $\Delta N$  model, trap density
- **Conclusions**

# Comparison Si : SiGe : SiGeC

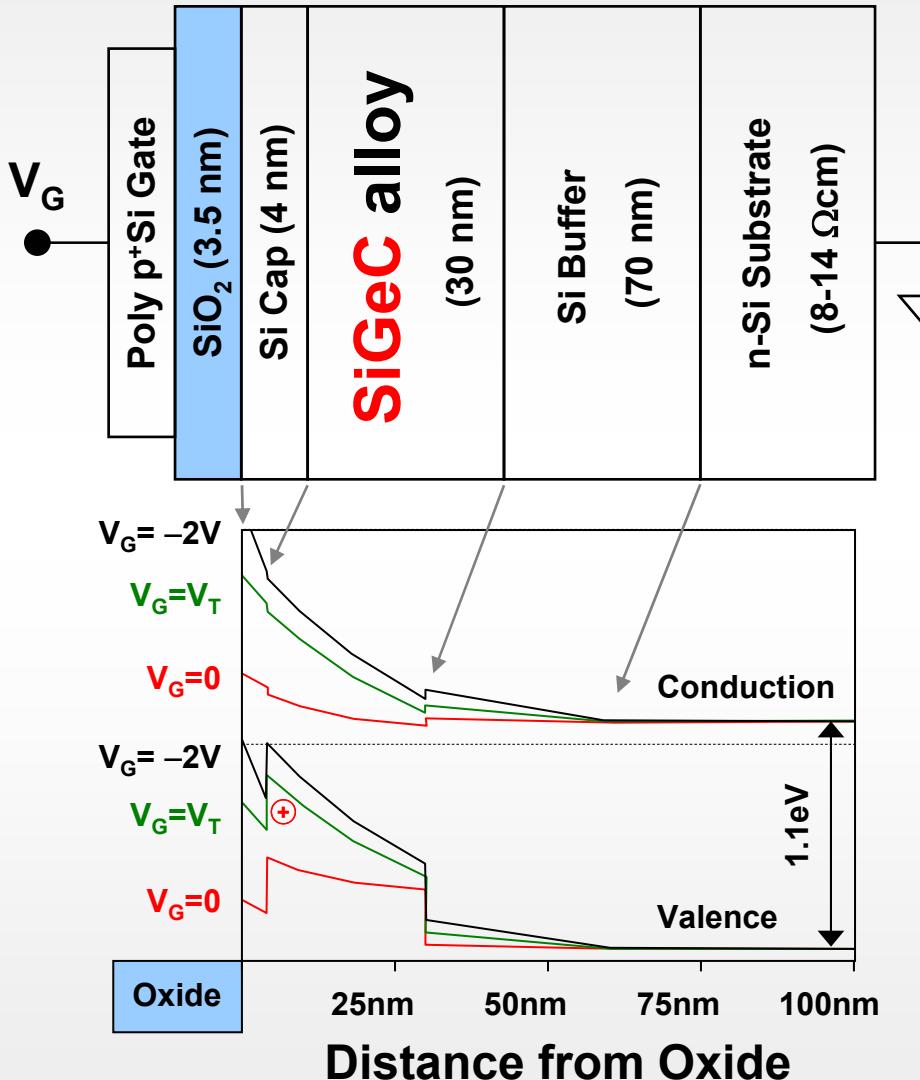
	<u>Si</u>	<u>SiGe</u>	<u>SiGeC</u>
● Mobility	$\mu_n/3$	$\sim\mu_n$	$\sim\mu_{\text{SiGe}}$
● Strain	No	High	Relaxed
● Gap Tuning			

# Low-Freq. Noise in pMOSFETs

	<u>Si</u>	<u>SiGe</u>	<u>SiGeC</u>
• $\Delta N$	?	$S_{ID} = S_{VG} g_m^2$	?
• $\Delta \mu$	Yes	Sometimes	?
• $S_{ID} \propto 1/\text{Area}$	Yes	Yes	?

A. Lambert, *et al*, TED, 46(7), 1484 (1999)

# SiGeC pMOSFET Samples



- Alloy

- $\text{SiGe}_{40\%}\text{C}_{1.5\%}$
- $\text{SiGe}_{40\%}\text{C}_{1\%}$
- $\text{SiGe}_{40\%}\text{C}_{0.5\%}$
- $\text{SiGe}_{40\%}$
- Si

- Channel Sizes

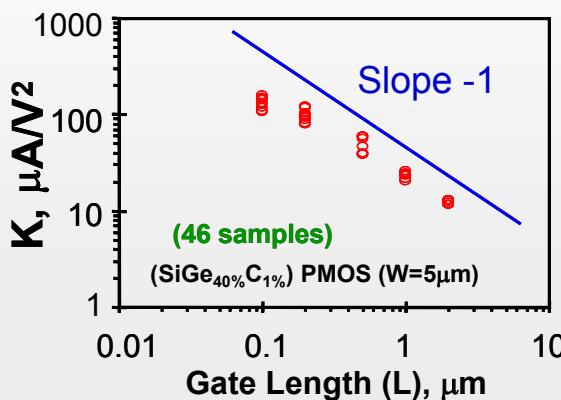
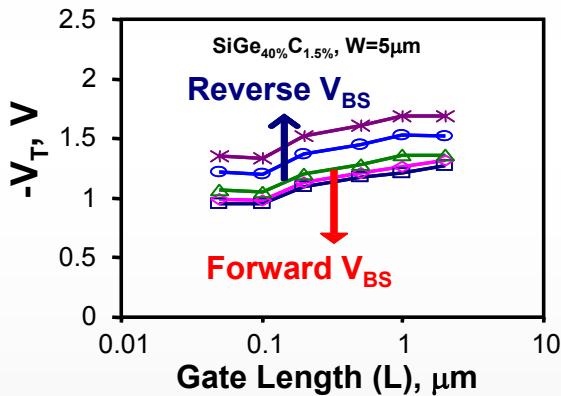
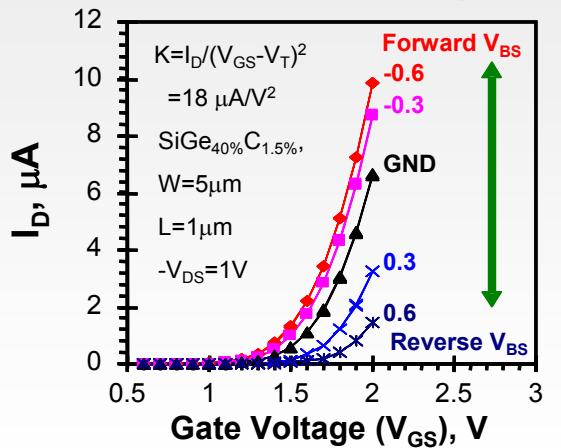
- Width (W)= 5 μm
- Length (L)=0.1-2μm

- Number of Samples

- DC: more than 200
- LFN: more than 20

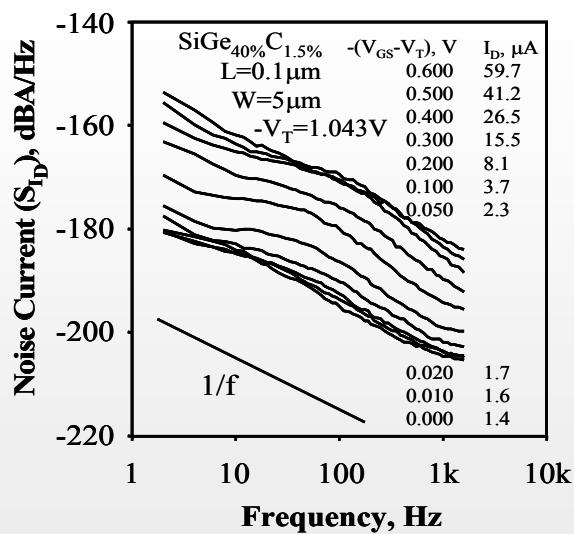
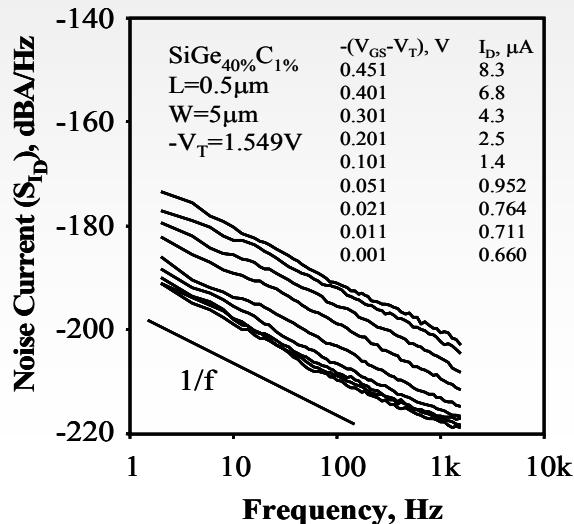
- Data Files ~ 3000

# DC Experiments



- Wafer Mapping
  - ✿ Le leakages
  - ✿ Proper I-V
- Transfer I-V Curves
  - ✿  $V_{GS} = |V_T - 0.3V| \dots -2V$
  - ✿  $V_{DS} = -1V \dots -50mV$
  - ✿  $V_{BS} = -0.6 \dots +0.6V$
- DC Modeling
  - ✿ Strong to Weak Inversion
  - ✿ Parameter Extraction
- Statistics
  - ✿  $V_T(V_{BS})$ ,  $g_m$ (bias)
  - ✿  $K = I_D / |V_{GS} - V_T|^2$

# 1/f and Lorentzian LF Noise



## ● Biasing

- \*  $V_{GS} = |V_T - 0.1V| \dots -2V$
- \*  $V_{DS} = -1V \dots -50mV$
- \*  $V_{BS} = -0.6 \dots +0.6V$

## ● $S_{ID}$ Spectra (about 800)

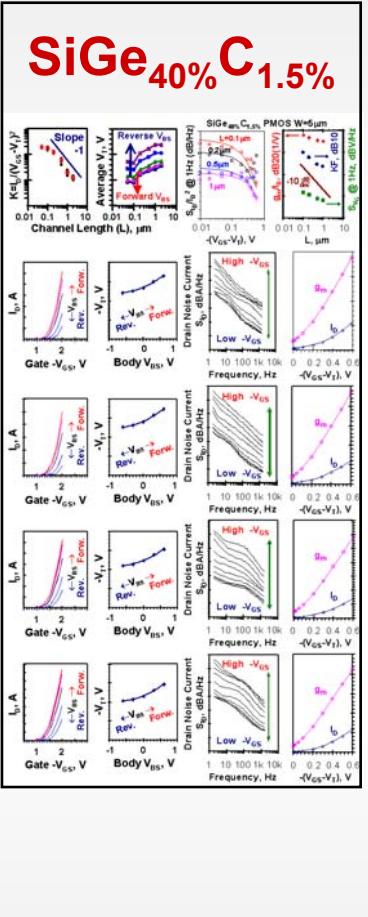
- \* 2Hz – 1.6kHz
- \*  $S_{ID}/I_D^2, S_{ID}/g_m^2$

## ● Corresponding DC

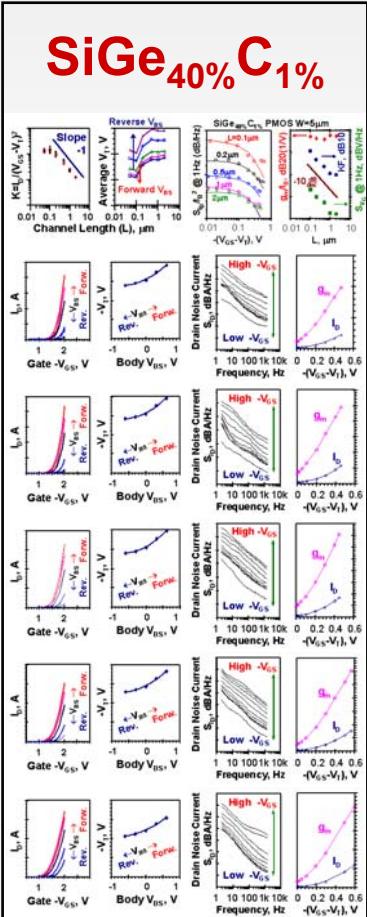
- \*  $V_{GS}, V_{GS}-V_T$
- \*  $I_D$
- \*  $g_m$

# Extensive DC and LFN Data

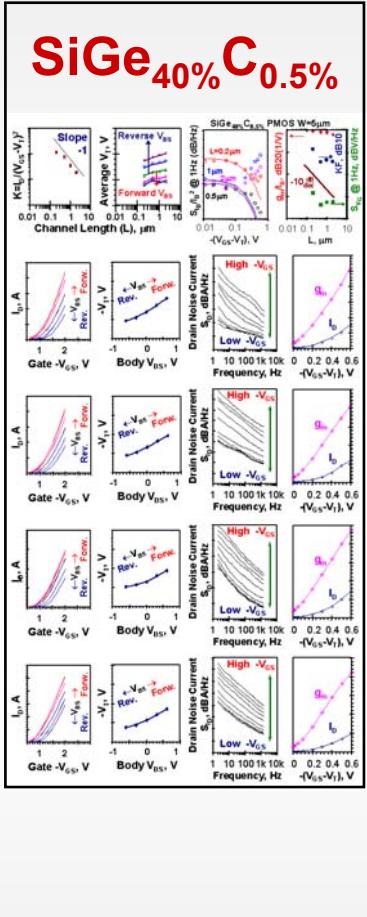
**SiGe<sub>40%</sub>C<sub>1.5%</sub>**



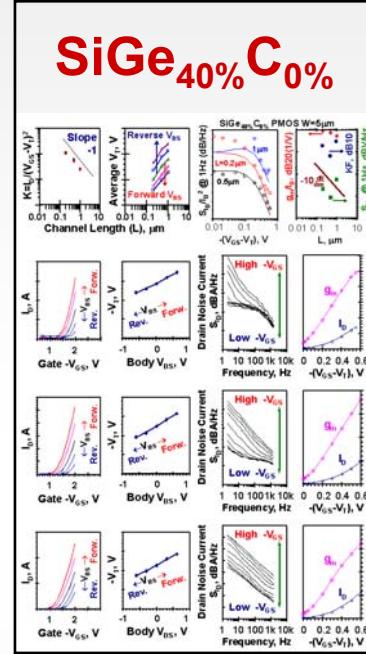
**SiGe<sub>40%</sub>C<sub>1%</sub>**



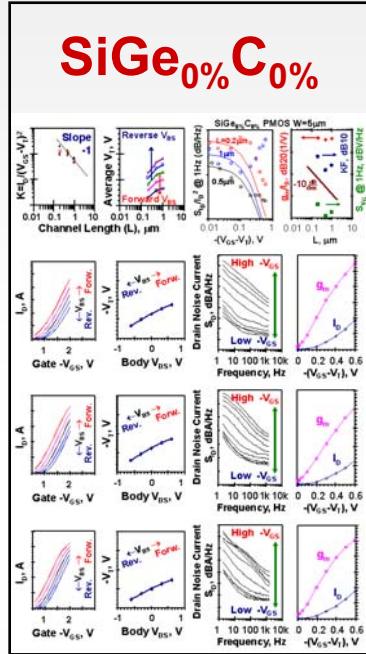
**SiGe<sub>40%</sub>C<sub>0.5%</sub>**



**SiGe<sub>40%</sub>C<sub>0%</sub>**



**SiGe<sub>0%</sub>C<sub>0%</sub>**

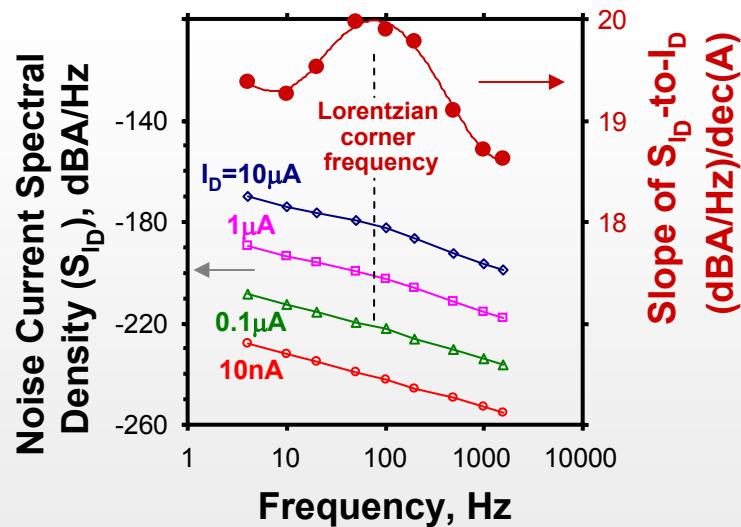
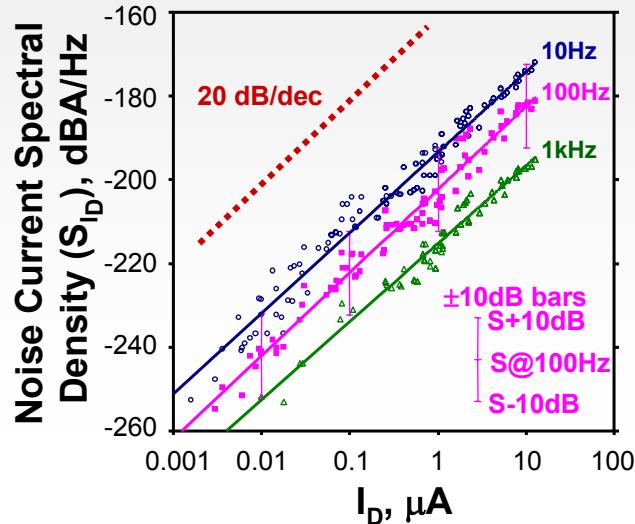


Numerical data available through [www.RDIE.ca](http://www.RDIE.ca)

Marinov, et al, [www.RDIE.ca](http://www.RDIE.ca), 1(1), 1 (2004)

# Trend of Noise Results

(SiGe<sub>40%</sub>C<sub>1.5%</sub>) PMOS (W=5μm, L=1μm)



Despite variations

- $S_{ID} \propto I_D^2$

- $S_{ID}$  spectra  $\sim 1/f$

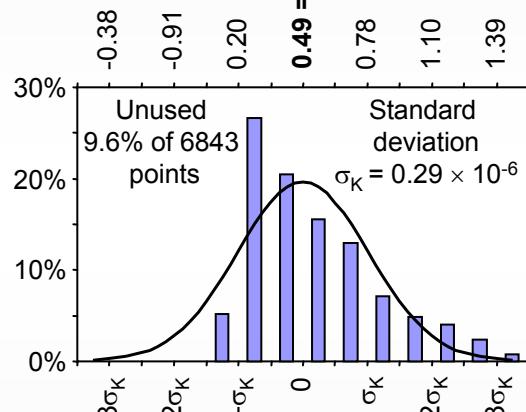
$$(S_{ID})_{avg} = (K_F)_{avg} \frac{I_D^2}{f}$$

# Distribution - $K_F = S_{ID} \times f / I_D^2$

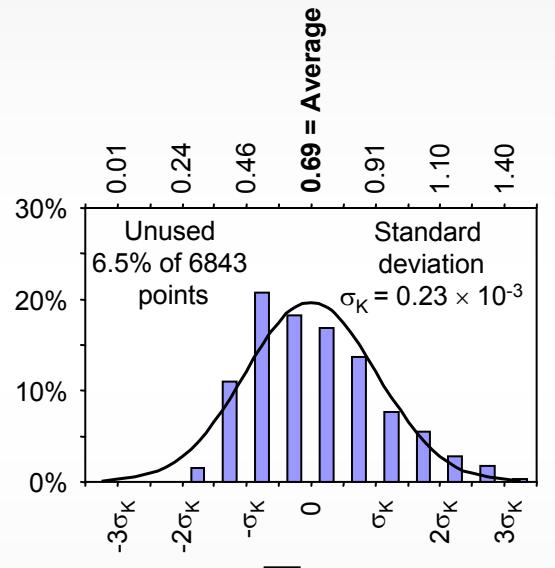
(SiGe<sub>40%</sub>C<sub>1.5%</sub>) PMOS (W=5μm, L=1μm)

Relative Frequency  
of Occurrence

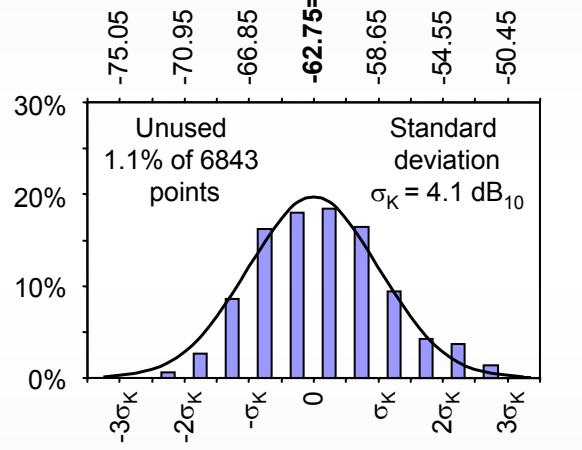
$K_F$ , a.u. × 10<sup>-6</sup>



$\sqrt{K_F}$ , a.u. × 10<sup>-3</sup>



$K_F$ , dB<sub>10</sub>



Averaging of  
 $K_F$  fails

Averaging of  
Noise Power  $S \cdot f / I^2$

*fails*

Averaging of  
 $\sqrt{K_F}$  fails

Averaging of  
Noise Current  $i \cdot \sqrt{f / I}$

*fails*

Log-Normal Noise  
 $\log(S \cdot f / I^2)$   
applies

# Log-Normal LFN Model

- Exponential-Logarithmic form for noise equation

## ★ Exponential

$$S_{I_D}(f, \text{bias}) = \frac{(K_F)_{\text{avg}} \cdot I_D^2(\text{bias})}{f} 10^{\pm t \cdot \sigma_{\text{dB}} / 10 \text{dB}} = \frac{(K_F)_{\text{avg}} \cdot I_D^2(\text{bias})}{f} \exp(\pm t \cdot \sigma_{Np}); \sigma_{Np} \approx 0.23 \sigma_{\text{dB}}$$

## ★ Logarithmic

$$S_{I_D}(f, \text{bias})_{\text{dB}} = (K_{F,\text{dB}})_{\text{avg}} + 20 \text{dB} \cdot \log_{10}(I_D) - 10 \text{dB} \cdot \log_{10}(f) \pm t \cdot \sigma_{\text{dB}}$$

- Noise averaging

$$(K_{F,\text{dB}})_{\text{avg}} = \frac{10 \text{dB}}{N} \sum_{j=1}^N \log_{10} \left( \frac{S_{I_D}}{I_D^2} f \right)_j$$

## ★ Geometric (arithmetic in dB)

$$\sigma_{\text{dB}} = \sqrt{\frac{1}{N-1} \sum_{j=1}^N \left[ 10 \text{dB} \cdot \log_{10} \left( \frac{S_{I_D}}{I_D^2} f \right)_j - (K_{F,\text{dB}})_{\text{avg}} \right]^2}$$

- Model parameters

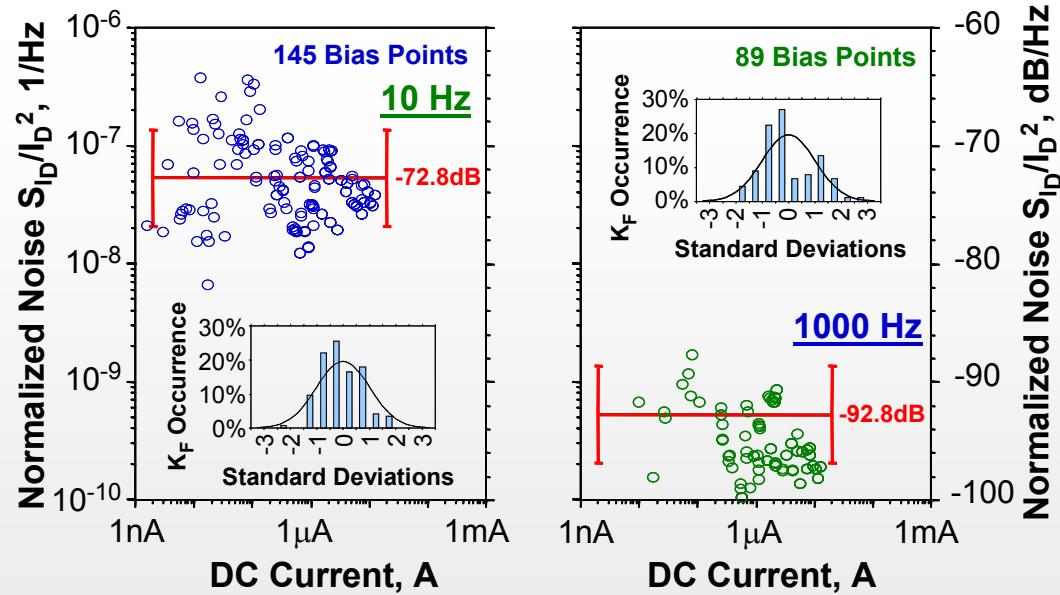
★ Average Noise:  $K_F = 10^{(K_{F,\text{dB}})/10 \text{dB}}$

★ Log-Normal deviation:  $\sigma_{\text{dB}}$

★  $t=(1, \dots, 3)$  for confidence probability (60%, ..., 99%)

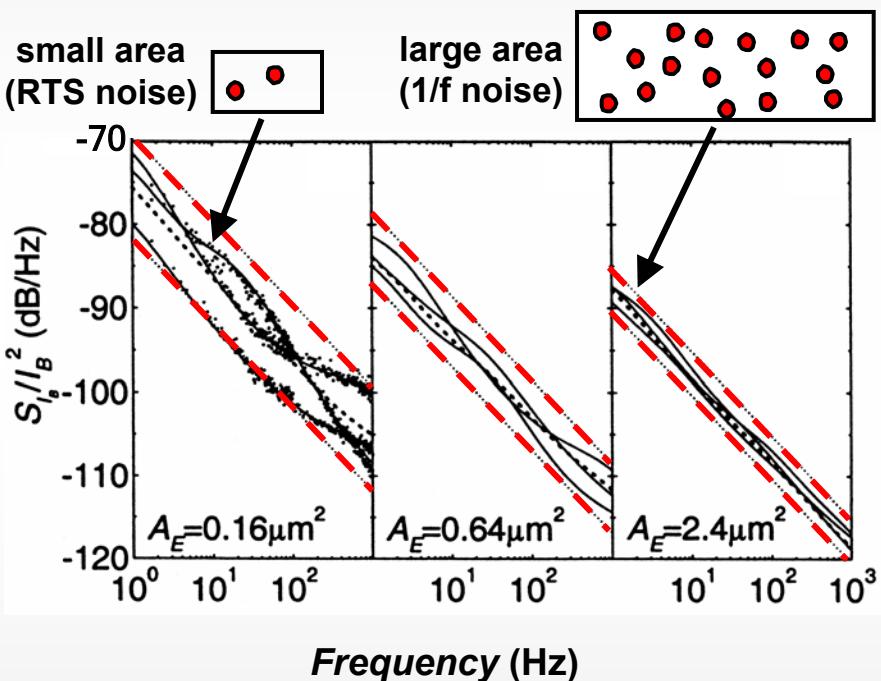
# Population Requirements

- $N > 250$  for  $K_F$  and  $\sigma_K$  evaluation
  - ✿ Frequency points  $\geq 30$
  - ✿ Bias points  $\geq 8$
- $N > 2000$  for inspection of distribution
  - ✿ Frequency points  $\geq 50$
  - ✿ Bias points  $\geq 60$
- Small Population:



# Similarity to PE-BJT

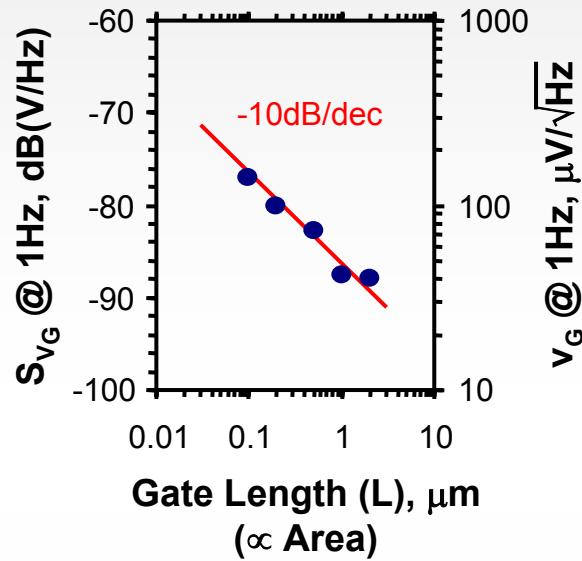
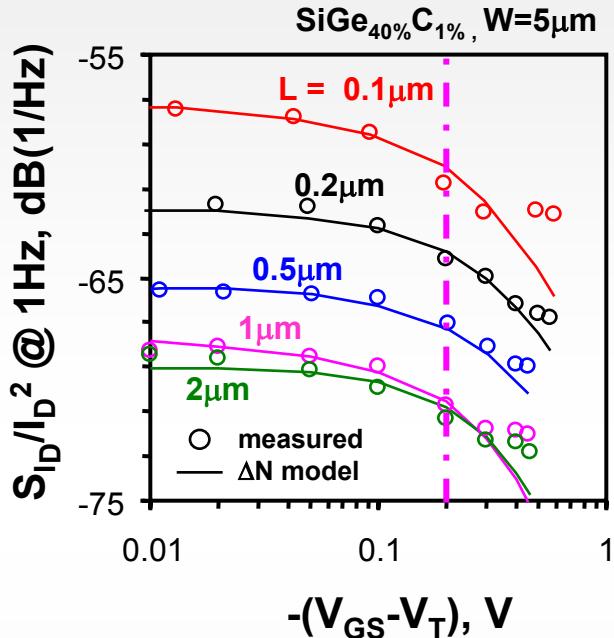
M. Sanden, et al, TED, 49(3), 514 (2002)



- $S_{I,\text{avg}} \propto 1/f$
- $S_{I,\text{avg}} \propto I_{DC}^2$
- $S_{I,\text{avg}} \propto 1/\text{Area}$
- $S_{I,\text{dev}} \propto 10^{(t \times \sigma_{\text{dB}} / 10 \text{dB})}$

## $\Delta N$ noise?

# $\Delta N$ model for LFN



$$\frac{S_{ID}}{I_D^2} = S_{VG} \left( \frac{g_m}{I_D} \right)^2$$

$$g_m^2 = (g_{m,\text{SiGeC}} + g_{m,\text{cap}})^2$$

$$S_{VG} = S_{FB} \propto 1/\text{Area}$$

G. Ghibaudo, et al, SSE, 46, 393 (2002)

Number fluctuation in all samples for  
 $|V_{GS}-V_T| < 0.2\text{V}$

# Conclusion

- Experiments of SiGeC pMOSFETs
  - ✿ Detailed LFN measurements
  - ✿ Necessary DC characterization
- $\Delta N$  noise for  $|V_{GS} - V_T| < 0.2V$ 
  - ✿ LFN can be referred to gate terminal
  - ✿ Trade-off between noise performance and GeC concentration
- Noise scaling
  - ✿  $(S_{ID})_{avg} \propto I_D^2 / (f \times \text{Area})$
  - ✿ Log-normal distribution  $\Rightarrow$  averaging and deviation in dB
- Several factors contribute to LFN at increased gate biasing  $|V_{GS} - V_T| > 0.4V$

