

$$i_1 = \frac{V_{in} - V_2}{R_1}$$

$$i_2 = sC_2 V_2 \Rightarrow i_3 = i_2 = sC_2 V_2 = -\frac{V_o}{R_2}$$

$$\therefore \boxed{V_o = -sC_2 R_2 V_2}$$

$$i_1 = i_2 + i_4$$

$$\frac{V_{in} - V_2}{R_1} = V_2 sC_2 + (V_2 - V_o) sC_1 \quad \left(\text{but } V_2 = -\frac{V_o}{sC_2 R_2} \right)$$

$$\therefore \frac{V_{in} + \frac{V_o}{sC_2 R_2}}{R_1} = -\frac{V_o}{R_2} - V_o \left(\frac{1}{sC_2 R_2} + 1 \right) sC_1$$

organizing

$$\frac{V_{in}}{R_1} = -V_o \left(\frac{1}{sC_2 R_1 R_2} + \frac{1}{R_2} + \frac{C_1}{C_2 R_2} + sC_1 \right)$$

$$\frac{V_o}{V_{in}} = \frac{-1}{\left(\frac{1}{sC_2 R_2} + \frac{R_1}{R_2} + \frac{C_1 R_1}{C_2 R_2} + sC_1 R_1 \right)}$$

$$\frac{V_o}{V_{in}} = \frac{-sC_2R_2}{(1 + sC_2R_1 + sC_1R_1 + s^2C_1C_2R_1R_2)}$$

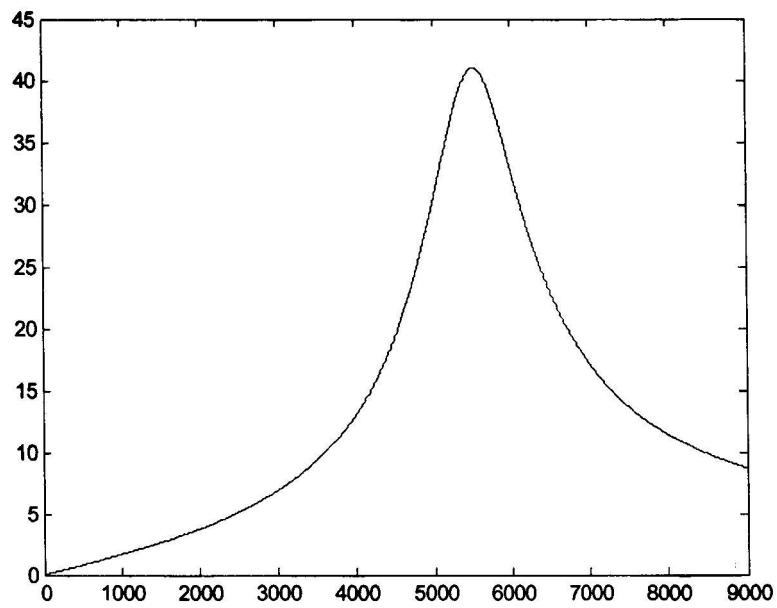
$$\frac{V_o}{V_2} = \frac{\left(-\frac{s}{C_1R_1}\right)}{\left(s^2 + s\left(\frac{1}{C_1R_2} + \frac{1}{C_2R_2}\right) + \frac{1}{C_1C_2R_1R_2}\right)}$$

For $C_1 = C_2 = 0.02 \mu\text{f}$ & $R_1 = 3\text{k}\Omega$, $R_2 = 8\text{k}\Omega$

we have

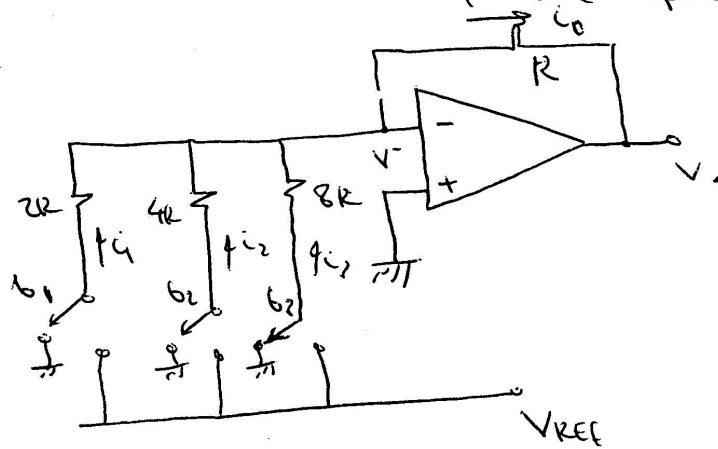
$$\frac{V_o}{V_2} = \frac{-5 \times 10^4 s}{s^2 + 1.2195 \times 10^3 s + 3.0488 \times 10^7}$$

```
NumberOfFrequencies=9000;  
AvValues=zeros(NumberOfFrequencies,1);  
DOmega=1;  
for Counter=1:NumberOfFrequencies  
    Omega=Counter*DOmega;  
    s=i*Omega;  
    AvValue(Counter,1)=(-5.0e4*s)/(s*s+1.2195e3*s+3.0488e7);  
end  
plot(abs(AvValue))
```



(4)

Find V_o as a function of the input bits



$$\text{A: } V^+ = 0 \Rightarrow V^- = 0$$

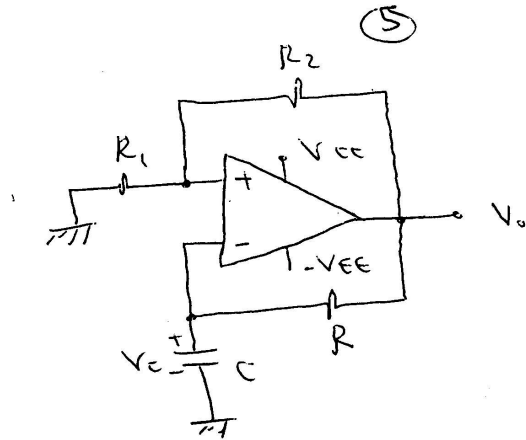
$$i_1 = \frac{b_1 V_{REF}}{2R}, \quad i_2 = \frac{b_2 V_{REF}}{4R}, \quad i_3 = \frac{b_3 V_{REF}}{8R}$$

$$V_o = -i_o R = -(i_1 + i_2 + i_3) R$$

$$= - \left(\frac{b_1 V_{REF}}{2R} + \frac{b_2 V_{REF}}{4R} + \frac{b_3 V_{REF}}{8R} \right) R$$

$$V_o = - (b_1 2^{-1} + b_2 2^{-2} + b_3 2^{-3}) V_{REF}$$

How to fix the -ve sign?



$V_o = V_{CC}$
 $V^+ = \frac{V_o R_1}{R_1 + R_2} = \beta V_{CC}$

$V^- = V_C \Rightarrow$ Capacitor charges until

$V_C^* = V^+ \Rightarrow$ output switches to $-V_{EE}$

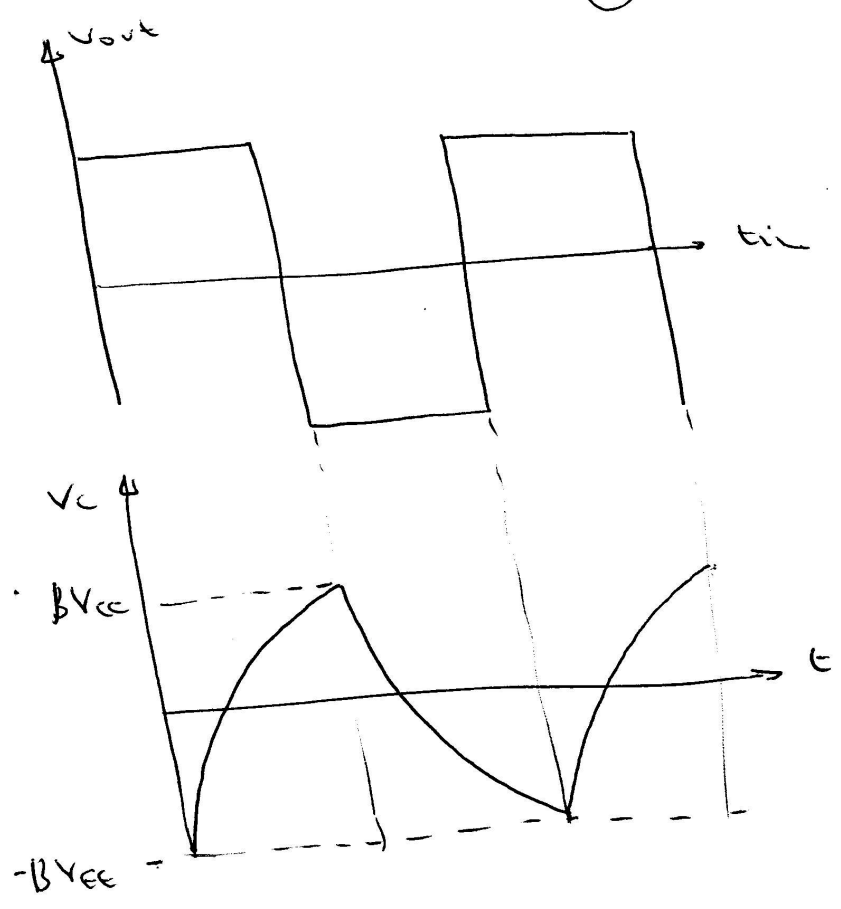
$V_o = -V_{EE}$

$V^+ = -V_{EE} \frac{R_1}{R_1 + R_2} = -\beta V_{EE}$

$V^- = V_C \Rightarrow$ Capacitor discharges until

$V_C = V^-$, output becomes V_{CC}

(6)



at charging ~~is~~

$$V_c(t) = V_{cc} - (V_{cc} + BV_{EE}) e^{-\frac{t}{RC}}$$

at discharging

$$V_c(t) = -V_{EE} - (-V_{EE} + BV_{CC}) e^{-\frac{t}{RC}}$$

