

# EE 791 Lecture 8

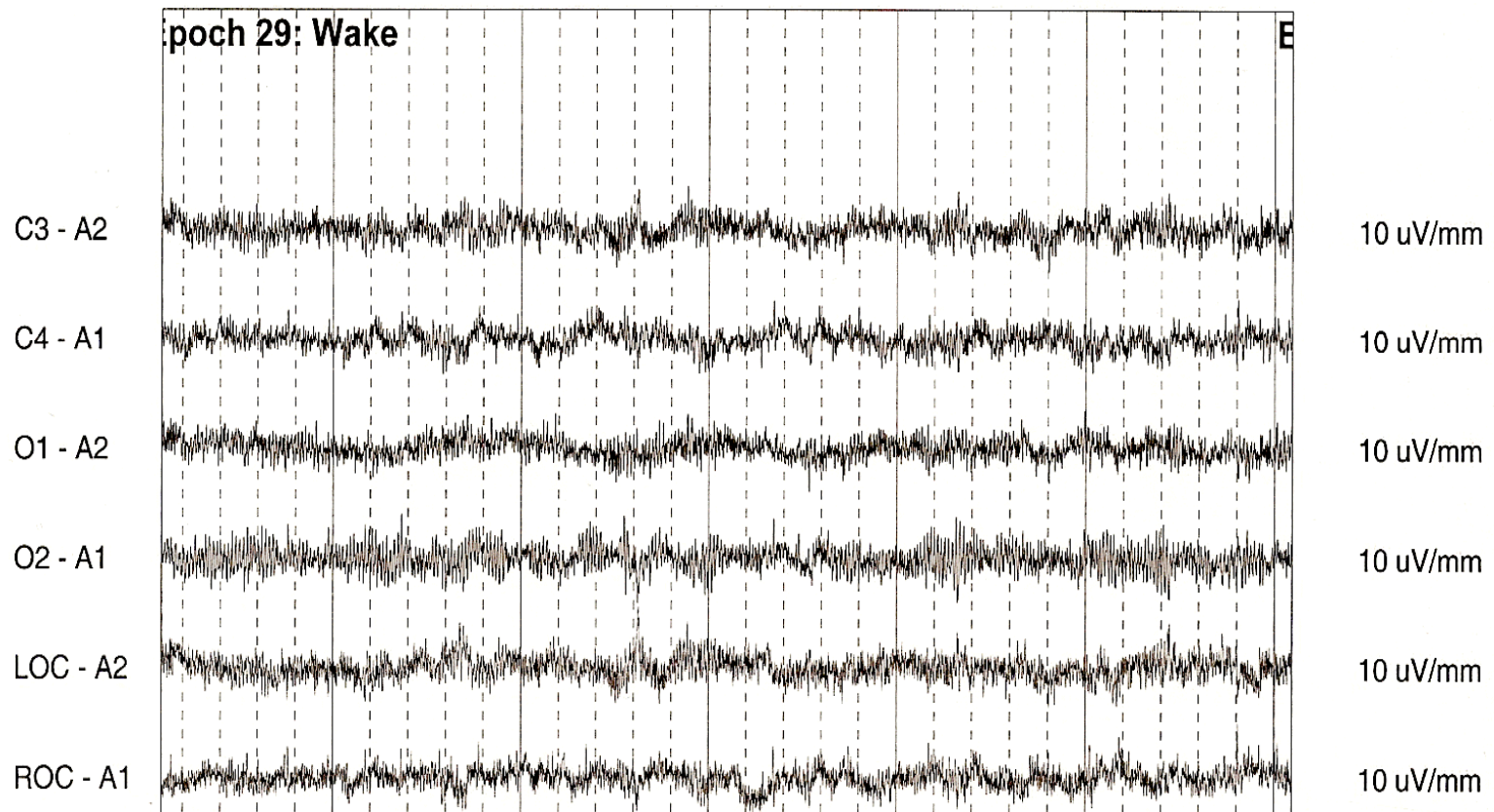
**Measures of Dynamic Properties (cont'd)**  
**March 15, 2018**

# Awake

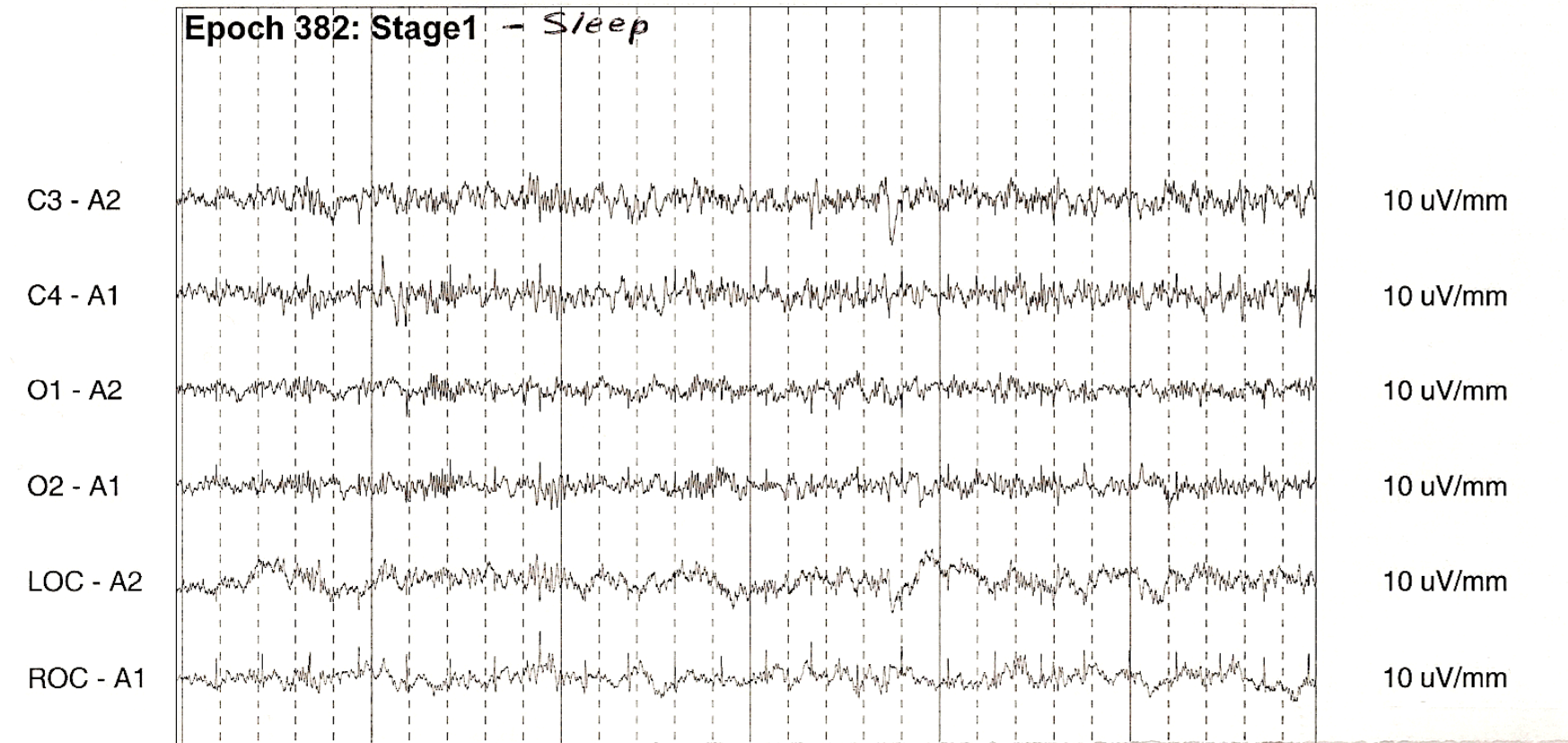
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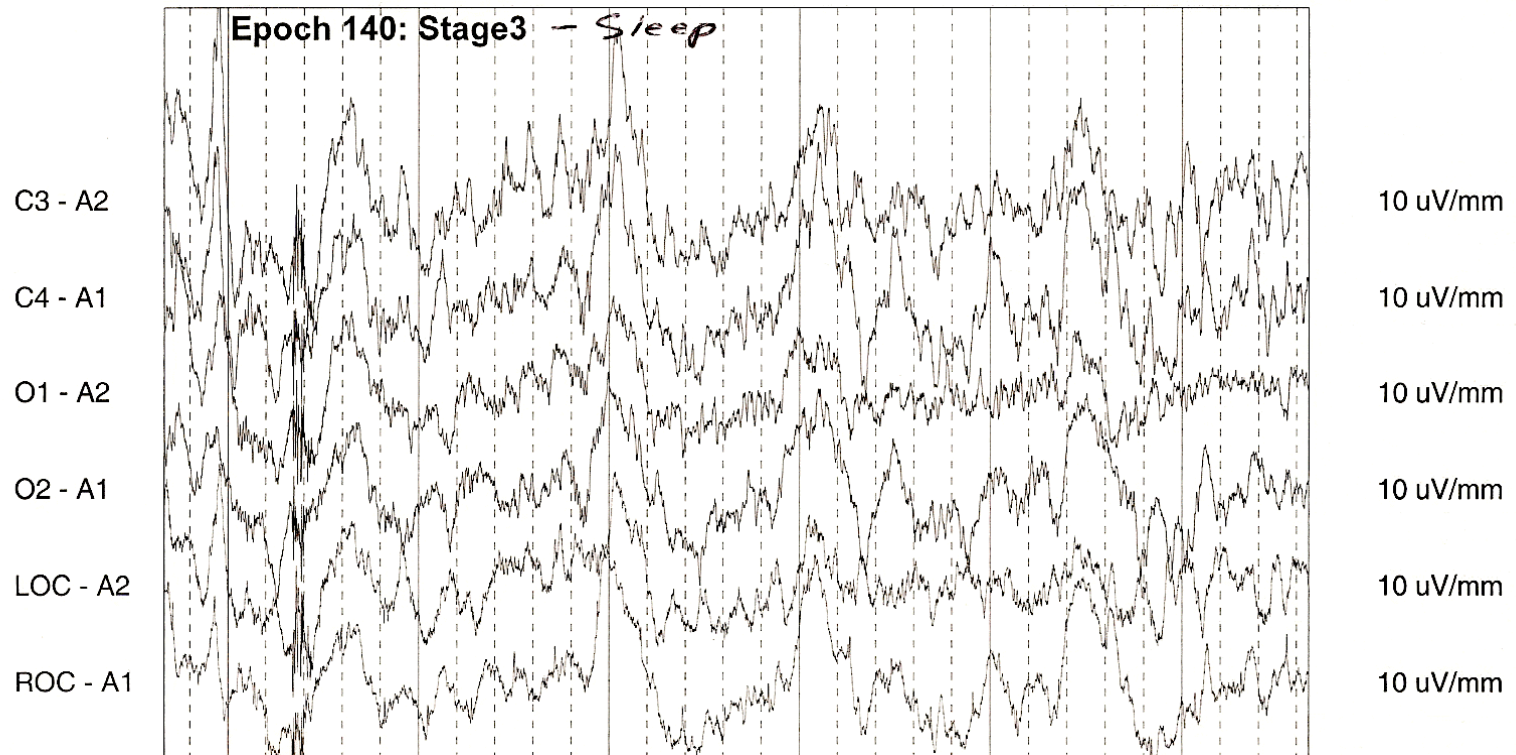
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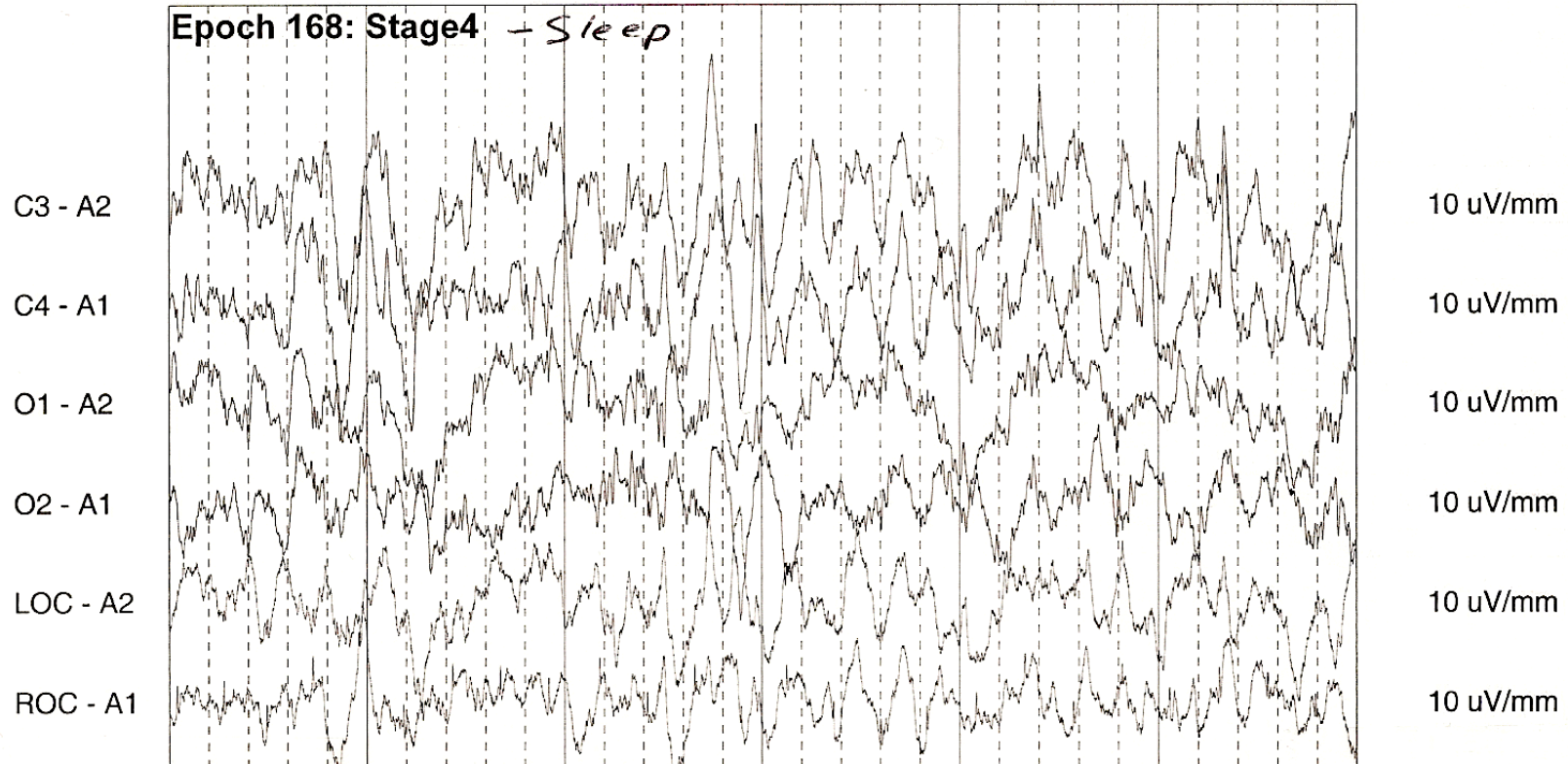
# Stage 1



# Stage 3



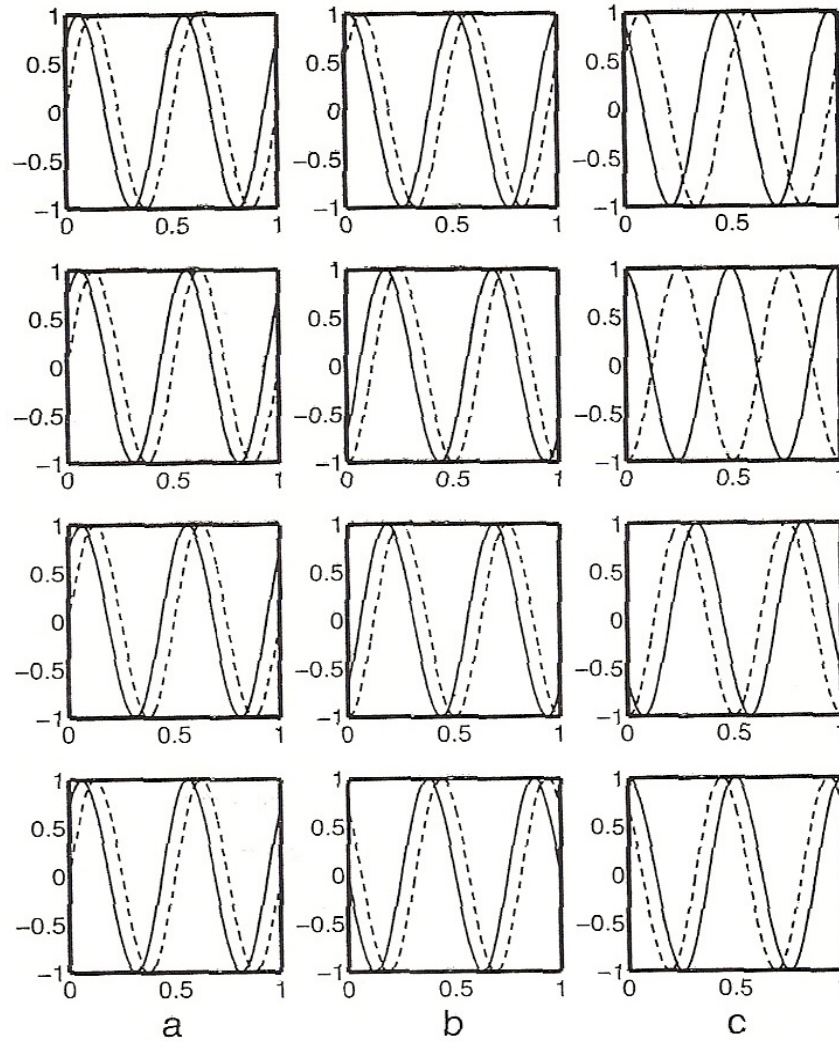
# Stage 4



# Coherence

- Spatial analysis of EEG
- Defined as a linear correlation coefficient that estimates primarily the amount of phase synchronization between any two data channels
- Obtain an estimate
- Similar to squared correlation coefficient which estimates the proportion of variance in one channel that can explained by a linear transformation of another channel

# Phase Relations



# Calculation of Coherence

- Cross Spectrum

$$C_{uv}(f_n) = A_{uv} e^{j\phi_{uv}} = \frac{2}{K} \sum_{k=1}^K F_{uk}(f_n) F_{vk}^*(f_n)$$

$$n = 1, 2, \dots, N/2-1$$

Where the estimate is made over K signal epochs and the F's are Fourier coefficients. Factor 2 because only considering positive f (similar to covariance)



# Calculation of Coherence (cont'd)

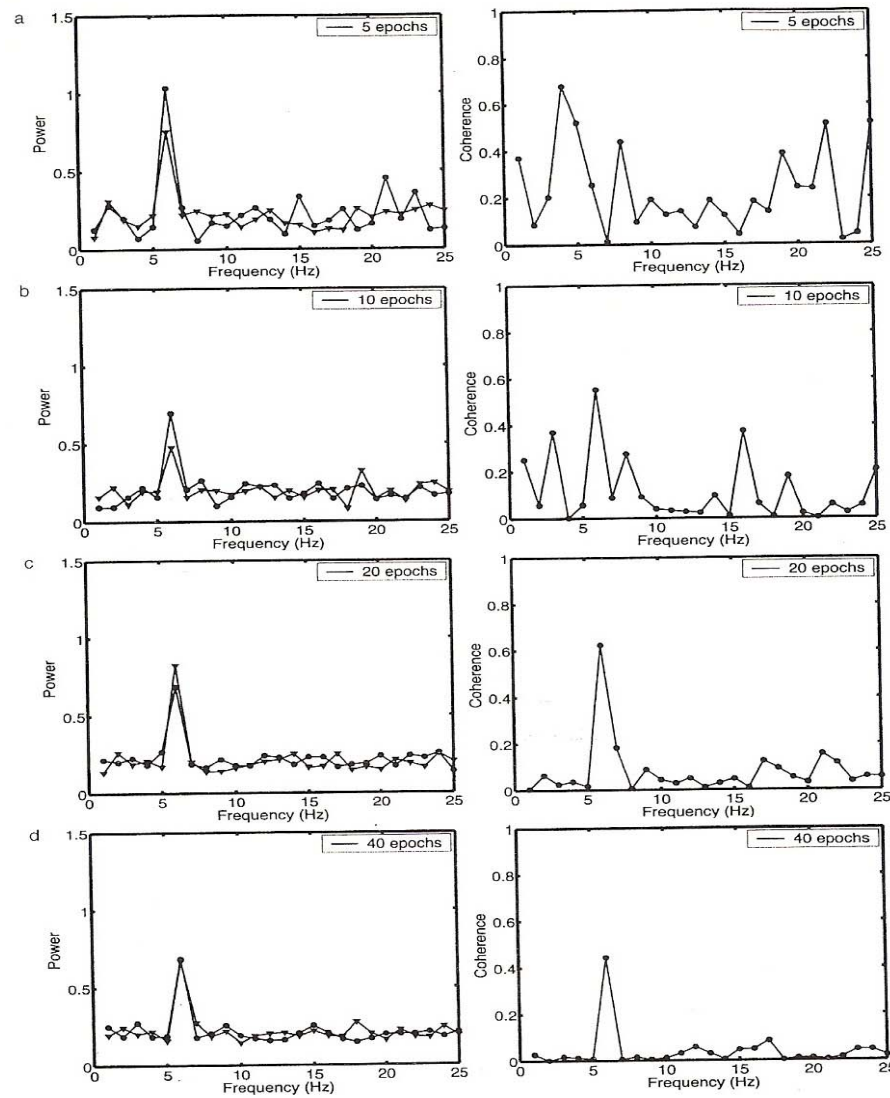
- Coherence between two channels

$$\Upsilon_{uv}^2(f_n) = \frac{|C_{uv}(f_n)|^2}{P_u(f_n)P_v(f_n)} \quad n = 0, 1, 2, \dots, (N-1)/2$$

Sensitive to relative phase between two channels. If phase difference is constant coherence = 1, if purely random = 0

# Spectra and Coherence

- Fig 9.10

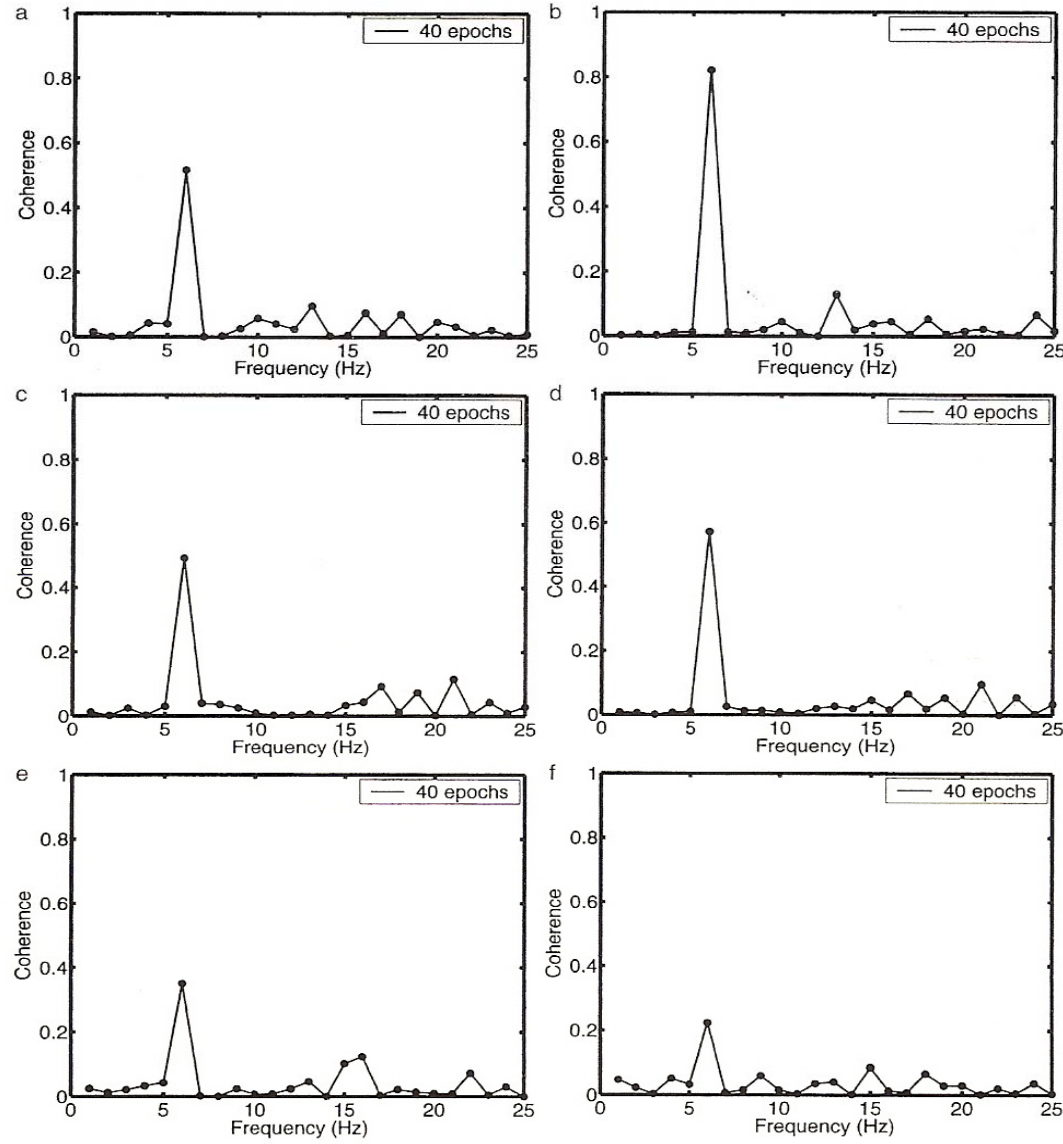


# Implications of Coherence

- A coherence value does not imply a linear relationship between two dynamic processes just the fraction of the phase coherence between the data sets (i.e. a model)
- Relationship between two EEG channels could be deterministic but nonlinear, resulting in a coefficient  $<1$
- Consider both relative phase and amplitude with larger EEG Fourier coefficients giving more reliable estimates of coherence.

# Effects of Phase-only Coherence

- Fig 9.11

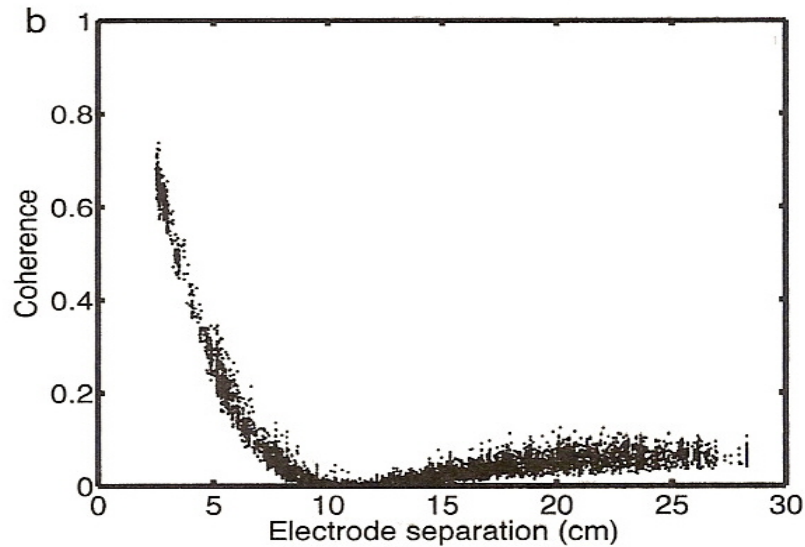
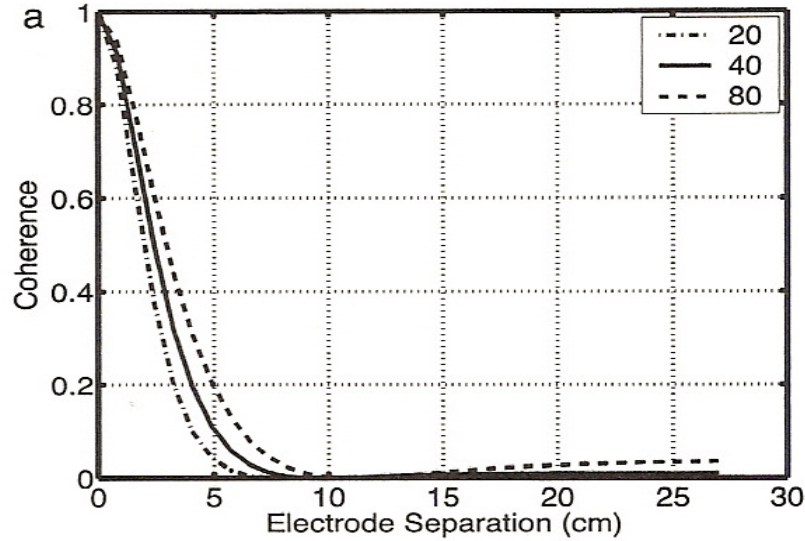


# Effects of Spatial Filtering by Volume Conduction

- Objective of coherence estimates is to estimate statistical properties of source processes.
- Need a model to relate these properties to statistical properties of scalp potentials.
- Effects of volume conduction on EEG coherence are independent of temporal frequency.
- Perceived coherence effect due to angular distance between electrodes relative to source

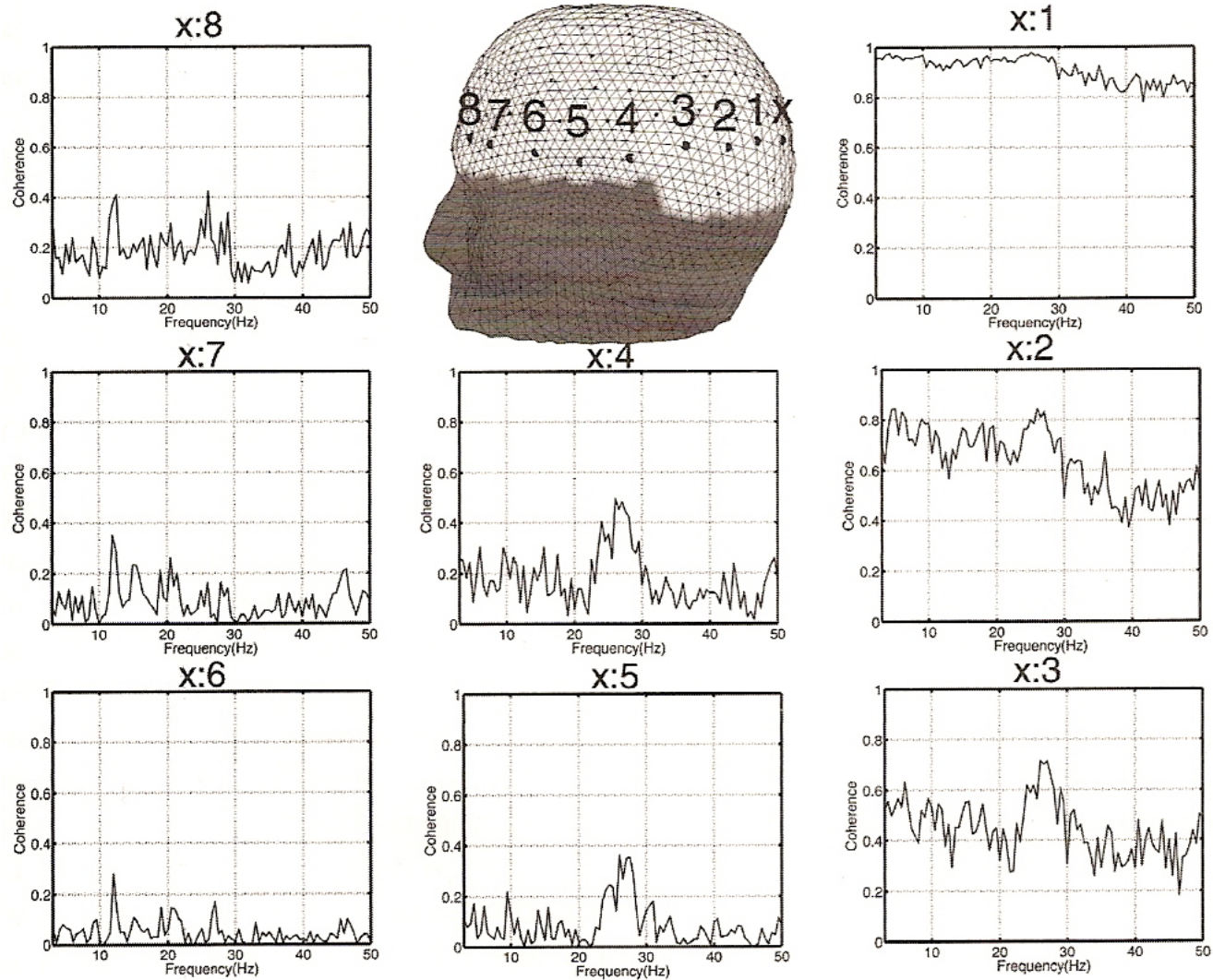
# Effect of Volume Conduction (simulated)

- Fig 9.12



# Effect of Volume Conduction (real)

- Fig 9.13



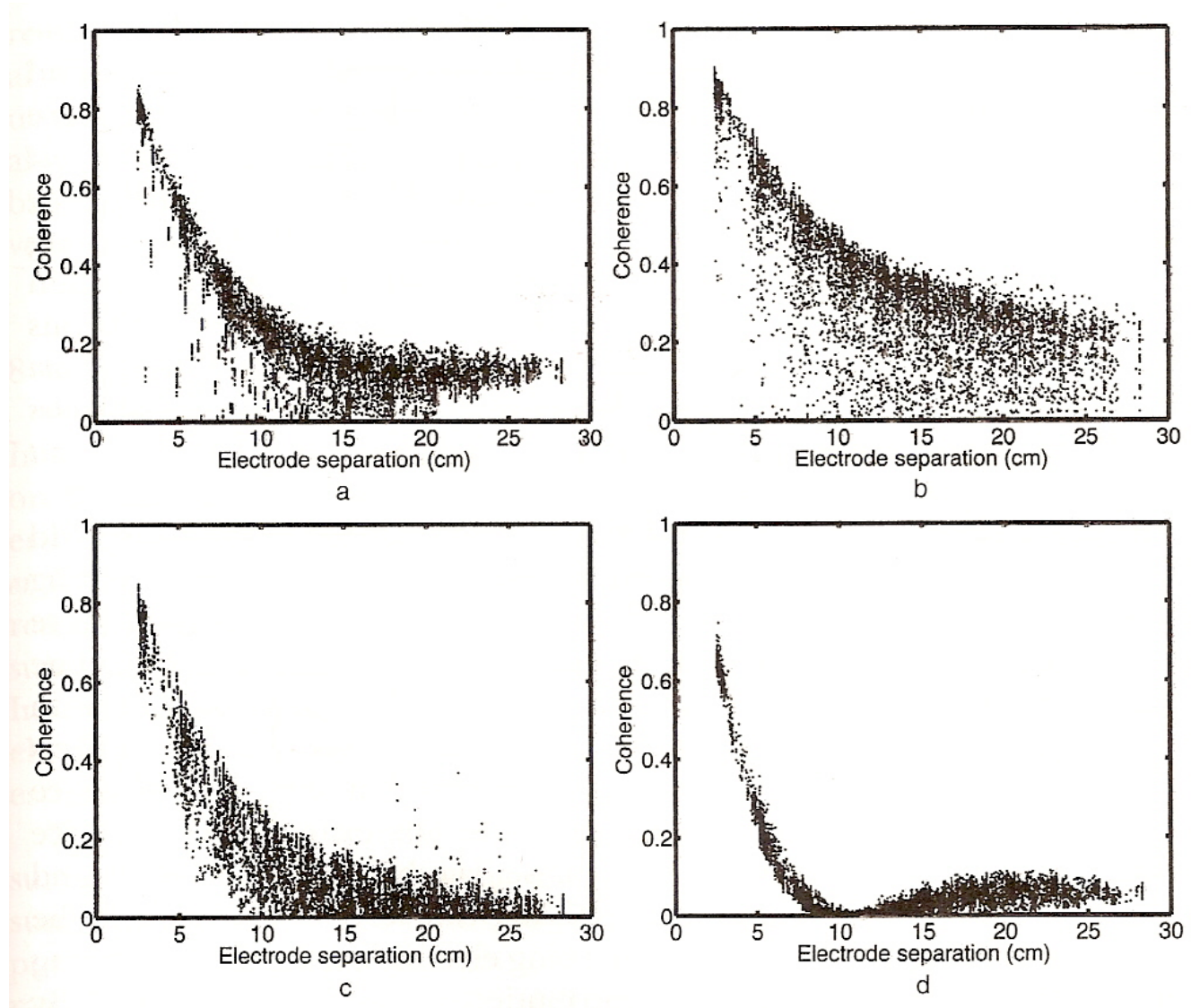
# Effects of Reference System

- Simulations using 3600 dipole sources and 111 electrodes with a 4-sphere head model
- Results show using vertex as reference results in lower coherence than a single mastoid
- Linked ear is better but best results for averaged reference (similar to reference free theoretical calculations)

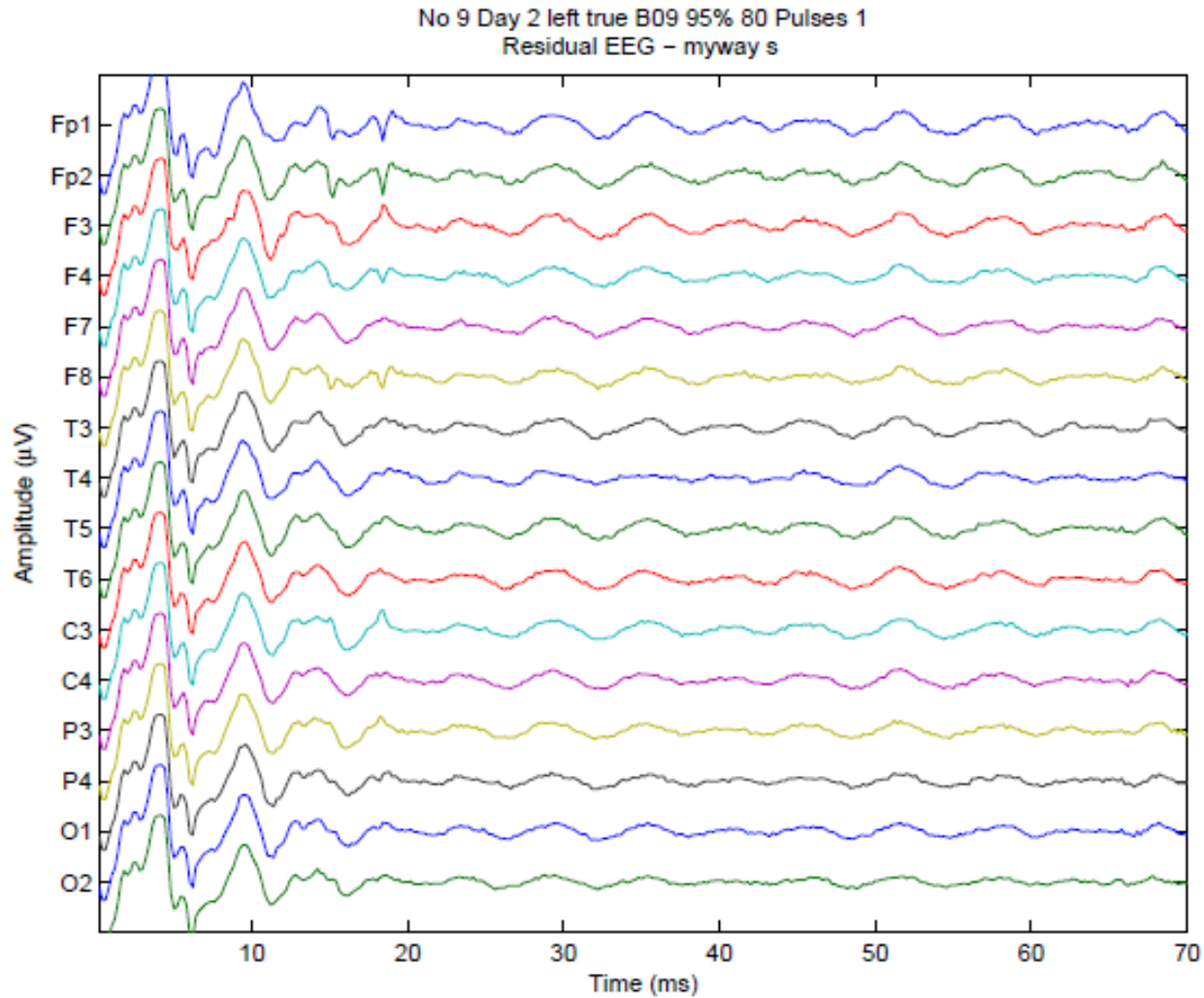


# Effects of Reference

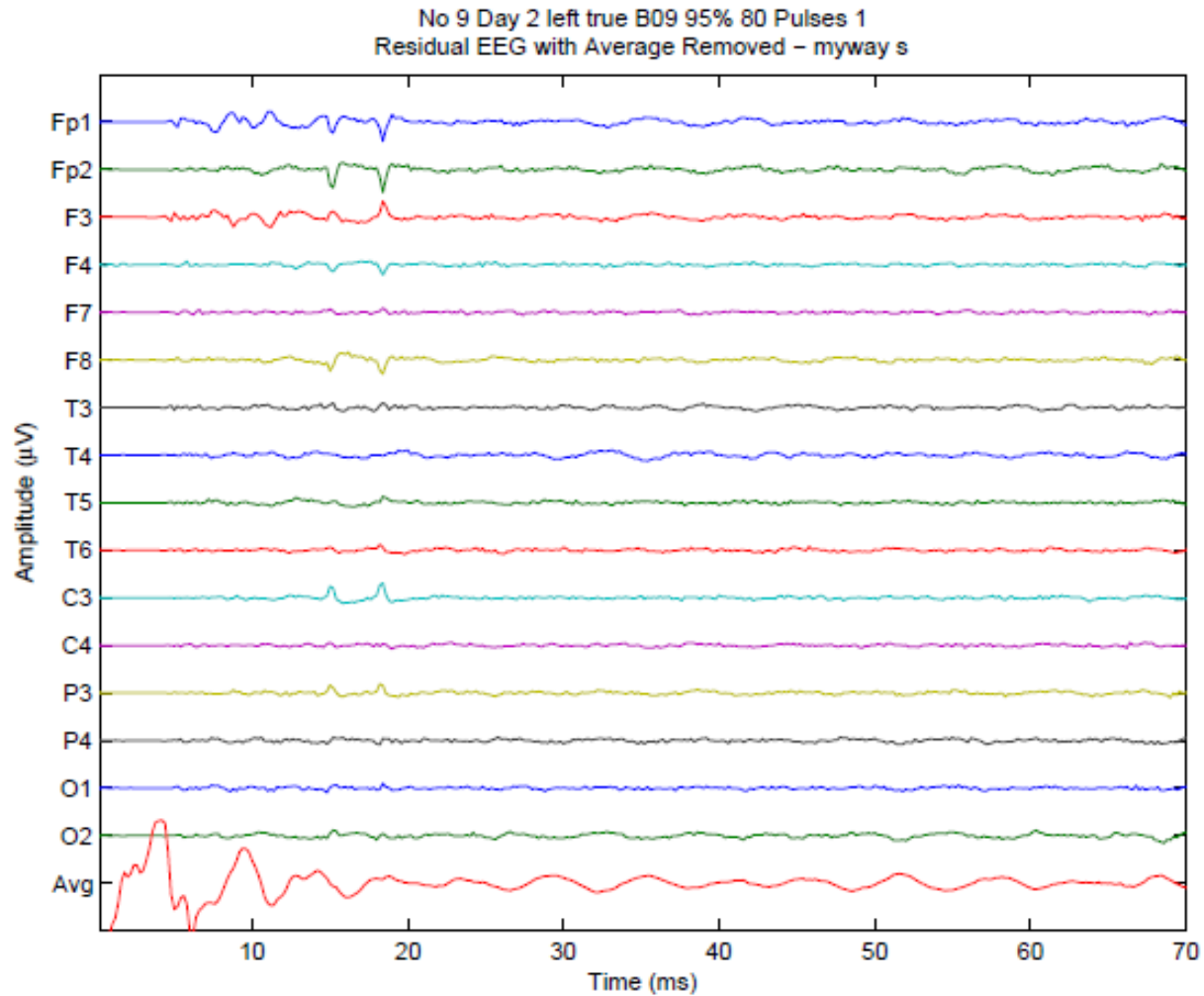
- Fig 9.14



# Evoked Potential Data

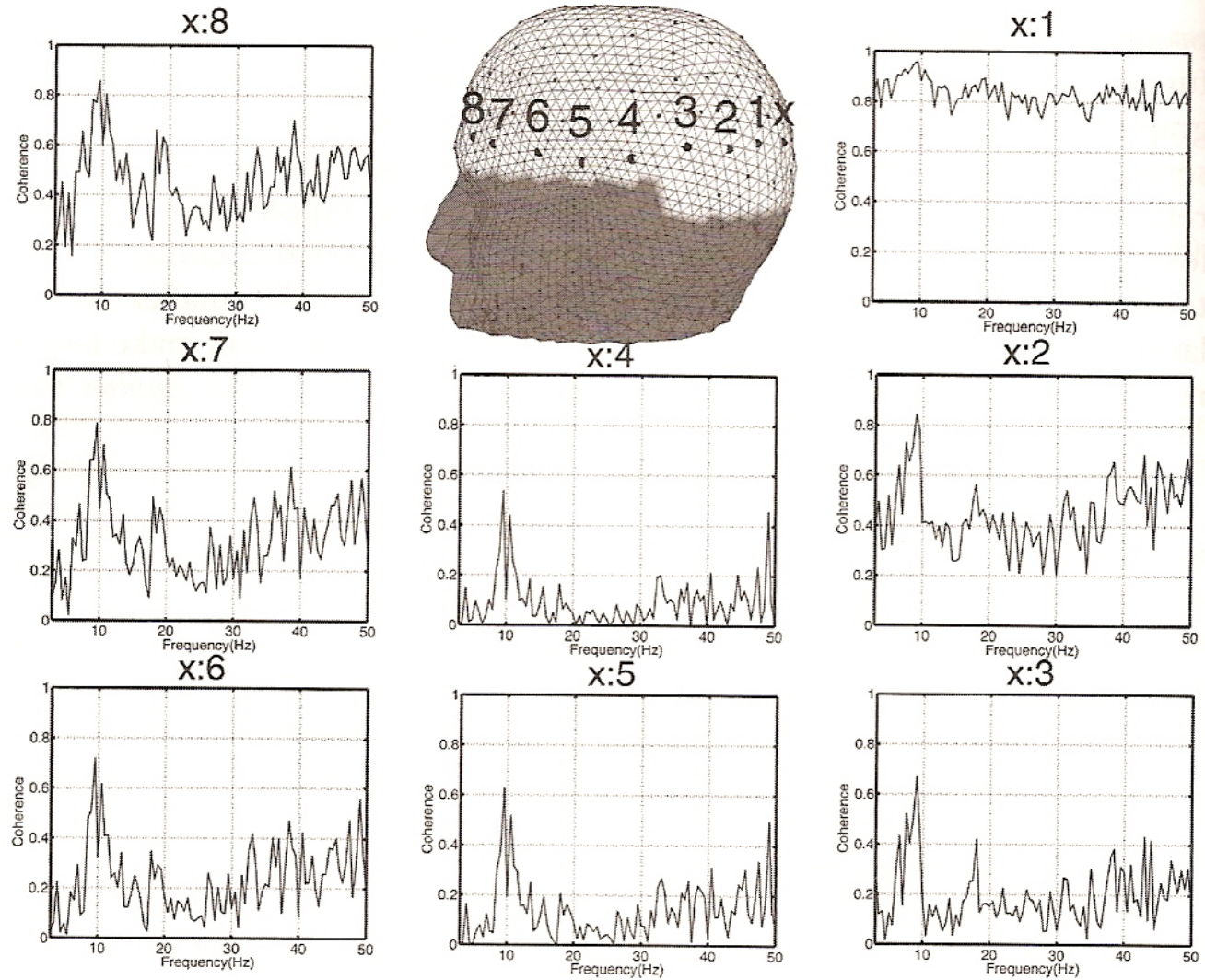


# Evoked Potential Avg. Reference



# Standard Coherence Calculations

- Fig 9.17



# Laplacian Reference

- Previous real results were calculated using an average reference
- Earlier Laplacians with the 10-20 system could be estimated as the average potential between an electrode and its 4 surrounding electrodes
- Later versions, such as that used for the 111 electrode arrays shown in the figures use spline functions to estimate continuous functions of the Laplacian

# Coherence Calculations using Spline Laplacian

- Fig 9.18

