

Power Factor

Again, for a linear circuit with sinusoidal input and an output which has reached the steady-state,

$$\text{Average power absorbed} = P_{av} = \frac{V_m I_m}{2} \cos(\phi - \theta)$$

$$\text{Apparent power} = |\underline{S}| = \frac{V_m I_m}{2}$$

Recall that $v(t) = V_m \cos(\omega t + \phi)$, $i(t) = I_m \cos(\omega t + \theta)$

The power factor, or power factor angle is

$$\text{pf} = \frac{P_{av}}{|\underline{S}|} = \cos(\phi - \theta) = \cos(\theta - \phi)$$

$$\text{Hence} \quad P_{av} = \frac{V_m I_m}{2} \text{ pf}$$

- * Since $\cos(\cdot)$ is even, given a power factor ~~we~~ we cannot tell whether $\phi - \theta > 0$ or $\phi - \theta < 0$. We need more information.
- * The power factor is said to be leading when $\phi - \theta < 0$ and lagging when $\phi - \theta > 0$.