

# EE 4BD4 Lecture 15

Strain ( force) Gauges, pressure  
sensors and Load Cells

# The Strain Gauge

- Measures the effects of very small displacements (lengthening or shortening) of a resistive sensor
- Is an isometric device with conductor strain gauges having a maximum resistive change of 1 to 3 %
- Resistive change based on both dimensional changes of conductor and strain placed on the sensor (piezoresistive effect)
- Sensors are small, but glued (bonded) to larger structures to increase range of forces measured

# Basic Theory

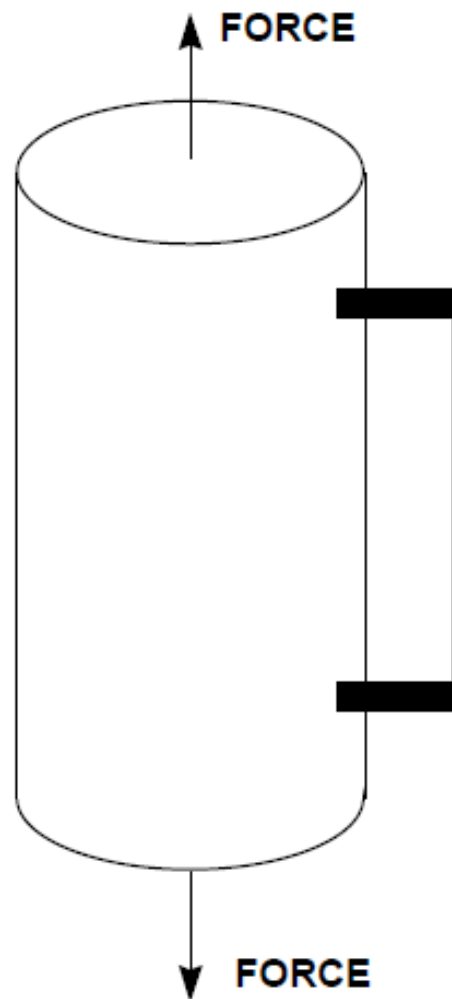
$$R = \frac{\rho L}{A}$$

$$dR = \frac{\rho dL}{A} - \rho A^{-2} L dA + L \frac{d\rho}{A} \rightarrow \frac{\Delta R}{R} = \frac{\Delta L}{L} - \frac{\Delta A}{A} + \frac{\Delta \rho}{\rho}$$

Poisson's ratio  $\mu$  relates the change in diameter  $\Delta D$  to the change in length,  $\Delta D/D = -\mu \Delta L/L$ . Substituting this into the center term of (2.3) yields

$$\frac{\Delta R}{R} = \underbrace{(1 + 2\mu) \frac{\Delta L}{L}}_{\text{Dimensional effect}} + \underbrace{\frac{\Delta \rho}{\rho}}_{\text{Piezoresistive effect}} \quad G = \frac{\Delta R/R}{\Delta L/L} = (1 + 2\mu) + \frac{\Delta \rho/\rho}{\Delta L/L}$$

# UNBONDED WIRE STRAIN GAGE



STRAIN  
SENSING  
WIRE

AREA = A  
LENGTH = L  
RESISTIVITY =  $\rho$   
RESISTANCE = R

$$R = \frac{\rho L}{A}$$

$$\frac{\Delta R}{R} = GF \cdot \frac{\Delta L}{L}$$

GF = GAGE FACTOR  
2 TO 4.5 FOR METALS  
>150 FOR SEMICONDUCTORS

$$\frac{\Delta L}{L} = \text{MICROSTRAINS } (\mu\varepsilon)$$

$$1 \mu\varepsilon = 1 \times 10^{-6} \text{ cm / cm} = 1 \text{ ppm}$$

# Different Conductive Materials

**Table 2.1** Properties of Strain-Gage Materials

| Material                | Composition (%)   | Gage Factor  | Temperature Coefficient of Resistivity ( $^{\circ}\text{C}^{-1} - 10^{-5}$ ) |
|-------------------------|---|--------------|--|
| Constantan<br>(advance) | Ni <sub>45</sub> , Cu <sub>55</sub>   | 2.1          | $\pm 2$  |
| Isoelastic              | Ni <sub>36</sub> , Cr <sub>8</sub><br>(Mn, Si, Mo) <sub>4</sub><br>Fe <sub>52</sub> | 3.52 to 3.6  | +17  |
| Karma                   | Ni <sub>74</sub> , Cr <sub>20</sub> , Fe <sub>3</sub><br>Cu <sub>3</sub>            | 2.1          | +2   |
| Manganin                | Cu <sub>84</sub> , Mn <sub>12</sub> , Ni <sub>4</sub>                               | 0.3 to 0.47  | $\pm 2$  |
| Alloy 479               | Pt <sub>92</sub> , W <sub>8</sub>   | 3.6 to 4.4   | +24  |
| Nickel                  | Pure  | -12 to -20   | 670  |
| Nichrome V              | Ni <sub>80</sub> , Cr <sub>20</sub>   | 2.1 to 2.63  | 10   |
| Silicon                 | ( <i>p</i> type)  | 100 to 170   | 70 to 700  |
| Silicon                 | ( <i>n</i> type)  | -100 to -140 | 70 to 700  |
| Germanium               | ( <i>p</i> type)  | 102          |  |
| Germanium               | ( <i>n</i> type)  | -150         |  |

SOURCE: FROM R. S. C. COBBOLD, *Transducers for Biomedical Measurements*, 1974, John Wiley & Sons, Inc.. Used with permission of John Wiley & Sons, Inc., New York.

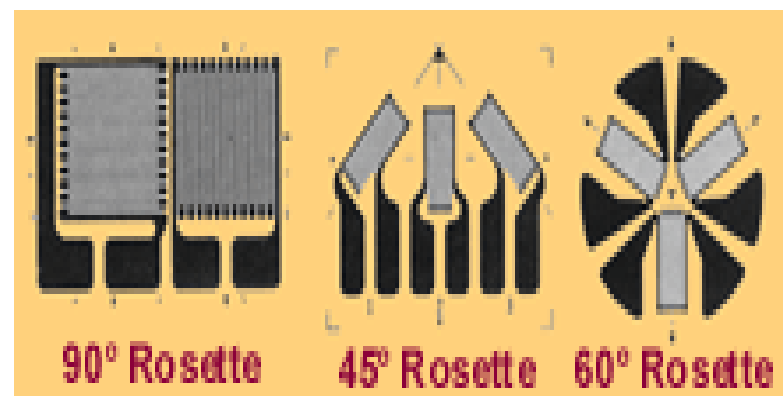
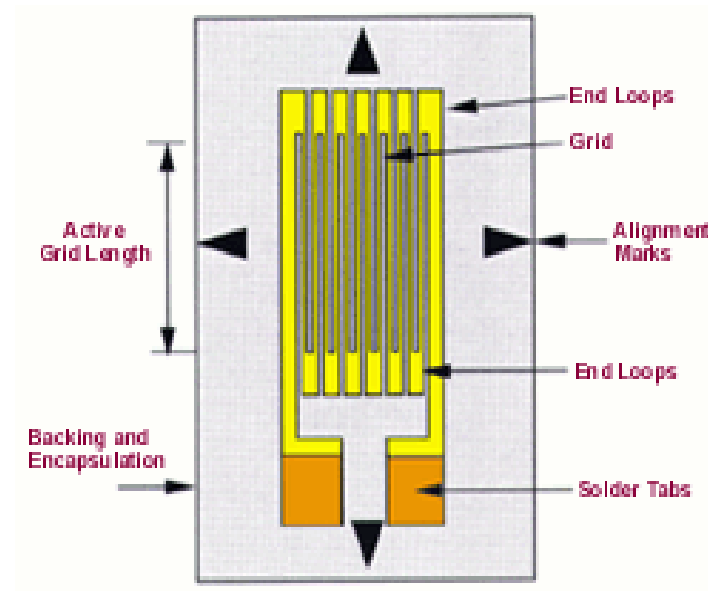
# Selection of Type

- Metal foil gauges have a linear resistance change with strain but are less sensitive
- Semiconductor gauges based on piezoresistive effect in germanium and silicon and are much more temperature sensitive
- Resistance change is nonlinear for S-C strain gauges and are not as commonly used as metal foil

## COMPARISON BETWEEN METAL AND SEMICONDUCTOR STRAIN GAGES

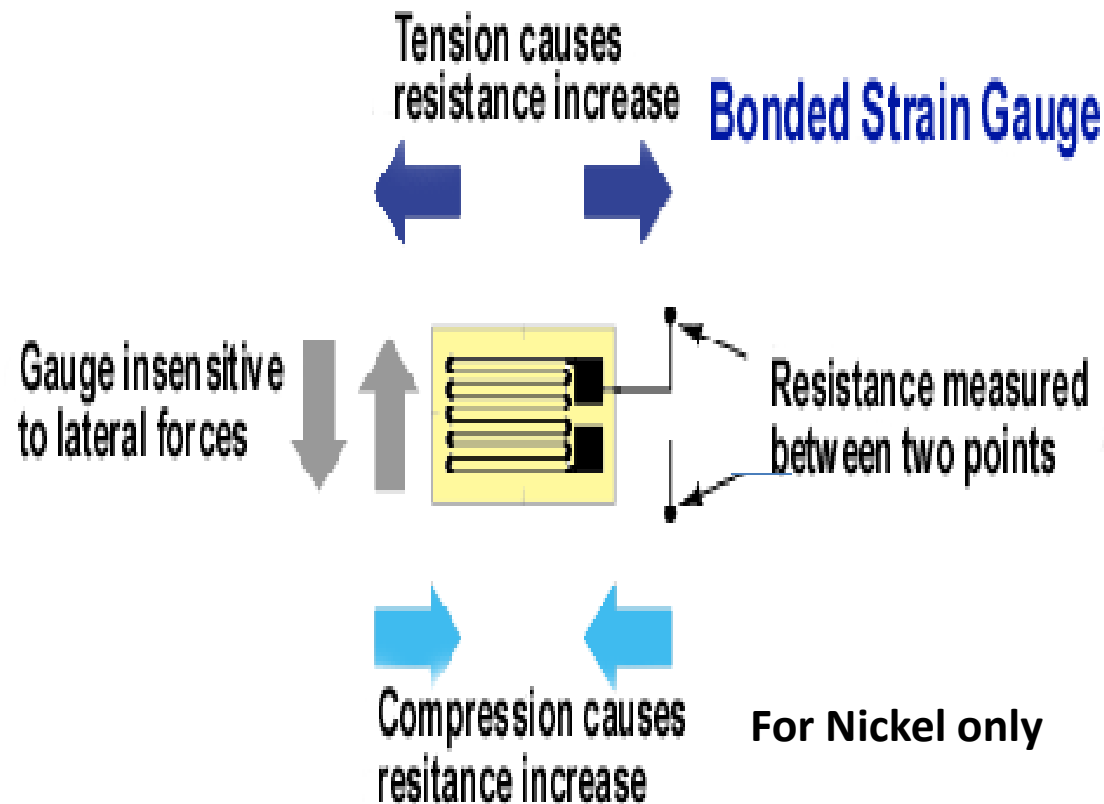
| PARAMETER            | METAL STRAIN GAGE              | SEMICONDUCTOR STRAIN GAGE   |
|----------------------|--------------------------------|-----------------------------|
| Measurement Range    | 0.1 to 40,000 $\mu\epsilon$    | 0.001 to 3000 $\mu\epsilon$ |
| Gage Factor          | 2.0 to 4.5                     | 50 to 200                   |
| Resistance, $\Omega$ | 120, 350, 600, ..., 5000       | 1000 to 5000                |
| Resistance Tolerance | 0.1% to 0.2%                   | 1% to 2%                    |
| Size, mm             | 0.4 to 150<br>Standard: 3 to 6 | 1 to 5                      |

# Types of Foil Strain Gauges





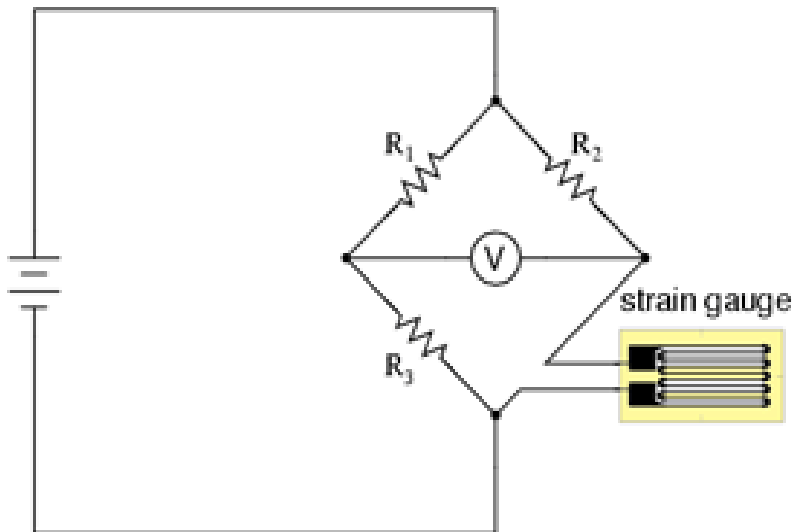
# Principle of Operation



# Measurement Circuits

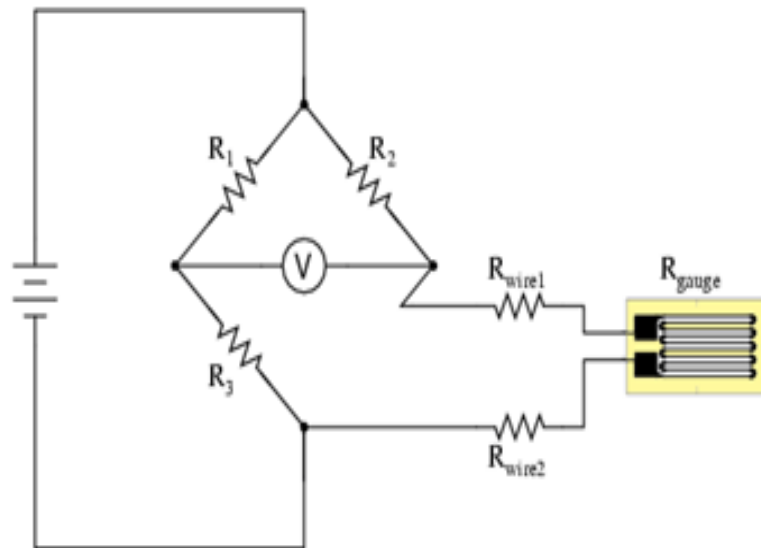
- Base resistance for bonded gauges between  $30\ \Omega$  and  $3\ \text{k}\Omega$  (typically  $350\ \Omega$ )

*Quarter-bridge strain gauge circuit*

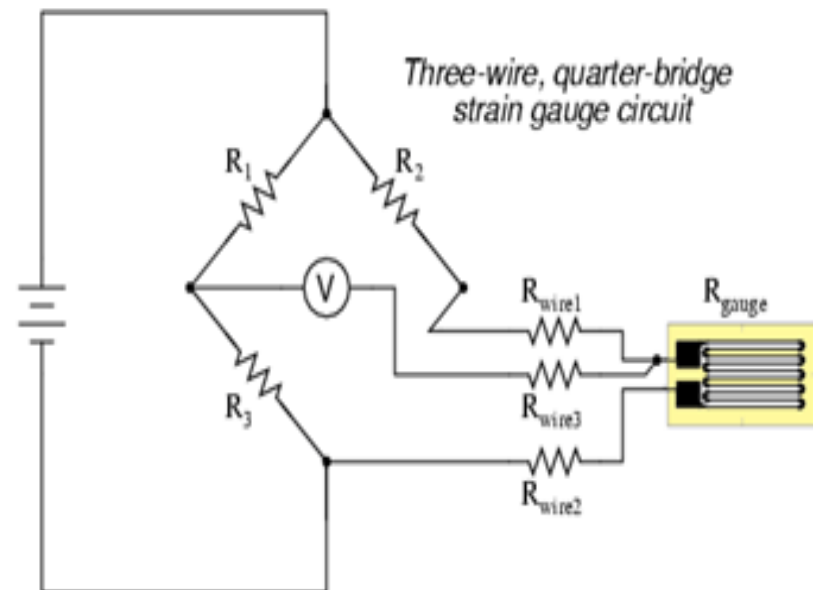


- $R_1$ ,  $R_2$  and  $R_3$  are balancing resistors (e.g.  $350\ \Omega$ ) so bridge balanced at 0 strain and  $V = 0$
- Temperature changes cause change in dimensions of structure and gauge and resistivity of gauge resulting in baseline drift

- Effects of lead resistance temperature changes



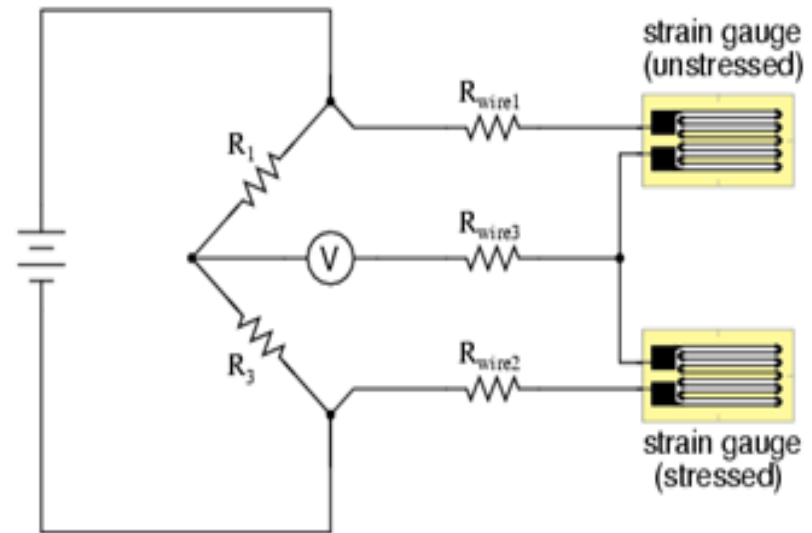
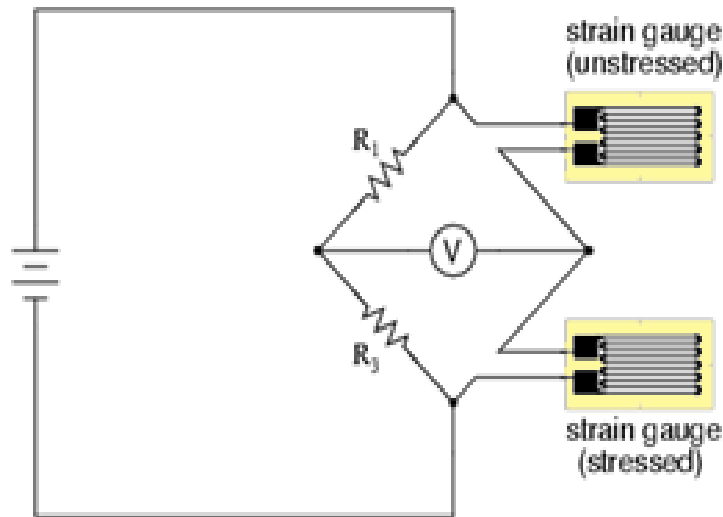
- Lead temperature compensated bridge



# Using an Extra Gauge for Temperature Compensation

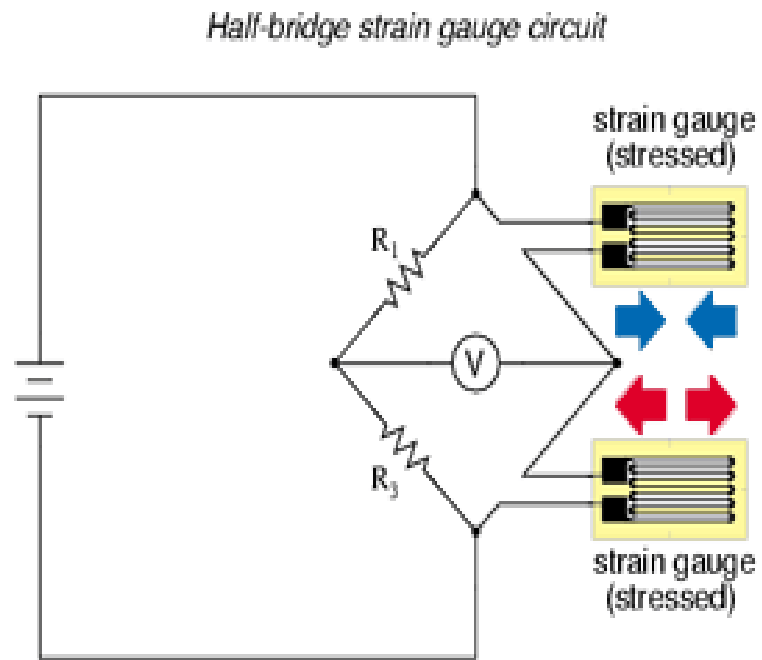
- Circuit to compensate for temperature effects on structure and gauges
- Fully temperature compensated circuit

*Quarter-bridge strain gauge circuit with temperature compensation*

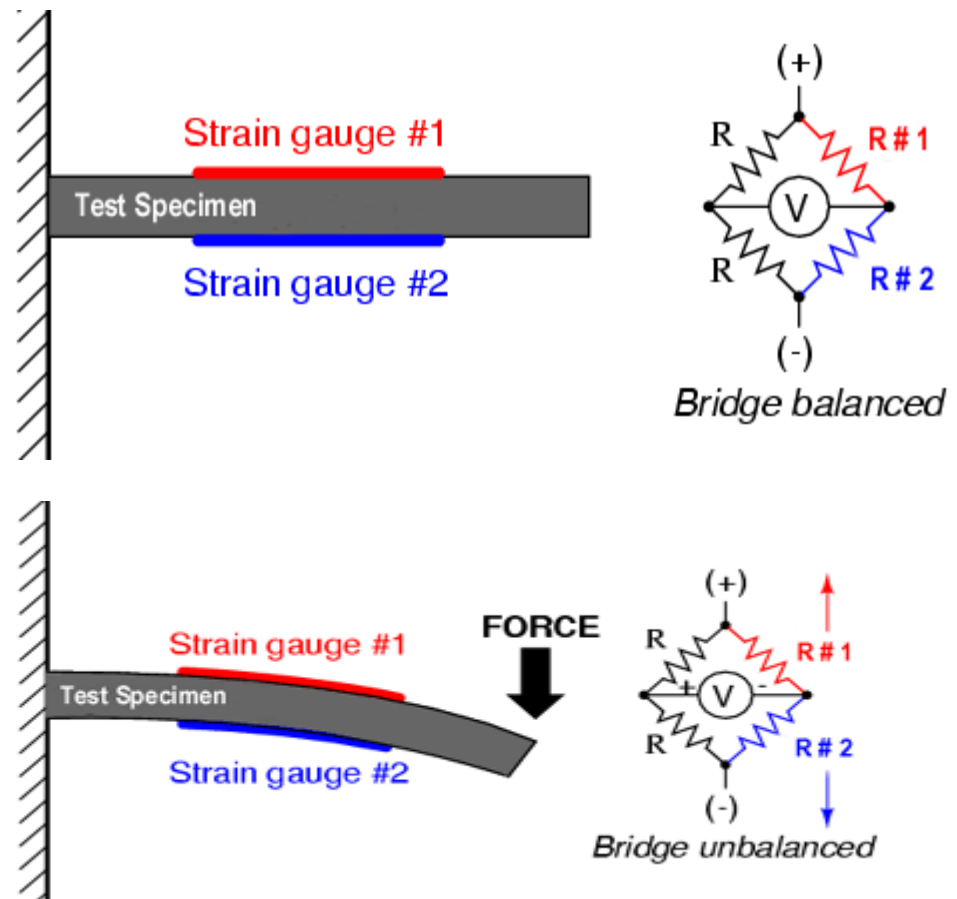


# Beam with Two Gauges

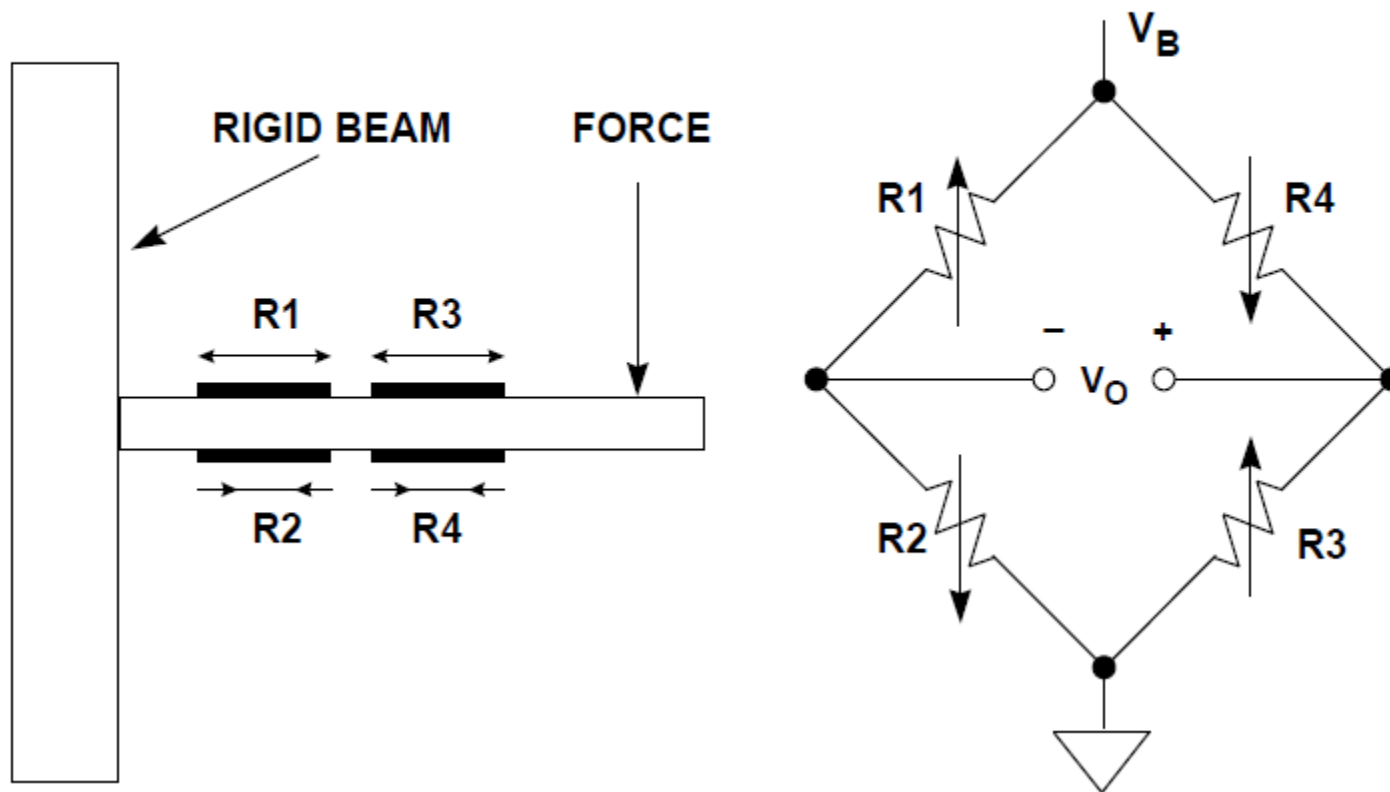
- Two stressed gauges



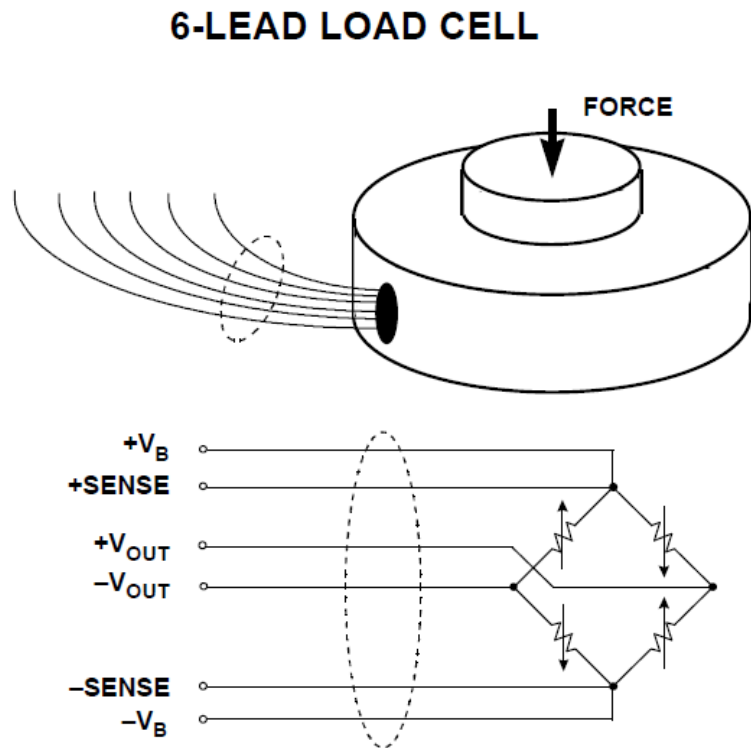
- Beam example



## STRAIN GAGE BEAM FORCE SENSOR

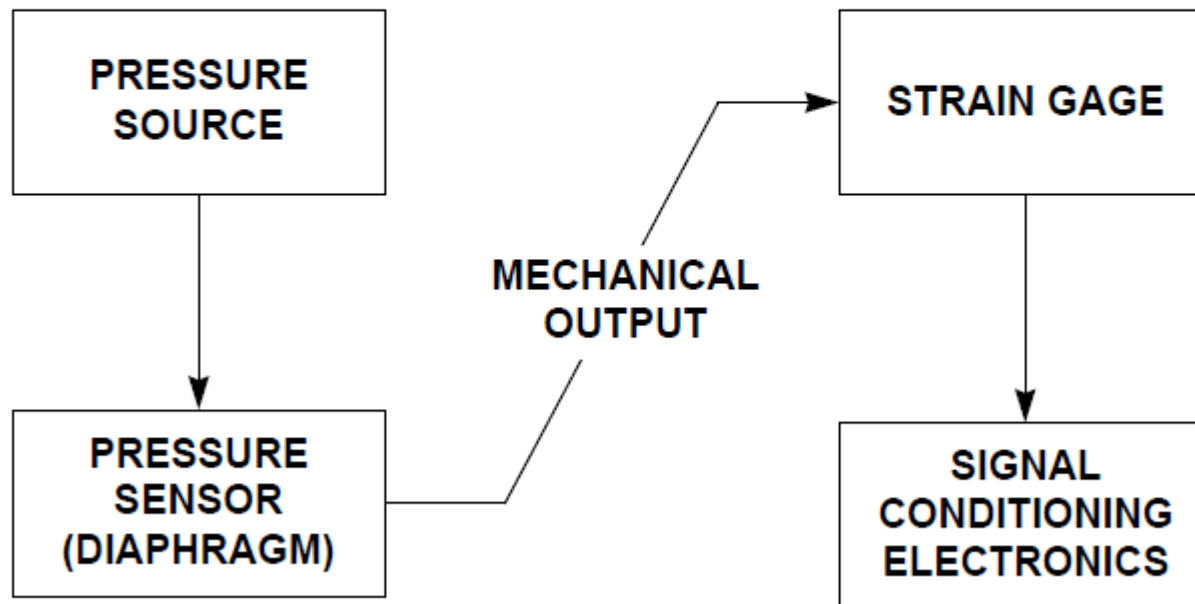


# Load Cells



- Force range based on size of load cell structure and beams
- Typical 30 mV output for full load
- If source voltage too high you get excessive heating of resistors

# PRESSURE SENSORS





# LOW-VOLTAGE AMPLIFIED OUTPUT TRANSDUCER FOR 5 Vdc POWER

## PX139 Series

±1.0 to ±30 psi  
±0.07 to ±2 bar

All Ranges  
**\$105**



- ✓ Available for Differential, Gage, or Absolute Measurement
- ✓ Calibrated 4V Output Span
- ✓ Precise Temperature Compensation
- ✓ For Dry Gas

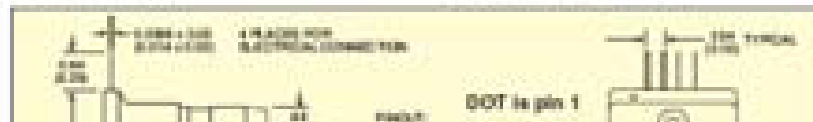


Actual size



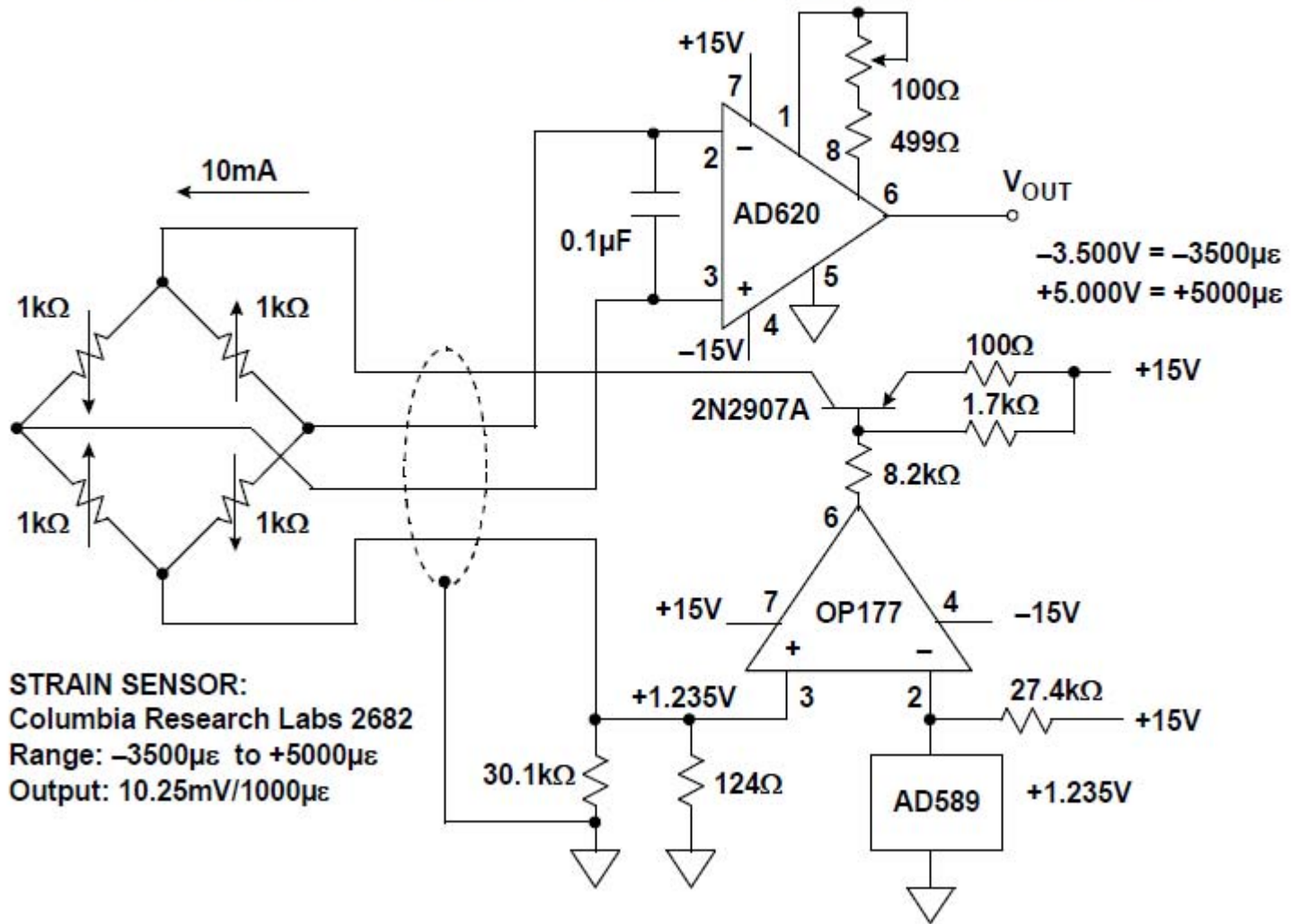
PX139-001D4V, \$105, shown 2.5x larger than actual size.

Burst Pressure: >5x FS pressure  
Common Mode Press: 50 psi  
Media Compatibility: For use with gases compatible with silicon, glass-filled nylon and alumina ceramic  
Mating Connector: CXC139-4 (sold separately)

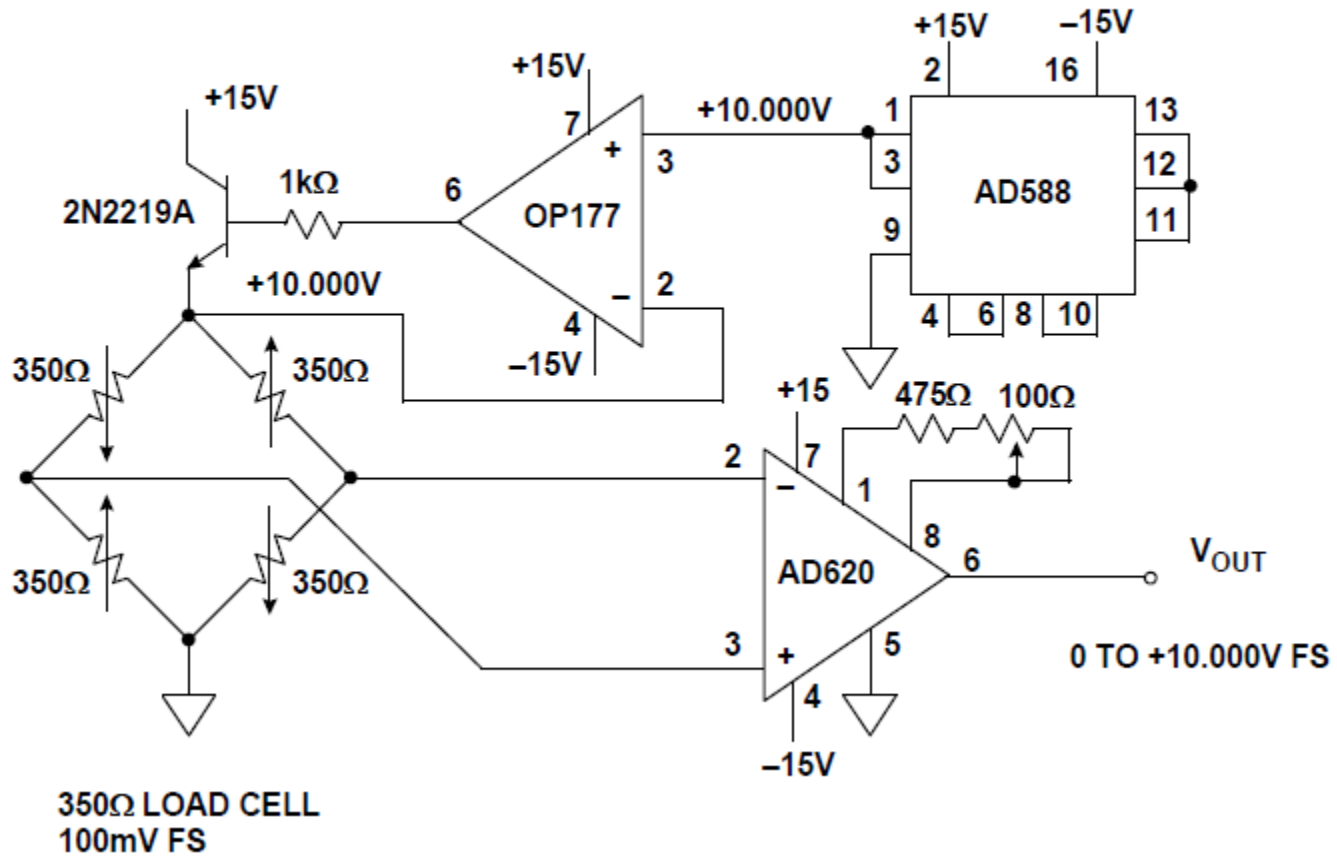


VOLTAGE OUTPUT  
PRESSURE TRANSDUCERS

# PRECISION STRAIN GAGE SENSOR AMPLIFIER



# PRECISION LOAD CELL AMPLIFIER



## SINGLE SUPPLY LOAD CELL AMPLIFIER

