

Use the following formulae in your solutions

### Mathematical Model of the pn junction

$$i_D = I_S \left\{ \exp \left( \frac{V_D}{V_T} \right) - 1 \right\}$$

### Mathematical Model of a finite gain OpAmp

$$V_o = 0.5A_{cm}(V_+ + V_-) + A_d(V_+ - V_-)$$

$$CMRR = A_d/A_{cm}$$

### NMOS Transistor Mathematical Model

$V_{GS} \leq V_{TN}$	$i_{DS} = 0$	Cutoff
$V_{GS} \geq V_{TN}$ $0 \leq V_{DS} \leq (V_{GS} - V_{TN})$	$i_{DS} = K_n \left\{ (V_{GS} - V_{TN})V_{DS} - \frac{V_{DS}^2}{2} \right\}$	Linear
$V_{GS} \geq V_{TN}$ $V_{DS} \geq (V_{GS} - V_{TN}) \geq 0$	$i_{DS} = \frac{K_n}{2} (V_{GS} - V_{TN})^2 (1 + \lambda V_{DS})$	Saturation

### PMOS Transistor Mathematical Model

$V_{SG} \leq -V_{TP}$	$i_{SD} = 0$	Cutoff
$V_{SG} \geq -V_{TP}$ $0 \leq V_{SD} \leq (V_{SG} + V_{TP})$	$i_{SD} = K_p \left\{ (V_{SG} + V_{TP})V_{SD} - \frac{V_{SD}^2}{2} \right\}$	Linear
$V_{SG} \geq -V_{TP}$ $V_{SD} \geq (V_{SG} + V_{TP}) \geq 0$	$i_{SD} = \frac{K_p}{2} (V_{SG} + V_{TP})^2 (1 + \lambda V_{SD})$	Saturation

### Small signal Model Parameters of NMOS Transistors

$$g_m = \sqrt{2 K_n I_{DS} (1 + \lambda V_{DS})}$$

$$r_o = \frac{\frac{1}{\lambda} + V_{DS}}{I_{DS}}$$

Valid for  $V_{gs} \leq 0.2(V_{GS} - V_T)$

### Common source amplifier

$$A_v \approx -\frac{R_{IN}}{R_{IN} + R_S} g_m (R_D \parallel r_o \parallel R_L) \quad R_{IN} = R_G$$

## Propagation delays for reference CMOS inverter with $V_{DD}=5V$ , $V_{TN}=1V$ and $V_{TP}=-1V$

$$\tau_{PHL} = 0.322 \frac{C}{K_n} \quad \tau_{PLH} = 0.322 \frac{C}{K_p}$$

## Full Transport Model of npn transistors

$$i_C = I_s \left[ \exp\left(\frac{v_{BE}}{V_T}\right) - \exp\left(\frac{v_{BC}}{V_T}\right) \right] - \frac{I_s}{\beta_R} \left[ \exp\left(\frac{v_{BC}}{V_T}\right) - 1 \right]$$

$$i_E = I_s \left[ \exp\left(\frac{v_{BE}}{V_T}\right) - \exp\left(\frac{v_{BC}}{V_T}\right) \right] + \frac{I_s}{\beta_F} \left[ \exp\left(\frac{v_{BE}}{V_T}\right) - 1 \right]$$

$$i_B = \frac{I_s}{\beta_F} \left[ \exp\left(\frac{v_{BE}}{V_T}\right) - 1 \right] + \frac{I_s}{\beta_R} \left[ \exp\left(\frac{v_{BC}}{V_T}\right) - 1 \right]$$

## Simplifications of the Transport Model of npn Transistors

Forward active region:  $i_C = I_s \exp\left(\frac{v_{BE}}{V_T}\right)$ ,  $i_B = \frac{i_C}{\beta_F}$  and  $i_E = \frac{i_C}{\alpha_F}$

Saturation Region:  $v_{CESAT}=0.2$  V

Cut-off region:  $i_B = i_C = i_E = 0$

## Full Transport Model of pnp transistors

$$i_C = I_s \left[ \exp\left(\frac{v_{EB}}{V_T}\right) - \exp\left(\frac{v_{CB}}{V_T}\right) \right] - \frac{I_s}{\beta_R} \left[ \exp\left(\frac{v_{CB}}{V_T}\right) - 1 \right]$$

$$i_E = I_s \left[ \exp\left(\frac{v_{EB}}{V_T}\right) - \exp\left(\frac{v_{CB}}{V_T}\right) \right] + \frac{I_s}{\beta_F} \left[ \exp\left(\frac{v_{EB}}{V_T}\right) - 1 \right]$$

$$i_B = \frac{I_s}{\beta_F} \left[ \exp\left(\frac{v_{EB}}{V_T}\right) - 1 \right] + \frac{I_s}{\beta_R} \left[ \exp\left(\frac{v_{CB}}{V_T}\right) - 1 \right]$$

## Simplifications of the Transport Model of pnp Transistors

Forward active region:  $i_C = I_s \exp\left(\frac{v_{EB}}{V_T}\right)$ ,  $i_B = \frac{i_C}{\beta_F}$  and  $i_E = \frac{i_C}{\alpha_F}$

Saturation Region:  $v_{ECSAT}=0.2$  V

Cut-off region:  $i_B = i_C = i_E = 0$

## Small signal model for the BJT

$$g_m = \frac{I_C}{V_T} \quad r_\pi = \frac{\beta}{g_m} \quad r_e = \frac{\alpha}{g_m}$$

$$r_o = \frac{V_A}{I_C} \quad \text{Valid for } v_{be} \leq 0.005V$$

## Common emitter amplifier

$$A_v = -\frac{R_{IN}}{R_{IN} + R_S} g_m (R_C \parallel r_o \parallel R_L) \quad R_{IN} = R_{BB} \parallel r_\pi$$

## 2-Port Network Parameters

$$V_1 = Z_{11}I_1 + Z_{12}I_2$$

$$V_2 = Z_{21}I_1 + Z_{22}I_2$$

$$I_1 = Y_{11}V_1 + Y_{12}V_2$$

$$I_2 = Y_{21}V_1 + Y_{22}V_2$$

$$V_1 = h_{11}I_1 + h_{12}V_2$$

$$V_2 = h_{21}I_1 + h_{22}V_2$$

$$I_1 = g_{11}V_1 + g_{12}I_2$$

$$V_2 = g_{21}V_1 + g_{22}I_2$$