

## Supplied Equations

**Axial stress equations:**

$$\sigma = F/A \quad (\text{M5.13})$$

$$\begin{aligned} \tau_{xx} &= T/A \quad \text{for tension} \\ \tau_{xx} &= -C/A \quad \text{for compression} \end{aligned} \quad (\text{B1.93})$$

**Axial strain equations:**

$$\begin{aligned} \epsilon_{xx} &= \Delta L/L \quad \text{for tension} \\ \epsilon_{xx} &= -\Delta L/L \quad \text{for compression} \end{aligned} \quad (\text{B1.95})$$

**Linear elasticity equation:**

$$\sigma = E\epsilon \quad (\text{M5.14})$$

$$\tau_{xx} = E\epsilon_{xx} \quad (\text{B1.117})$$

**Ground reaction force equations:**

$$F_{gz}(t) = mg + ma_z(t)$$

$$F_{gy}(t) = ma_y(t)$$

**Kinetic energy:**

$$E_{\text{kin}}(t) = \frac{1}{2}mv_z^2(t) + \frac{1}{2}mv_y^2(t)$$

**Gravitational potential energy:**

$$E_{\text{grav}}(t) = mgd_z(t)$$

**Force versus velocity relationship for contracting muscle:**

$$(F + a)(v + b) = (F_0 + a)b \quad (\text{B10.7})$$

**Net joint power:**

$$\text{net joint power} = \mathbf{M} \cdot \boldsymbol{\omega} \quad (\text{W})$$

**Principal stresses in two dimensions:**

$$\sigma_{\max} = \frac{\sigma_x + \sigma_y}{2} + \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} \quad (\text{M5.29})$$

$$\sigma_{\min} = \frac{\sigma_x + \sigma_y}{2} - \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} \quad (\text{M5.30})$$

**The angle of the principal stresses in two dimensions:**

$$\tan 2\theta_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y} \quad (\text{M5.28})$$

**The maximum shear stress in two dimensions:**

$$\tau_{\max} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2} \quad (\text{M5.31})$$

**Mapping of Cartesian stress tensor to principal stresses in three dimensions:**

$$\begin{vmatrix} \tau_{xx} & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \tau_{yy} & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \tau_{zz} \end{vmatrix} \rightarrow \begin{vmatrix} \sigma_1 & 0 & 0 \\ 0 & \sigma_2 & 0 \\ 0 & 0 & \sigma_3 \end{vmatrix} \quad (\text{B1.99})$$

using the relation

$$\begin{aligned} (\tau_{ji} - \sigma_k \delta_{ji}) \hat{e}_i &= 0 \quad \text{for } i, j = x, y, z \\ &\text{and } k = 1, 2, 3 \end{aligned} \quad (\text{B1.100})$$

**Von Mises stresses in three dimensions:**

$$\begin{aligned} \sigma_v &= \sqrt{\frac{(\tau_{xx} - \tau_{yy})^2 + (\tau_{yy} - \tau_{zz})^2 + (\tau_{xx} - \tau_{zz})^2 + 6(\tau_{xy}^2 + \tau_{yz}^2 + \tau_{zx}^2)}{2}} \\ &= \sqrt{\frac{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}{2}} \end{aligned}$$

**Specific gravity of a liquid:**

$$s = \rho(\text{liquid}) / \rho(\text{H}_2\text{O})$$

**Shear stress versus shear rate for a Newtonian fluid:**

$$\tau = \mu \frac{dV}{dy} = \mu \dot{\gamma} \quad (\text{M4.5})$$

$$\tau = \mu \frac{du}{dy} \quad (\text{B2.3})$$

**Bulk modulus (fluid compressibility) equation:**

$$E_V = \rho \frac{dp}{d\rho} \quad (\text{B2.7})$$

**Speed of sound in a substance:**

$$c = \sqrt{\frac{E_V}{\rho}} \quad (\text{B2.8})$$

**Fluid acceleration equation:**

$$\frac{dV}{dt} = \frac{\partial V}{\partial t} + u \frac{\partial V}{\partial x} + v \frac{\partial V}{\partial y} + w \frac{\partial V}{\partial z} \quad (\text{B2.10})$$

**Fluid acceleration along a streamline:**

$$\left(\frac{dV}{dt}\right)_{\text{tang.}} = \frac{\partial V}{\partial t} + V \frac{\partial V}{\partial s} \quad (\text{B2.11})$$

**Fluid acceleration normal to a curving streamline:**

$$\left(\frac{dV}{dt}\right)_{\text{norm.}} = \frac{V^2}{R_c} \quad (\text{B2.12})$$

**Hydrostatic equilibrium equation:**

$$\frac{dp}{dz} = -\rho g \quad (\text{B2.15})$$

**Hydrostatic pressure difference equation:**

$$p_2 - p_1 = -\rho g (z_2 - z_1) \quad (\text{B2.16})$$

$$\Delta P = \rho g_c \Delta h \quad (\text{M2.2})$$

**Conservation of mass for flow within a stream-tube:**

$$\int_{A_2} \rho V_{2n} dA_2 - \int_{A_1} \rho V_{1n} dA_1 = -\frac{\partial}{\partial t} \int_{\mathcal{V}} \rho d\mathcal{V} \quad (\text{B2.20})$$

**Conservation of mass for flow within a stream-tube of constant volume:**

$$A_2 V_2 = A_1 V_1 = Q \text{ (a constant)} \quad (\text{B2.21})$$

$$\dot{m}_{\text{out}} = \dot{m}_{\text{in}} \quad (\text{M4.1})$$

$$(\rho \dot{Q})_{\text{out}} = (\rho \dot{Q})_{\text{in}} \quad (\text{M4.2})$$

$$\dot{m} = \rho_{\text{out}} V_{\text{out}} A_{\text{out}} = \rho_{\text{in}} V_{\text{in}} A_{\text{in}}$$

**Conservation of momentum for flow along a stream-line:**

$$\rho \left( \frac{\partial V}{\partial t} + V \frac{\partial V}{\partial s} \right) ds = -\frac{\partial p}{\partial s} ds - \rho g dz \quad (\text{B2.22})$$

**Bernoulli equation (conservation of momentum for steady flow along a stream-line):**

$$p + \rho \frac{V^2}{2} + \rho g z = H \text{ (a constant)} \quad (\text{B2.24})$$

$$\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\rho g} + \frac{V_2^2}{2g} + z_2 \quad (\text{M4.27})$$

**Reynolds number criterion for laminar flow:**

$$\text{Re} = \frac{\rho V d}{\mu} < \text{Re}_{\text{crit}} \approx 2000 \quad (\text{B2.35})$$

$$N_{\text{Re}} = \frac{\rho D V}{\mu} \quad (\text{M4.7})$$

**Poiseuille flow velocity profile (laminar viscous flow in a circular tube):**

$$u = -\frac{1}{4\mu} \frac{dp}{dx} (a^2 - r^2) \quad (\text{B2.31a})$$

$$V = \frac{(P_1 - P_2) (R^2 - r^2)}{4\mu L} \quad (\text{M4.8})$$

**Poiseuille flow pressure drop:**

$$\Delta p = \frac{32\mu L V}{d^2} \quad (\text{B2.33})$$

**Poiseuille flow entry length equation:**

$$\frac{L_e}{d} \approx 0.06 \text{Re} \quad (\text{B2.36})$$

**Mean kinetic energy of a particle:**

$$\left\langle \frac{mv_x^2}{2} \right\rangle = \frac{k_B T}{2}$$

**Fick's law of diffusion:**

$$J_D = -D_{AB} \frac{dC_A}{dx} \quad (\text{M2.8})$$

**Photon attenuation equation:**

$$I = I_0 e^{-\mu z} \quad (\text{B12.1})$$

$$I_x = I_0 e^{-\mu x} \quad (\text{M8.13})$$

**Radionuclide decay equation:**

$$N = N_0 e^{-\lambda t} \quad (\text{B13.2})$$

**Physical half-life:**

$$T_{p1/2} = \log_e 2 / \lambda \quad (\text{B13.2})$$

**Acoustic intensity, pressure, velocity and impedance relations:**

$$I = pv = Zv^2 = \frac{p^2}{Z}$$

**Acoustic impedance:**

$$Z = \rho c \quad (\text{B12.15})$$

**Pressure reflection coefficient:**

$$R_P = \frac{P_r}{P_i} = \frac{Z_2 - Z_1}{Z_2 + Z_1}$$

**Intensity reflection coefficient:**

$$R_I = \frac{I_r}{I_i} = R_P^2$$

**Intensity transmission coefficient:**

$$T_I = \frac{I_t}{I_i} = 1 - R_I$$

**Ultrasound attenuation equation:**

$$I = I_o e^{-\mu d} \quad (\text{B12.17})$$

**Doppler frequency equation:**

$$f_r = f_o + \Delta f \quad (\text{B12.19})$$

**Doppler frequency shift:**

$$\Delta f = \frac{-2vf_o}{c + v} \cos \theta \approx \frac{-2vf_o}{c} \cos \theta \quad (\text{B12.18})$$

**Larmor equation:**

$$\omega_o = \gamma B_o \quad (\text{B12.9})$$

$$f_R = \gamma B \quad (\text{M8.24})$$

**T1 and T2 relaxation equations:**

$$M_z = M \left( 1 - e^{-t/\tau_1} \right) \quad (\text{M8.31})$$

$$M_{xy} = M e^{-t/\tau_2} \quad (\text{M8.32})$$

**Spin echo sequence NMR signal strength:**

$$S \approx N f(v) \left[ e^{-TE/T2} \right] \left[ 1 - e^{-TR/T1} \right] \quad (\text{B12.10})$$

**THE END**