

LECTURE 12: Loop Antennas

(Radiation parameters of a small loop. Circular loop of constant current. Equivalent circuit of the loop antenna. The small loop as a receiving antenna. Ferrite loops.)

1. Introduction

Loop antennas feature simplicity, low cost and versatility. They may have various shapes: circular, triangular, square, elliptical, etc. They are widely used in communication links up to the microwave bands (up to ≈ 3 GHz). They are also used as electromagnetic (EM) field probes in the microwave bands.

Loop antennas are usually classified as electrically small ($C < 0.1\lambda$) and electrically large ($C \sim \lambda$). Here, C denotes the loop's circumference. Electrically small loops of a single turn have very small radiation resistance (comparable to their loss resistance). Their radiation resistance can be substantially improved by adding more turns. Multi-turn loops have better radiation resistance although their efficiency is still poor. That is why they are used mostly as receiving antennas where losses are not so important. The radiation characteristics of a small loop antenna can be additionally improved by inserting a ferromagnetic core. Radio-receivers of AM broadcast are usually equipped with ferrite-loop antennas. Such antennas are used in pagers, too.

The small loops, regardless of their shape, have a far-field pattern very similar to that of a small electric dipole (normal to the plane of the loop). This is expected because they are equivalent to a magnetic dipole. Note, however, that the field polarization is orthogonal to that of the electric dipole.

As the circumference of the loop increases, the pattern maximum shifts towards the loop's normal, and when $C \approx \lambda$, the maximum of the pattern is at the loop's normal.

2. Radiation parameters of a small loop

A small loop is a loop of constant current whose radius satisfies

$$a < \frac{\lambda}{6\pi}, \quad (12.1)$$

or, whose circumference C satisfies $C < \lambda/3$. The limit (12.1) is mathematically derived later in this Lecture from the first-order approximation

of the Bessel function of the first order $J_1(x)$ in the general solution for a loop of constant current. Actually, to make sure that the current has constant distribution along the loop, a tighter limit must be imposed:

$$a < 0.03\lambda, \quad (12.2)$$

or, $C < \lambda / 5$. A good approximation of a small loop is the infinitesimal loop (or the infinitesimal magnetic dipole).

The expressions for the field of an infinitesimal loop of electric current of area A were already derived in Lecture 3. Here, we give only the far-field components of its field when the loop's normal is along the z -axis:

$$E_\varphi = \eta\beta^2 \cdot (IA) \cdot \frac{e^{-j\beta r}}{4\pi r} \cdot \sin\theta, \quad (12.3)$$

$$H_\theta = -\beta^2 \cdot (IA) \cdot \frac{e^{-j\beta r}}{4\pi r} \cdot \sin\theta. \quad (12.4)$$

It is obvious that the far-field pattern,

$$\bar{E}_\varphi(\theta) = \sin\theta, \quad (12.5)$$

is identical to that of a z -directed infinitesimal dipole. The loop's field polarization is orthogonal to that of the dipole. The power pattern is identical to that of the infinitesimal electric dipole:

$$F(\theta) = \sin^2\theta. \quad (12.6)$$

Radiated power:

$$\begin{aligned} \Pi &= \oint\oint \frac{1}{2\eta} |E_\varphi|^2 \cdot \underbrace{r^2 \sin\theta d\theta d\varphi}_{ds}, \\ \Pi &= \frac{1}{12\pi} \eta\beta^4 (IA)^2. \end{aligned} \quad (12.7)$$

Radiation resistance:

$$R_r = \eta \frac{8}{3} \pi^3 \left(\frac{A}{\lambda^2} \right)^2. \quad (12.8)$$

In free space, $\eta = 120\pi \Omega$, and

$$R_r \approx 31171(A / \lambda^2)^2. \quad (12.9)$$

Equation (12.9) gives the radiation resistance of a single loop. If the loop antenna has N turns, then the radiation resistance increases with a factor of N^2 :

$$R_r = \eta \frac{8}{3} \pi^3 \left(N \frac{A}{\lambda^2} \right)^2. \quad (12.10)$$

The relation in (12.10) provides a handy mechanism to increase R_r and the radiated power Π . Unfortunately, the losses of the loop antenna also increase (although only as $\sim N$). Typically, loop antennas have low efficiency.

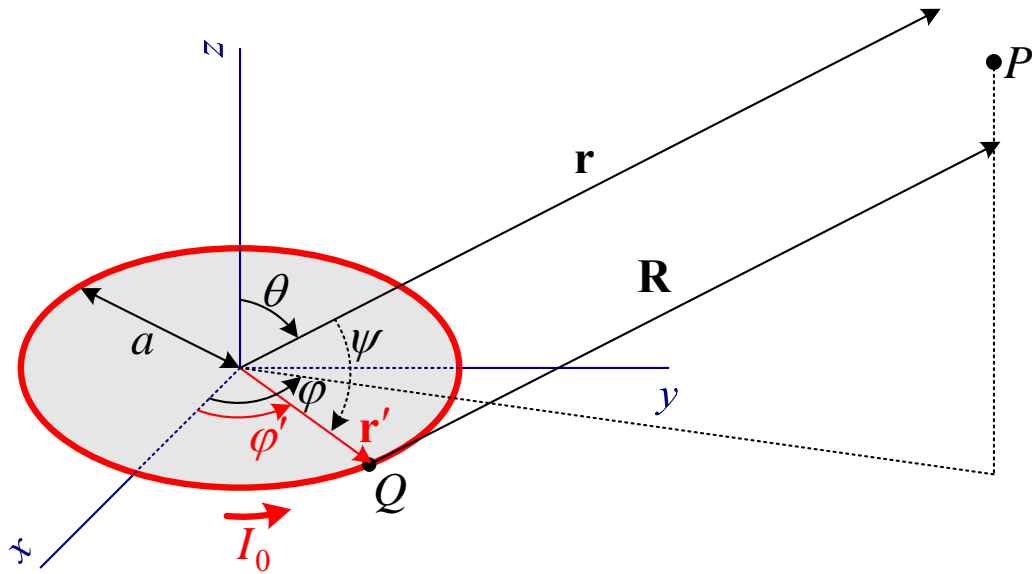
The directivity is the same as that of an infinitesimal dipole:

$$D_0 = 4\pi \frac{U_{\max}}{\Pi_{rad}} = 1.5. \quad (12.11)$$

3. Circular loop of constant current – general solution

So far, we have assumed that the loop is of infinitesimal radius a , which allowed the use of the expressions for the infinitesimal magnetic dipole. Now, we derive the far field of a circular loop, which might not be necessarily very small, but still has constant current distribution. This derivation illustrates the general approach to the loop antenna analysis. This approach is used in the solutions to circular loop problems of nonuniform distributions, too.

The circular loop can be divided into an infinite number of infinitesimal current elements. The position of a current element in the xy plane is characterized by $0^\circ \leq \varphi' < 360^\circ$ and $\theta' = 90^\circ$. The position of the observation point P is defined by (θ, φ) .



The far-field approximations are

$$\left\{ \begin{array}{l} R \approx r - a \cos \psi, \text{ for the phase term,} \\ \frac{1}{R} \approx \frac{1}{r}, \text{ for the amplitude term.} \end{array} \right. \quad (12.12)$$

In general, the solution for \mathbf{A} does not depend on φ because of the cylindrical symmetry of the problem. Set $\varphi = 0$. The angle between the position vector of the source point Q and that of the observation point P is determined as

$$\begin{aligned} \cos \psi &= \hat{\mathbf{r}} \cdot \hat{\mathbf{r}}' = (\hat{\mathbf{x}} \sin \theta \cos \varphi + \hat{\mathbf{y}} \sin \theta \sin \varphi + \hat{\mathbf{z}} \cos \theta) \cdot (\hat{\mathbf{x}} \cos \varphi' + \hat{\mathbf{y}} \sin \varphi'), \\ &\Rightarrow \cos \psi = \sin \theta \cos \varphi'. \end{aligned} \quad (12.13)$$

Now the vector potential integral can be solved for the far zone:

$$\mathbf{A}(r, \theta, \varphi) = \frac{\mu}{4\pi c} \oint I_0 \frac{e^{-j\beta(r - a \sin \theta \cos \varphi')}}{r} d\mathbf{l} \quad (12.14)$$

where $d\mathbf{l} = \hat{\boldsymbol{\phi}}' a d\varphi'$ is the linear element of the loop contour. The current element changes its direction along the loop and its contribution depends on the angle between its direction and the respective \mathbf{A} component. The problem is cylindrically symmetrical thus it is appropriate to represent it through the A_φ

component where $\mathbf{A} = A_\varphi \hat{\boldsymbol{\phi}}$:

$$A_\varphi(\theta, \varphi) = \frac{\mu}{4\pi} (I_0 a) \frac{e^{-j\beta r}}{r} \int_0^{2\pi} (\hat{\boldsymbol{\phi}} \cdot \hat{\boldsymbol{\phi}}') e^{j\beta a \sin \theta \cos \varphi'} d\varphi'. \quad (12.15)$$

Since

$$\begin{aligned} \hat{\boldsymbol{\phi}} \cdot \hat{\boldsymbol{\phi}}' &= (\hat{\mathbf{x}} \cos \varphi + \hat{\mathbf{y}} \sin \varphi) \cdot (\hat{\mathbf{x}} \cos \varphi' + \hat{\mathbf{y}} \sin \varphi') = \\ &= \cos \varphi \cos \varphi' + \sin \varphi \sin \varphi' = \\ &= \cos(\varphi - \varphi') \Big|_{\varphi=0} = \cos \varphi', \end{aligned} \quad (12.16)$$

the vector potential is

$$A_\varphi(\theta, 0) = \frac{\mu}{4\pi} (I_0 a) \frac{e^{-j\beta r}}{r} \int_0^{2\pi} \cos \varphi' \cdot e^{j\beta a \sin \theta \cos \varphi'} d\varphi', \quad (12.17)$$

$$A_\varphi(\theta) = \frac{\mu}{4\pi} (I_0 a) \frac{e^{-j\beta r}}{r} \left[\int_0^\pi \cos \varphi' \cdot e^{j\beta a \sin \theta \cos \varphi'} d\varphi' + \int_\pi^{2\pi} \cos \varphi' \cdot e^{j\beta a \sin \theta \cos \varphi'} d\varphi' \right].$$

We apply the following substitution in the second integral: $\varphi' = \varphi'' + \pi$. Then,

$$A_\varphi(\theta) = \frac{\mu I_0 a}{4\pi} \frac{e^{-j\beta r}}{r} \left[\int_0^\pi \cos \varphi' \cdot e^{j\beta a \sin \theta \cos \varphi'} d\varphi' - \int_0^\pi \cos \varphi'' \cdot e^{-j\beta a \sin \theta \cos \varphi''} d\varphi'' \right]. \quad (12.18)$$

The integrals in (12.18) can be expressed in terms of Bessel functions, which are defined as

$$\int_0^\pi \cos(n\varphi) e^{jz \cos \varphi} d\varphi = \pi j^n J_n(z). \quad (12.19)$$

Here, $J_n(z)$ is the Bessel function of the first kind of order n . From (12.18) and (12.19), it follows that

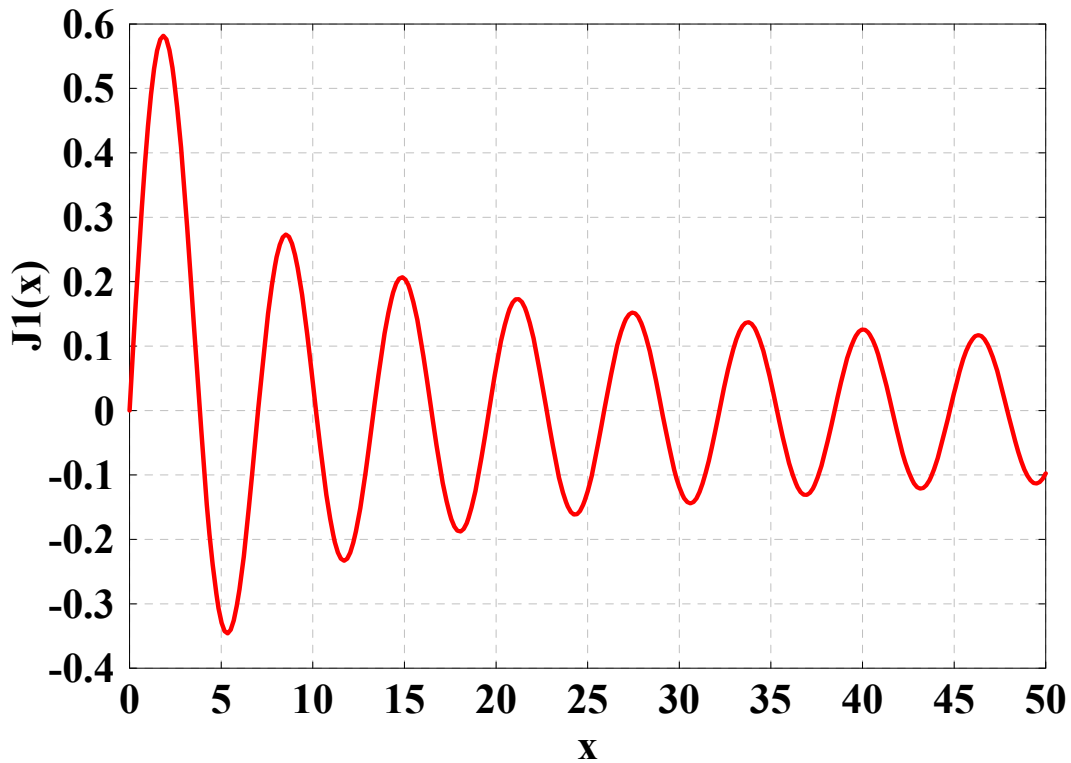
$$A_\varphi(\theta) = \frac{\mu}{4\pi} (I_0 a) \frac{e^{-j\beta r}}{r} \pi j \left[J_1(\beta a \sin \theta) - J_1(-\beta a \sin \theta) \right]. \quad (12.20)$$

Since

$$J_n(-z) = (-1)^n J_n(z), \quad (12.21)$$

equation (12.20) reduces to

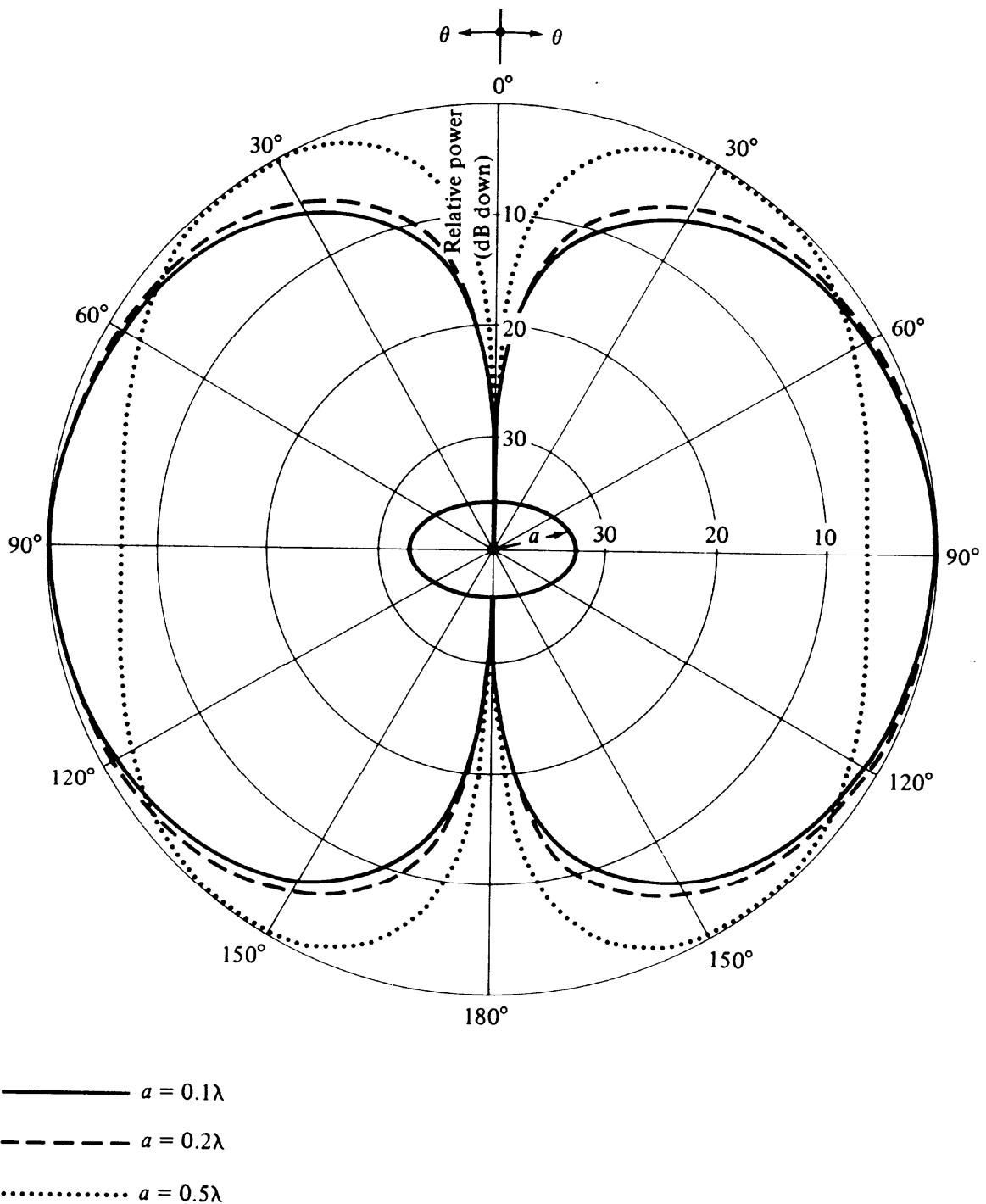
$$A_\varphi(\theta) = j \frac{\mu}{2} (I_0 a) \frac{e^{-j\beta r}}{r} J_1(\beta a \sin \theta). \quad (12.22)$$



The far-zone fields are derived as

$$\left| \begin{aligned} E_\varphi(\theta) &= \beta \eta (I_0 a) \frac{e^{-j\beta r}}{2r} J_1(\beta a \sin \theta), \\ H_\theta(\theta) &= -\frac{E_\varphi}{\eta} = -\beta (I_0 a) \frac{e^{-j\beta r}}{2r} J_1(\beta a \sin \theta). \end{aligned} \right. \quad (12.23)$$

The patterns of constant-current loops as per (12.23) are shown below:



The small-loop field solution in (12.3)-(12.4) is actually a first-order approximation of the solution in (12.23). This becomes obvious when the Bessel function is expanded in series as

$$J_1(\beta a \sin \theta) = \frac{1}{2}(\beta a \sin \theta) - \frac{1}{16}(\beta a \sin \theta)^3 + \dots \quad (12.24)$$

For small values of the argument ($\beta a < 1/3$), the first-order approximation is acceptable, i.e.,

$$J_1(\beta a \sin \theta) \approx \frac{1}{2}(\beta a \sin \theta). \quad (12.25)$$

The substitution of (12.25) in (12.23) yields (12.3)-(12.4).

It can be shown that the maximum of the pattern given by (12.23) is in the direction $\theta = 90^\circ$ for all loops, which have circumference $C < 1.84\lambda$.

Radiated power and radiation resistance

We substitute the E_φ expression (12.23) in

$$\Pi = \oint\oint \frac{1}{2\eta} |E_\varphi|^2 \cdot \underbrace{r^2 \sin \theta d\theta d\varphi}_{ds},$$

which yields

$$\Pi = \frac{(\omega\mu)^2}{4\eta} (I_0^2 A) \cdot \int_0^\pi J_1^2(\beta a \sin \theta) \sin \theta d\theta. \quad (12.26)$$

Here, $A = \pi a^2$ is the loop's area. The integral in (12.26) does not have a closed form solution. Often, the following transformation is applied:

$$\int_0^\pi J_1^2(\beta a \sin \theta) \sin \theta d\theta = \frac{1}{\beta a} \int_0^{2\beta a} J_2(x) dx. \quad (12.27)$$

The second integral in (12.27) does not have a closed form solution either but it can be approximated with highly convergent series, e.g.,

$$\int_0^{2\beta a} J_2(x) dx = 2 \sum_{m=0}^{\infty} J_{2m+3}(2\beta a). \quad (12.28)$$

The radiation resistance is obtained as

$$R_r = \frac{2\Pi}{I_0^2} = \frac{(\omega\mu)^2}{2\eta} A \cdot \int_0^\pi J_1^2(\beta a \sin \theta) \sin \theta d\theta. \quad (12.29)$$

The radiation resistance of small loops is very small. For example, for $\lambda/100 < a < \lambda/30$ the radiation resistance increases from $\approx 3 \times 10^{-3}$ up to

$\approx 0.5 \Omega$. This is often less than the loss resistance of the loop. That is why small loop antennas are constructed with multiple turns and on a ferromagnetic core. Such loop antennas have large inductive reactance, which is compensated by a capacitor. This is convenient in narrowband receivers, where the antenna itself is a very efficient filter (together with the tuning capacitor), which can be tuned for different frequency bands.

4. Circular loop of nonuniform current

When the loop radius becomes larger than 0.2λ , the constant-current assumption does not hold. A common assumption is the cosine distribution.^{1,2} Lindsay, Jr.,³ considers the circular loop to be a deformation of a shorted parallel-wire line. If I_s is the current magnitude at the “shorted” end, i.e., the point opposite to the feed point where $\varphi' = \pi$, then

$$I(\alpha) = I_s \cosh(\gamma a \alpha) \quad (12.30)$$

where $\alpha = \pi - \varphi'$ is the angle with respect to the shorted end, γ is the line propagation constant and a is the loop radius. If we assume loss-free transmission-line model, then $\gamma = j\beta$ and $\cosh(\gamma a \alpha) = \cos(\beta a \alpha)$. For a loop in open space, β is assumed to be the free-space wave number ($\beta = \omega\sqrt{\mu_0\epsilon_0}$).

The cosine distribution is not very accurate, especially close to the terminals, and this has a negative impact on the accuracy of the computed input impedance. That is why the current is often represented by a Fourier series:^{4,5}

$$I(\varphi') = I_0 + 2 \sum_{n=1}^N I_n \cos(n\varphi'). \quad (12.31)$$

Here, φ' is measured from the feed point. The complete analysis of this general case will be left out, and only some important results will be given. When the circumference of the loop approaches λ , the maximum of the radiation pattern shifts exactly along the loop's normal. Then, the input resistance of the antenna is also good (about 50 to 70 Ω). The maximum directivity occurs when

¹ E.A. Wolff, *Antenna Analysis*, Wiley, New York, 1966.

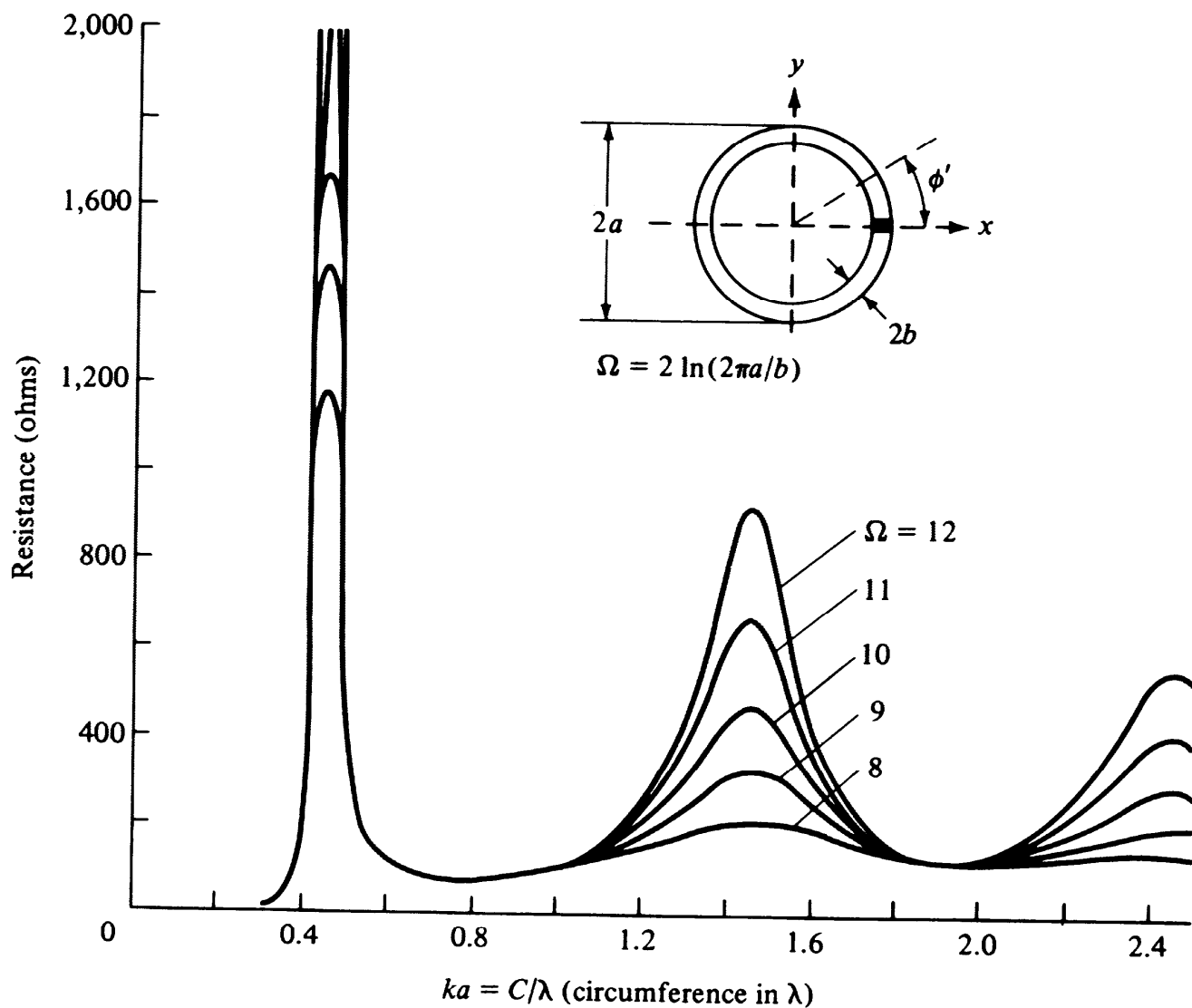
² A. Richtscheid, “Calculation of the radiation resistance of loop antennas with sinusoidal current distribution,” *IEEE Trans. Antennas Propagat.*, Nov. 1976, pp. 889-891.

³ J. E. Lindsay, Jr., “A circular loop antenna with non-uniform current distribution,” *IRE Trans. Antennas Propagat.*, vol. AP-8, No. 4, July 1960, pp. 439-441.

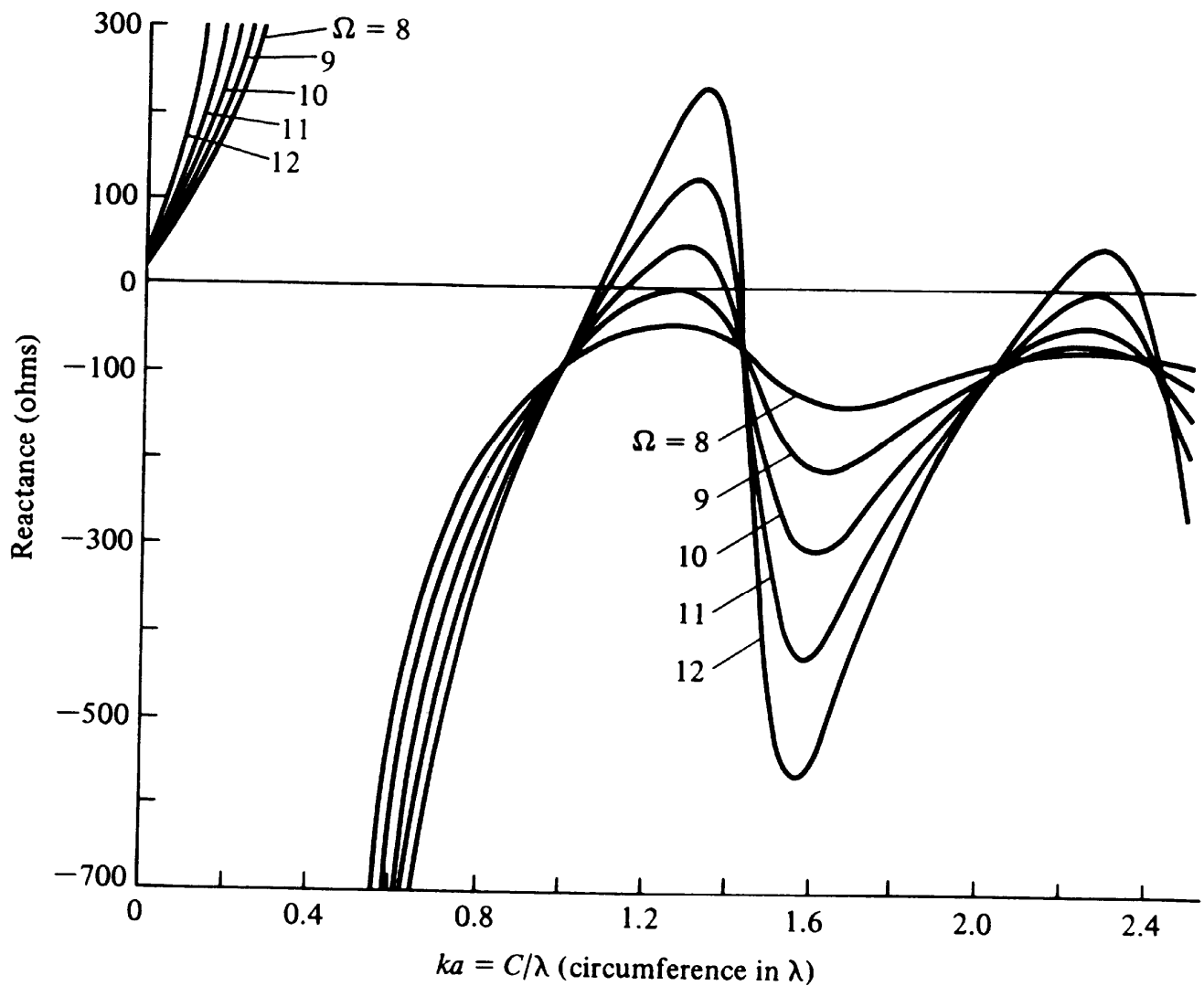
⁴ H. C. Pocklington, “Electrical oscillations in wire,” in *Cambridge Phil. Soc. Proc.*, vol. 9, 1897, pp. 324-332.

⁵ J. E. Storer, “Input impedance of circular loop antennas,” *Am. Inst. Electr. Eng. Trans.*, vol. 75, Nov. 1956.

$C \approx 1.4\lambda$ but then the input impedance is too large. The input resistance and reactance of the large circular loop are given below.



(a) Resistance



(b) Reactance

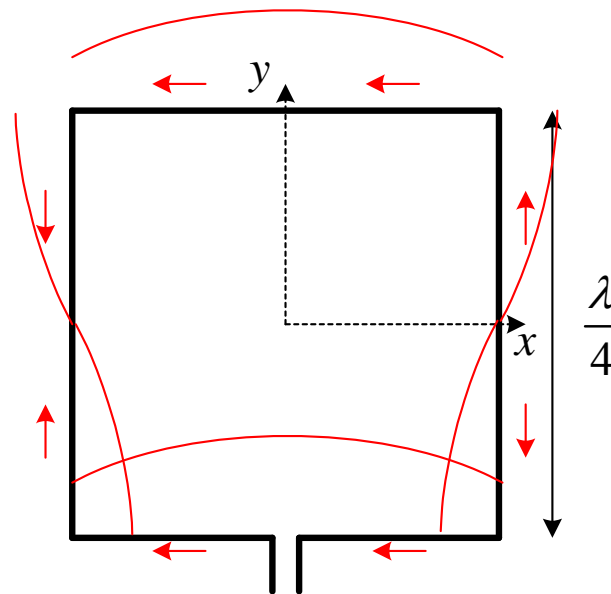
Figure 5.11 Input impedance of circular loop antennas. (SOURCE: J. E. Storer, "Impedance of Thin-Wire Loop Antennas," *AIEE Trans.*, Vol. 75, November 1956. © 1956 IEEE).

(Note: typo in author's name, read as J. E. Storer)

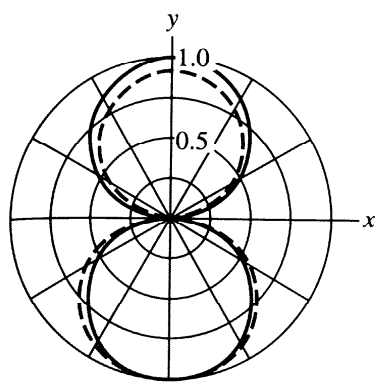
The large circular loop is very similar in its performance to the large square loop. An approximate solution of very good accuracy for the square-loop antenna can be found in

W.L. Stutzman and G.A. Thiele, *Antenna Theory and Design*, 2nd Ed., John Wiley & Sons, New York, 1998.

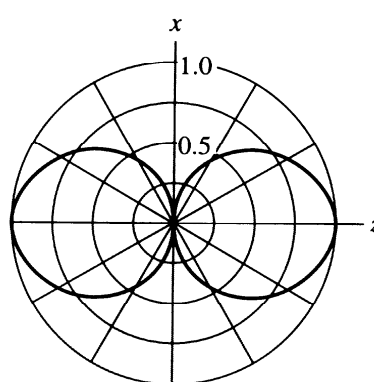
There, it is assumed that the total antenna loop is exactly one wavelength and has a sinusoidal current distribution along the loop's wire.



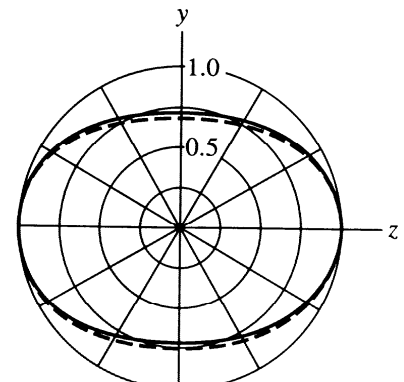
Principal plane patterns obtained through the sinusoidal-current assumption and using numerical methods:



(a) The xy -plane (the plane of the loop and an E -plane) normalized pattern plot of E_ϕ . In this plane, $HP = 94^\circ$.

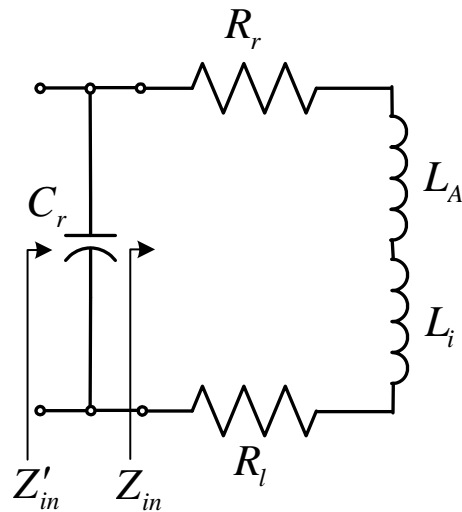


(b) The xz -plane (an E -plane) normalized pattern plot of E_θ . In this plane, $HP = 85^\circ$. The patterns from the two methods coincide in this plane.



(c) The yz -plane (the H -plane) pattern plot of E_ϕ .

5. Equivalent circuit of a loop antenna



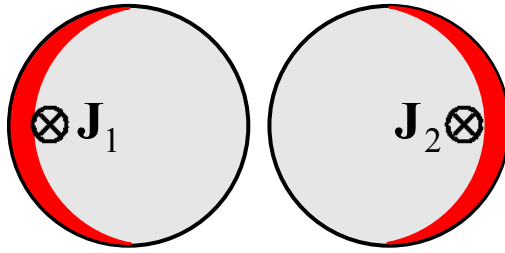
- C_r - resonance capacitor
- R_l - loss resistance of the loop antenna
- R_r - radiation resistance
- L_A - inductance of the loop
- L_i - inductance of the loop conductor (wire)

(a) Loss resistance

Usually, it is assumed that the loss resistance of the loop equals the high-frequency loss resistance of a straight wire of the same length as the loop and of the same current distribution. In the case of a uniform current distribution, the high-frequency resistance is calculated as

$$R_{hf} = \frac{l}{p} R_s, \quad R_s = \sqrt{\frac{\pi f \mu}{\sigma}}, \quad \Omega \quad (12.32)$$

where l is the length of the wire, and p is the perimeter of the wire's cross-section. We are not concerned with the current distribution now because it can be always taken into account in the same way as it is done for the dipole/monopole antennas. However, another important phenomenon has to be taken into account, namely the *proximity effect*.



When the spacing between the wires is very small, the loss resistance due to the proximity effect might be larger than that due to the skin effect. The following formula is used to calculate exactly the loss resistance of a loop with N turns, wire radius b , and loop separation $2c$:

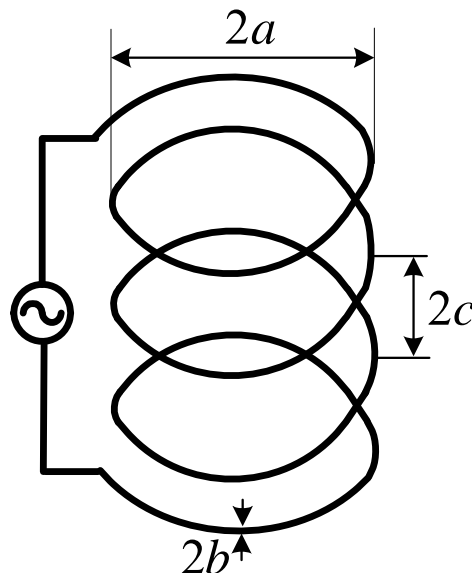
$$R_l = \frac{Na}{b} R_s \left(\frac{R_p}{R_0} + 1 \right) \quad (12.33)$$

where

R_s , Ω , is the surface resistance (see (12.32)),

R_p , Ω / m , is the ohmic resistance per unit length due to the proximity effect,

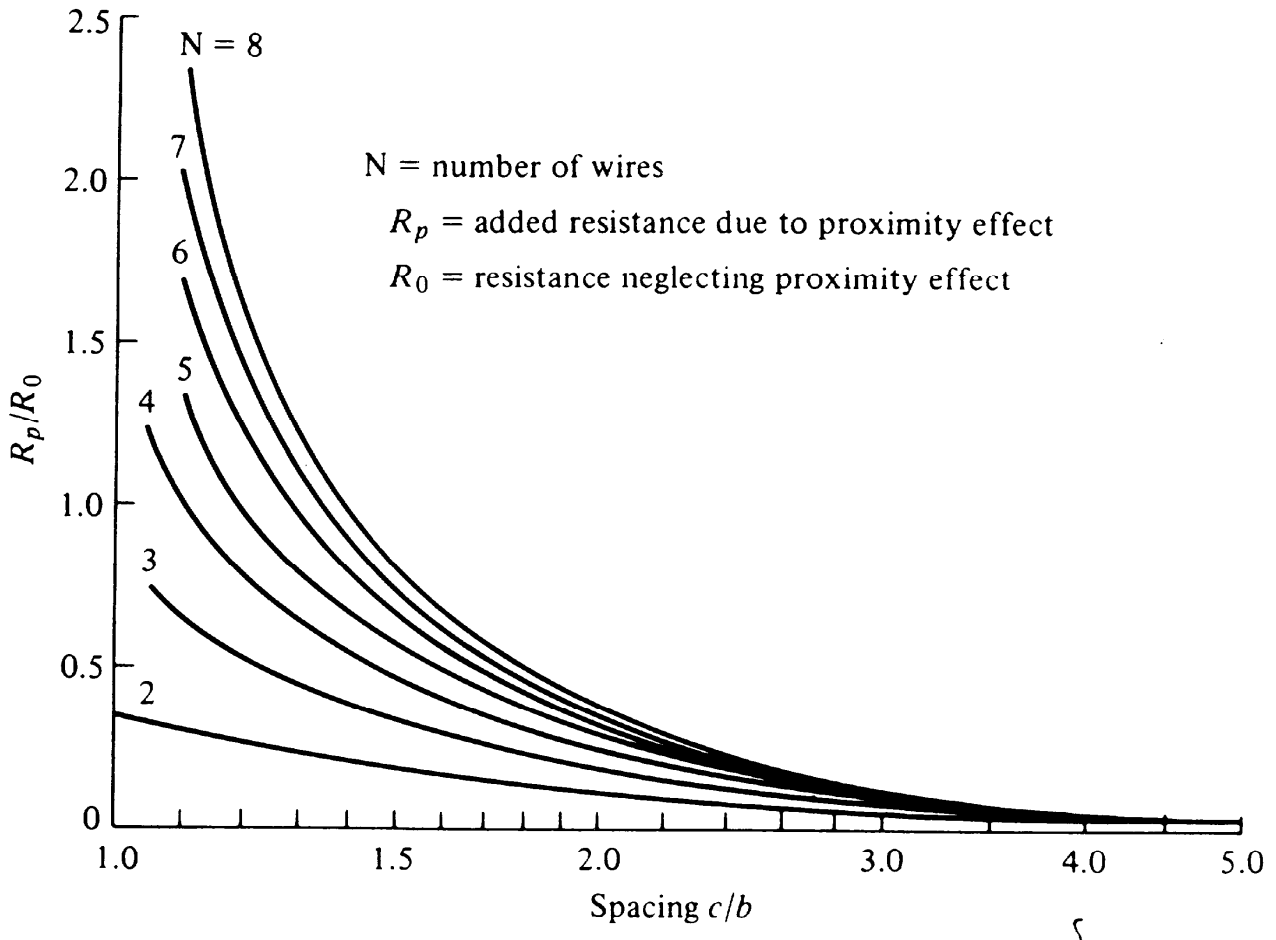
$R_0 = \frac{NR_s}{2\pi b}$, Ω / m , is the ohmic resistance per unit length due to the skin effect.



The ratio R_p / R_0 has been calculated for different relative spacings c / b , for loops with $2 \leq N \leq 8$ in:

G.N. Smith, "The proximity effect in systems of parallel conductors," *J. Appl. Phys.*, vol. 43, No. 5, May 1972, pp. 2196-2203.

The results are shown below:



(b) Ohmic resistance due to proximity (after G. N. Smith)

(b) Loop inductance

The inductance of a single circular loop of radius a made of wire of radius b is

$$L_{A1} = \mu a \left[\ln \left(\frac{8a}{b} \right) - 2 \right]. \quad (12.34)$$

The inductance of a square loop with sides a and wire radius b is calculated as

$$L_{A_1}^{sq} = 2\mu \frac{a}{\pi} \left[\ln\left(\frac{a}{b}\right) - 0.774 \right]. \quad (12.35)$$

The inductance of a multi-turn coil is obtained from the inductance of a single-turn loop multiplied by N^2 , where N is the number of turns.

The inductance of the wire itself is very small and is often neglected. It can be shown that the DC self-inductance of a straight wire of length l is

$$L_i = \frac{\mu_0}{8\pi} \cdot l. \quad (12.36)$$

For a single loop, $l = 2\pi a$.

(c) Tuning capacitor

The susceptance of the capacitor B_r must be chosen to eliminate the susceptance of the loop. The equivalent admittance of the loop is

$$Y_{in} = \frac{1}{Z_{in}} = \frac{1}{R_{in} + jX_{in}} \quad (12.37)$$

where

$$R_{in} = R_r + R_l,$$

$$X_{in} = j\omega(L_A + L_i).$$

The following transformation holds:

$$Y_{in} = G_{in} + jB_{in} \quad (12.38)$$

where

$$\begin{cases} G_{in} = \frac{R_{in}}{R_{in}^2 + X_{in}^2}, \\ B_{in} = \frac{-X_{in}}{R_{in}^2 + X_{in}^2}. \end{cases} \quad (12.39)$$

The susceptance of the capacitor is

$$B_r = \omega C_r. \quad (12.40)$$

For resonance to occur at $f_0 = \omega_0 / (2\pi)$, the condition

$$B_r = -B_{in} \quad (12.41)$$

must be fulfilled. Therefore,

$$2\pi f_0 C_r = \frac{X_{in}}{R_{in}^2 + X_{in}^2}, \quad (12.42)$$

$$\Rightarrow C_r = \frac{1}{2\pi f} \frac{X_{in}}{(R_{in}^2 + X_{in}^2)}. \quad (12.43)$$

Under resonance, the input impedance Z'_{in} becomes

$$Z'_{in} = R'_{in} = \frac{1}{G'_{in}} = \frac{1}{G_{in}} = \frac{R_{in}^2 + X_{in}^2}{R_{in}}, \quad (12.44)$$

$$\Rightarrow Z'_{in} = R_{in} + \frac{X_{in}^2}{R_{in}}, \quad \Omega. \quad (12.45)$$

5. The small loop as a receiving antenna

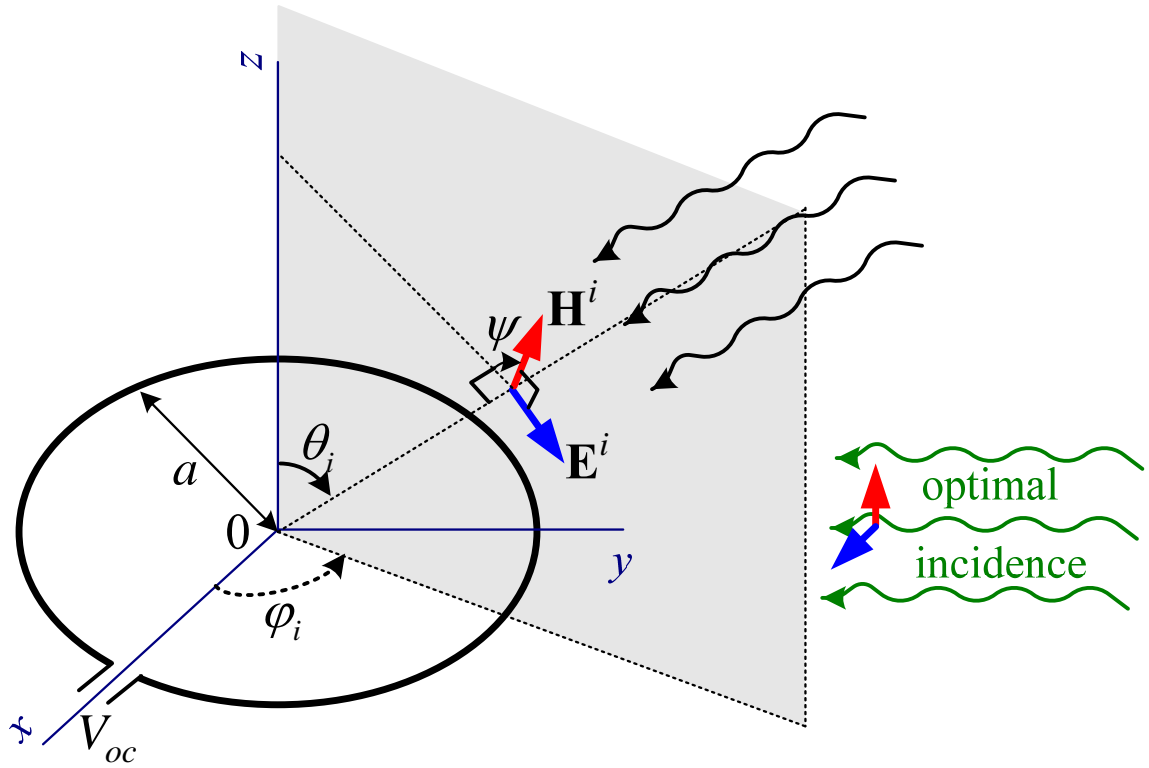
The small loop antennas have the following features:

- 1) high radiation resistance provided multi-turn ferrite-core constructions are used;
- 2) high losses, therefore, low radiation efficiency;
- 3) simple construction, small size and weight.

Small loop antennas are usually not used as transmitting antennas due to their low efficiency e_{cd} . However, they are very much preferred as receiving antennas in AM radio-receivers because of their high signal-to-noise ratio (they can be easily tuned to form a very high- Q resonant circuit), their small size and low cost.

Loops are constructed as magnetic field probes to measure magnetic flux densities. At higher frequencies (UHF and microwave), loops are used to measure the EM field intensity. In this case, ferrite rods are not used.

It is obvious that the loop has to be oriented properly to optimize the reception. The reception depends on the field polarization with the optimal case being a linearly polarized wave with the \mathbf{H} -field aligned with the loop's axis.



The open-circuit voltage at the loop terminals is induced by the time-varying magnetic flux through the loop:

$$V_{oc} = j\omega\Psi_m = j\omega\mathbf{B} \cdot \mathbf{s} = j\omega\mu H_z \cdot \pi a^2, \quad (12.46)$$

$$H_z = H^i \cos\psi \sin\theta_i. \quad (12.47)$$

Here,

Ψ_m is the magnetic flux, Wb;

(θ_i, φ_i) are the angles specifying the direction of incidence;

ψ is the angle between the \mathbf{H}^i vector and the plane of incidence.

Finally, the open-circuit voltage can be expressed as

$$V_{oc} = j\omega\mu S H^i \cos\psi \sin\theta_i = j\beta S E^i \cos\psi \sin\theta_i. \quad (12.48)$$

Here, $S = \pi a^2$ denotes the area of the loop, and $\beta = \omega\sqrt{\mu\epsilon}$ is the phase constant. V_{oc} is maximum for $\theta_i = 90^\circ$ and $\psi = 0^\circ$.

6. Ferrite loops

The radiation resistance and radiation efficiency can be raised by inserting a ferrite core, which has high magnetic permeability in the operating frequency band. Large magnetic permeability $\mu = \mu_0 \mu_r$ means large magnetic flux Ψ_m , and therefore large induced voltage V_{oc} . The radiation resistance of a small loop was already derived in (12.10) to include the number of turns, and it was shown that it increases as $\sim N^2$. Now the magnetic properties of the loop will be included in the expression for R_r .

The magnetic properties of a ferrite core depend not only on the relative magnetic permeability μ_r of the material it is made of but also on its geometry. The increase in the magnetic flux is then more realistically represented by the *effective relative permeability (effective magnetic constant)* $\mu_{r_{eff}}$. We show next that the radiation resistance of a ferrite-core loop is $(\mu_{r_{eff}})^2$ times larger than the radiation resistance of the air-core loop of the same geometry. When we calculated the far fields of a small loop, we made use of the equivalence between an electric current loop and a magnetic current element:

$$j\omega\mu(IA) = I_m l. \quad (12.49)$$

From (12.49) it is obvious that the equivalent magnetic current is proportional to μ . Then, it should be reminded that the field magnitudes are also proportional to I_m , and therefore they are proportional to μ as well. This means that the radiated power Π_{rad} is proportional to μ^2 , and therefore the radiation resistance increases as $\sim (\mu_{r_{eff}})^2$.

Finally, we can express the radiation resistance as

$$R_r = \eta_0 \frac{8}{3} \pi^3 \left(N \mu_{r_{eff}} \frac{A}{\lambda^2} \right)^2. \quad (12.50)$$

Here, $A = \pi a^2$ is the loop area, and $\eta_0 = \sqrt{\mu_0 / \epsilon_0}$ is the intrinsic impedance of vacuum.

Some notes are made below with regard to the properties of ferrite cores:

- The effective magnetic constant of a ferrite core is always less than the magnetic constant of the ferromagnetic material it is made of, i.e., $\mu_{r_{eff}} < \mu_r$. Toroidal cores have the highest $\mu_{r_{eff}}$, and ferrite-stick cores have the lowest $\mu_{r_{eff}}$.

- The effective magnetic constant is frequency dependent. One has to be careful when picking the right core for the application at hand.
- The magnetic losses of ferromagnetic materials increase with frequency. At very high (microwave) frequencies, the magnetic losses are not negligible. They have to be calculated and represented in the equivalent circuit of the antenna as a shunt conductance G_m .