ELEC ENG 3BB3 – Cellular Bioelectricity (2014) Tutorial 7

1. A patch of membrane at 21°C has the following intra- and extra-cellular ionic concentrations:

| Ion | [C] _{in} (mM) | $[C]_{out} (mM)$ |
|----------------|------------------------|------------------|
| \mathbf{K}^+ | 200 | 5 |
| Na^+ | 10 | 150 |

- a. If the resting conductances of voltage-gated potassium and sodium channels in this patch of membrane are $g_{\rm K} = 2.0 \,\mathrm{mS/cm^2}$ and $g_{\rm Na} = 0.05 \,\mathrm{mS/cm^2}$, respectively, find the resting potential $V_{\rm rest}$ for this patch of membrane.
- b. If a postsynaptic receptor in this patch of membrane has maximum conductances for potassium and sodium of $g_{\text{syn,K}} = 10 \text{ mS/cm}^2$ and $g_{\text{syn,Na}} = 5 \text{ mS/cm}^2$, respectively, determine whether the synapse is excitatory or inhibitory.
- 2. The subthreshold behaviour of a neural soma can be described by the circuit diagram shown below.



The neuron has a threshold potential of $V_{\text{th}} = -40 \text{ mV}$. Synaptic input onto this soma consists of one inhibitory synapse that produces the current:

$$I_{\mathrm{I}} = g_{\mathrm{I}}(t) [V_m - E_{\mathrm{I}}].$$

Consider the case where the membrane is at rest (i.e., $V_m = V_{rest}$) and the inhibitory conductance $g_1 = 0$ nS for time t < 0. At time t = 0, a step current of $I_{inj} = 0.5$ nA is injected into the interior of the soma. Assume that the inhibitory synaptic conductance g_1 steps instantaneously at time t = 2 ms to a new value in response to neurotransmitter binding and remains at that value until at least t = 4 ms.

What is the minimum value to which the inhibitory conductance g_1 can step at time t = 2 ms in order to stop the membrane potential V_m from reaching the threshold potential V_{th} by time t = 4 ms?