
COMPUTATIONAL PHOTOGRAPHY

Chapter 10

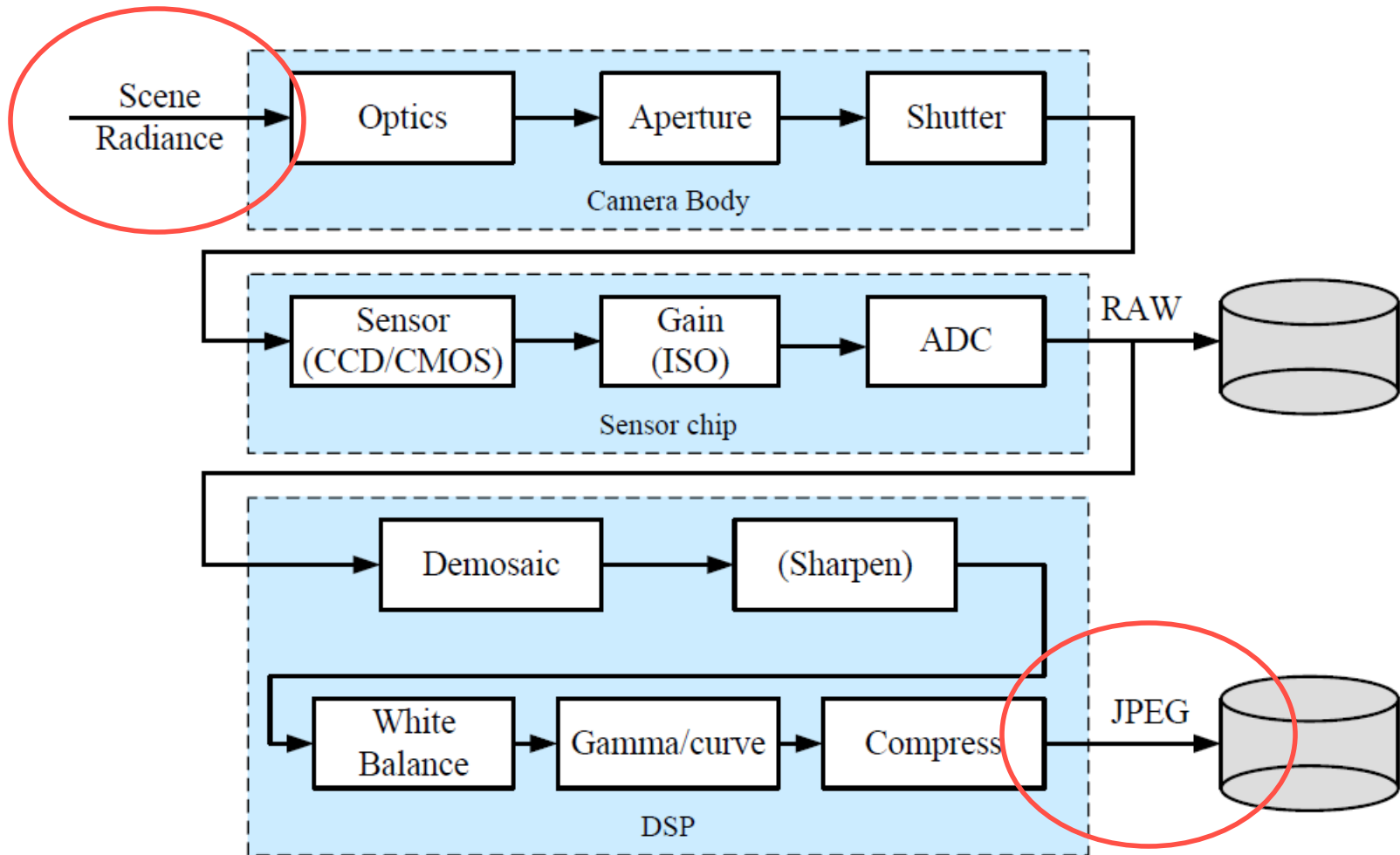
Computational photography

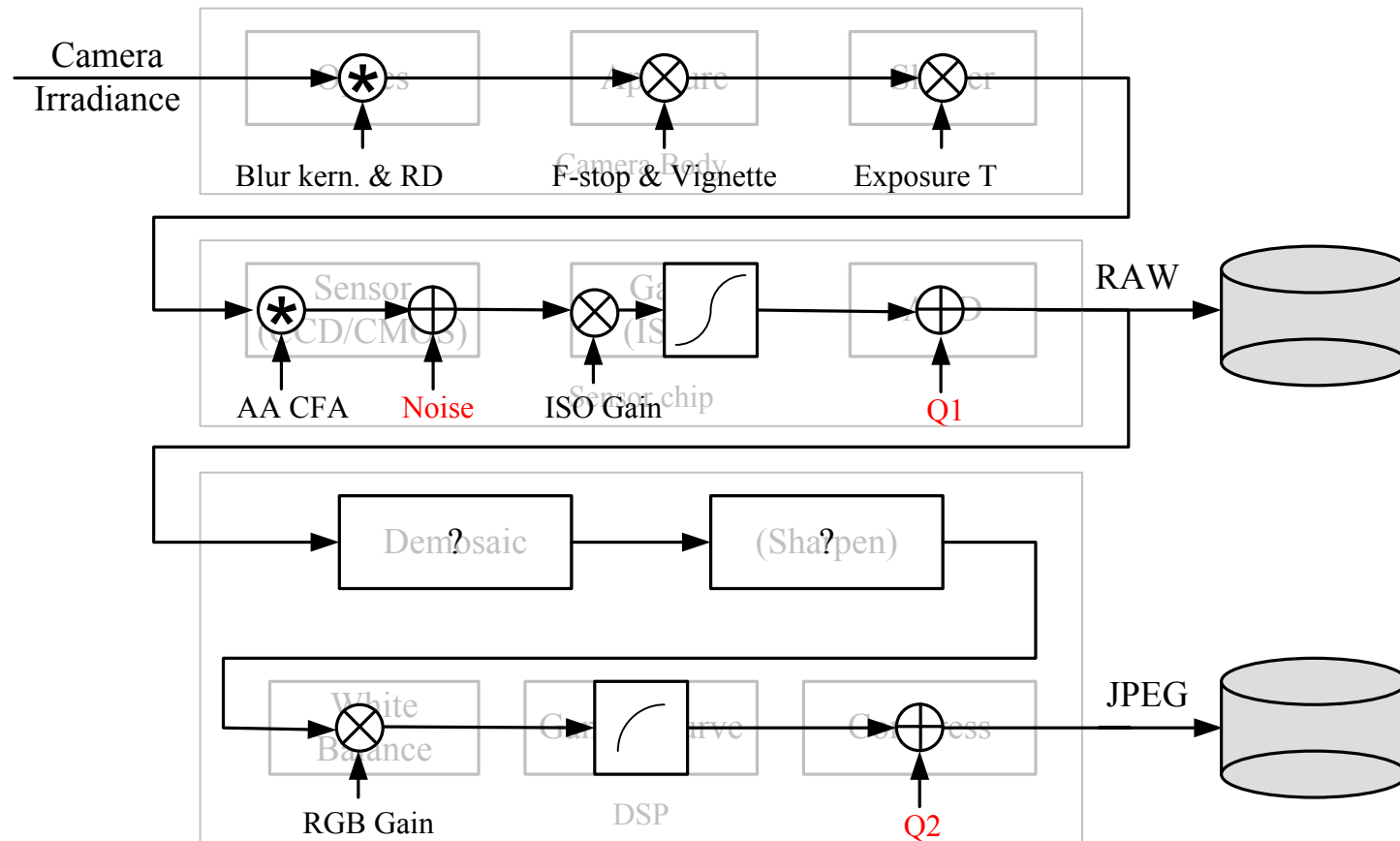
- Computational photography: image analysis and processing algorithms are applied to one or more photographs to create images that go beyond the capabilities of traditional imaging systems

Computational photography

- Photometric calibration: the measurement of camera and lens responses
- High dynamic range imaging: capturing the full range of in a scene through the use of multiple exposures
- Image matting and compositing: algorithms for cutting pieces of images from one photograph and pasting them into others
- Super-resolution and blur removal: improving the resolution of images
- Texture analysis and synthesis: how to generate novel textures from real-world samples for applications such as holes filling

Image sensing pipeline

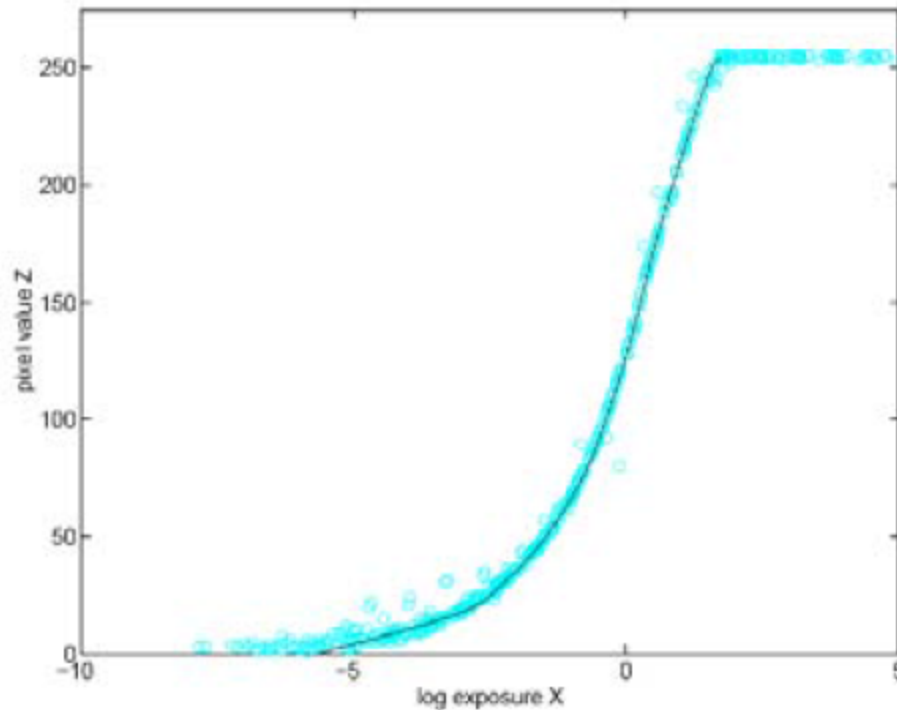




Calibration

- Radiometric response function: maps arriving photons into digital values stored in the file
- Noise level estimation

Radiometric response function



- **Affect Factors:**
 - 1. Aperture and shutter speed
 - 2. A/D converter (controlled by ISO, linear)
 - 3. Demosaicing
 - 4. ...
- Hard to model, easier to measure

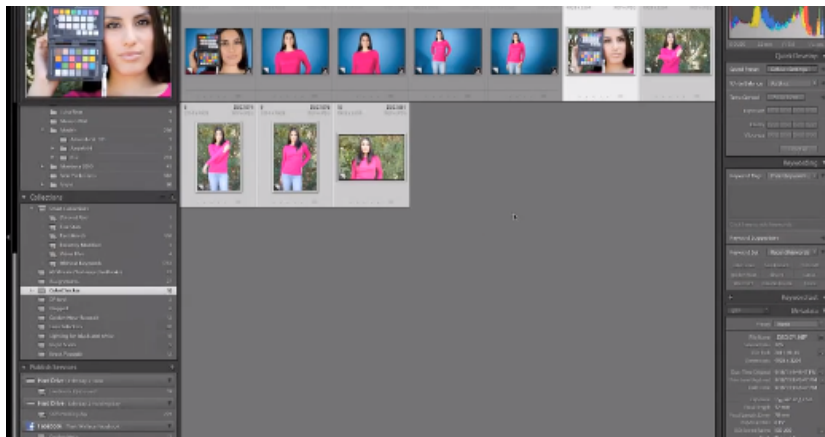
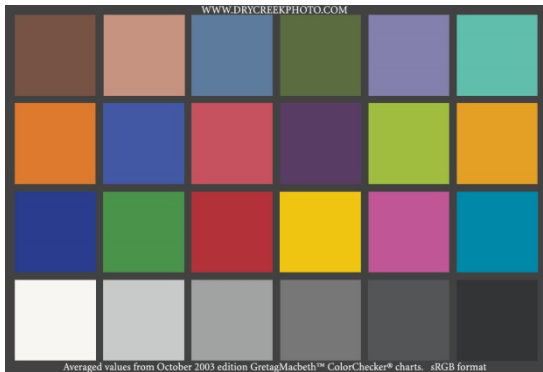
Approaches to measure response function

- Integrating sphere



Approaches to measure response function

- Calibration chart



<http://www.adorama.com/alcl0013301/article/Using-the-ColorChecker-Passport-Adorama-TV>

Noise level estimation



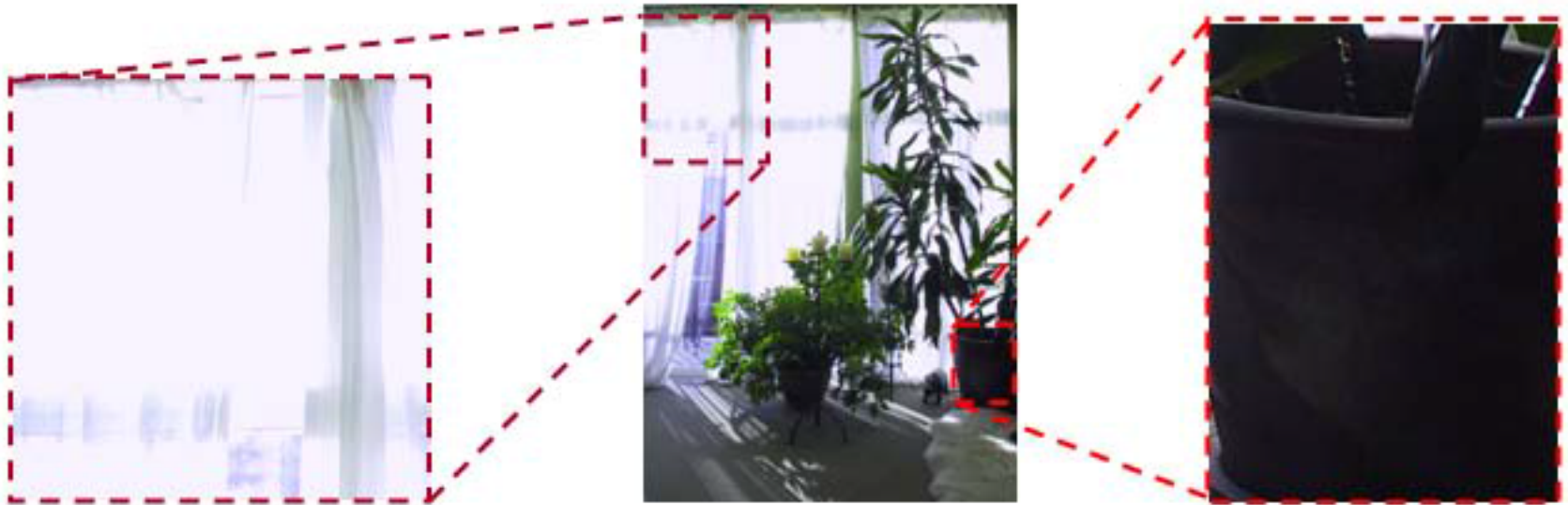
Approaches to measure noise

- Integrating sphere
- Calibration chart
- Taking repeated exposures and computing the variance
- Assuming pixel values should all be the same within some region

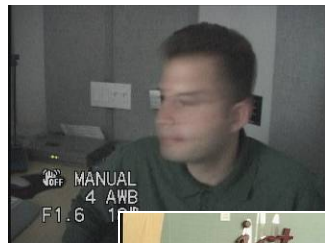
High dynamic range imaging

- Registered images taken at different exposures can be used to calibrate the radiometric response function of a camera
- They can create well-exposed photographs

High Dynamic Range



The Problem of Dynamic Range



1



1500



25,000

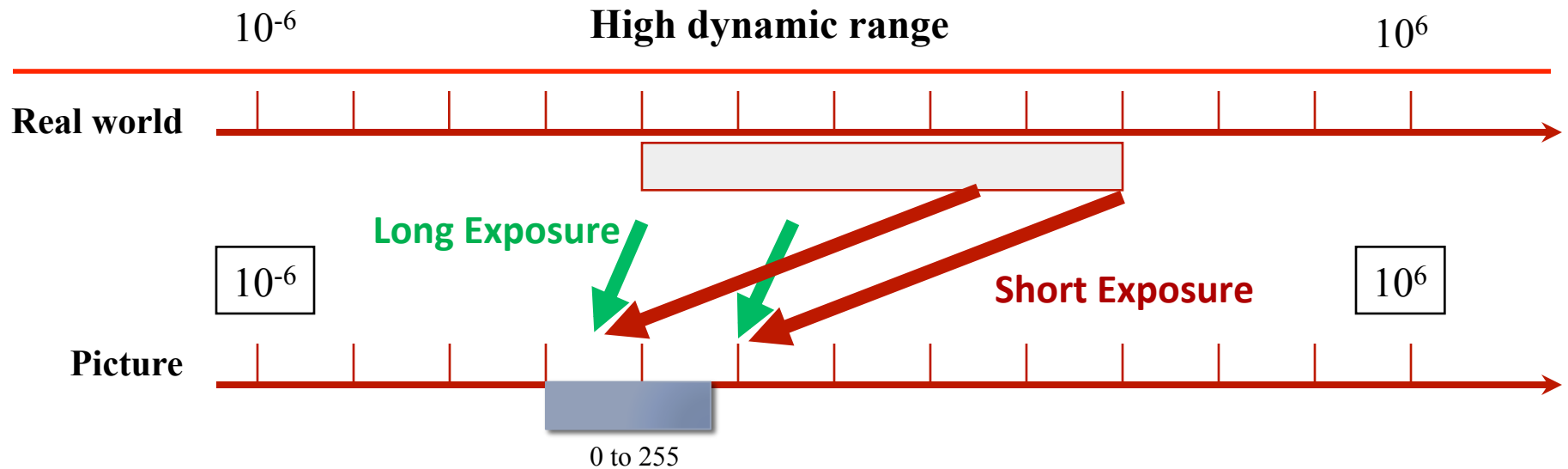


400,000

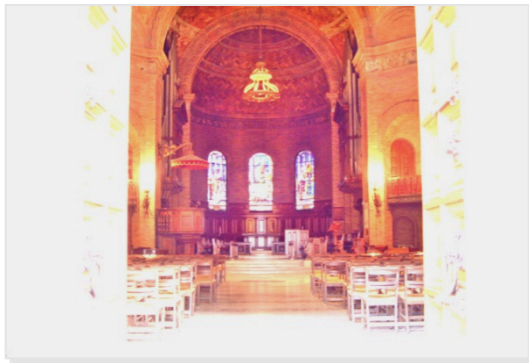


200,000,000

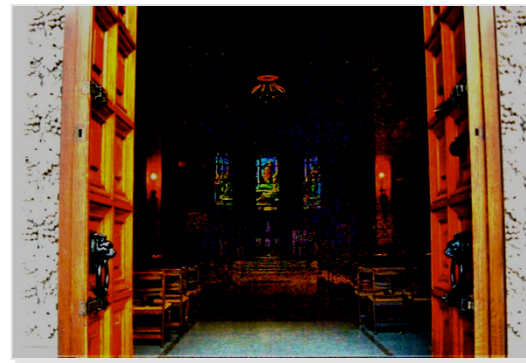
The real world is **high dynamic range!**



- Today's Cameras: Limited Dynamic Range



High Exposure Image



Low Exposure Image

- We need about 5-10 million values to store all brightnesses around us.
- But, typical 8-bit cameras provide **only 256 values!!**

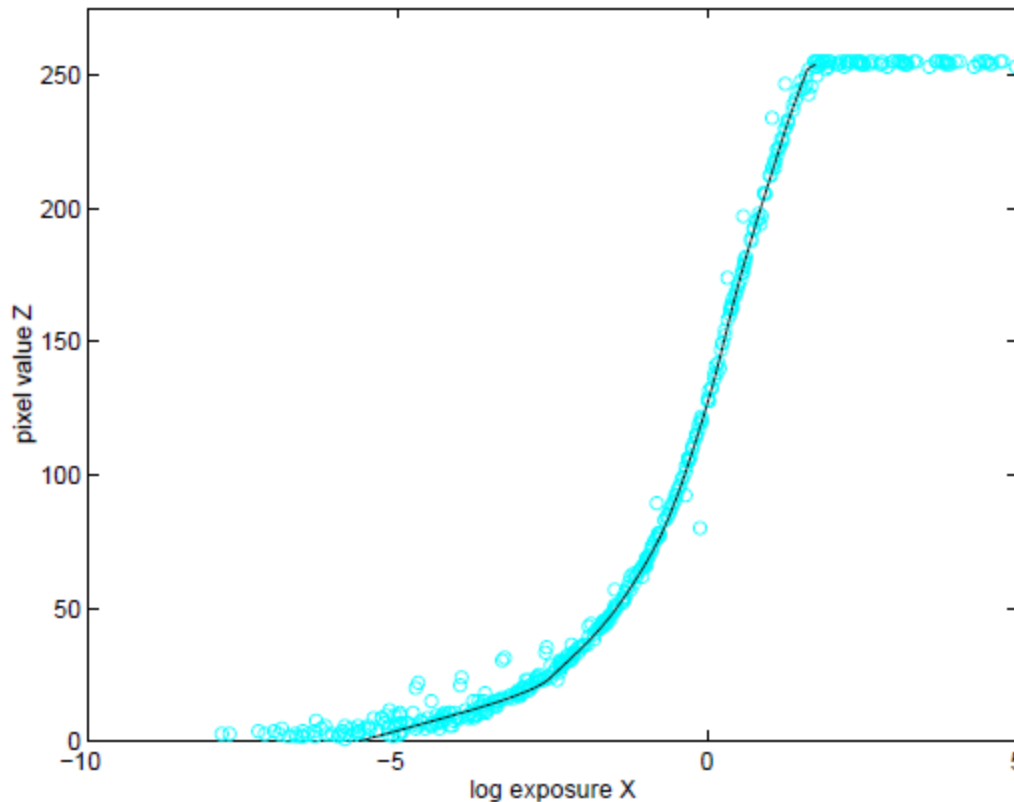
AEB mode and HDR Composite



Recovering HDR

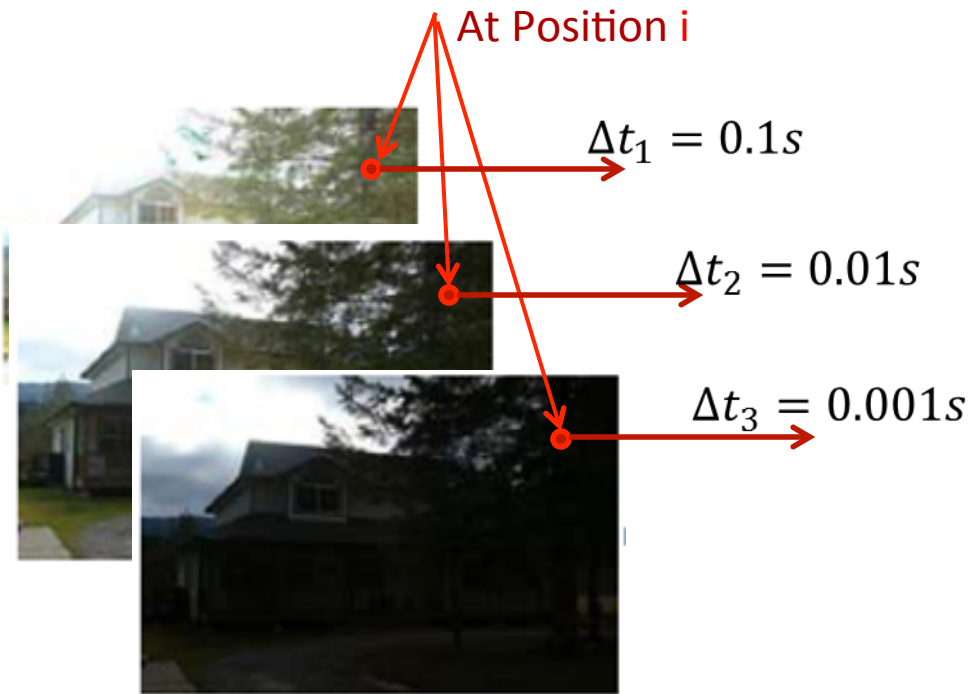
- 1. Extract the **radiometric response function** from the
- 2. Estimate a radiance map by blending pixels from different exposures
- 3. **Tone-map** it into a single low dynamic range image

Recover radiometric response



- **Given** multiple exposure pictures
- **Goal**: estimating the radiometric response function(radiance map)

Recover radiance map



- The radiance map can be written as:

$$Z_{ij} = f(E_i \cdot \Delta t_j)$$

- Where E_i is the radiance at position i.
- Define $E_i \Delta t_j$ as the exposure.
- Known: $\Delta t_j, Z_{ij}$
- Unknown: E_i, f

Recover radiance map

$Z_{ij} = f(E_i \cdot \Delta t_j)$ can be rewrite as:

$f^{-1}(Z_{ij}) = (E_i \cdot \Delta t_j)$, taking the natural logarithm of both sides, we have:

$\ln f^{-1}(Z_{ij}) = \ln E_i + \ln \Delta t_j$, to simplify notation, let $g = \log f^{-1}$

$$g(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

- Note: recovering g only requires recovering **finite** number of values.(Since the domain of Z is from 0-255)

Recover radiance map

- Objective function:

$$\hat{E}_i, \widehat{g(z)} = \min_{E_i, g(z)} \sum_{i=1}^N \sum_{j=1}^P [\mathbf{g}(\mathbf{Z}_{ij}) - \ln E_i - \ln \Delta t_j]^2 + \lambda \sum_{z=0}^{255} g''(z)$$

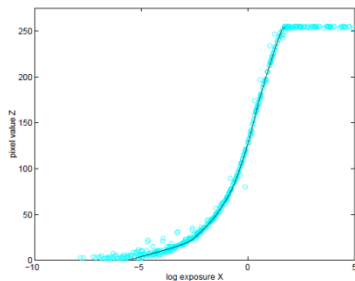
Recover radiance map

- **Refine objective function:**

- 1. scalar function: $g(Z_{mid}) = 0$

- 2. anticipating the basic shape of the response function:

$$w(z) = \begin{cases} z - Z_{min} & \text{for } z \leq \frac{1}{2}(Z_{min} + Z_{max}) \\ Z_{max} - z & \text{for } z > \frac{1}{2}(Z_{min} + Z_{max}) \end{cases}$$



$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 +$$

$$\lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

Recover radiance map

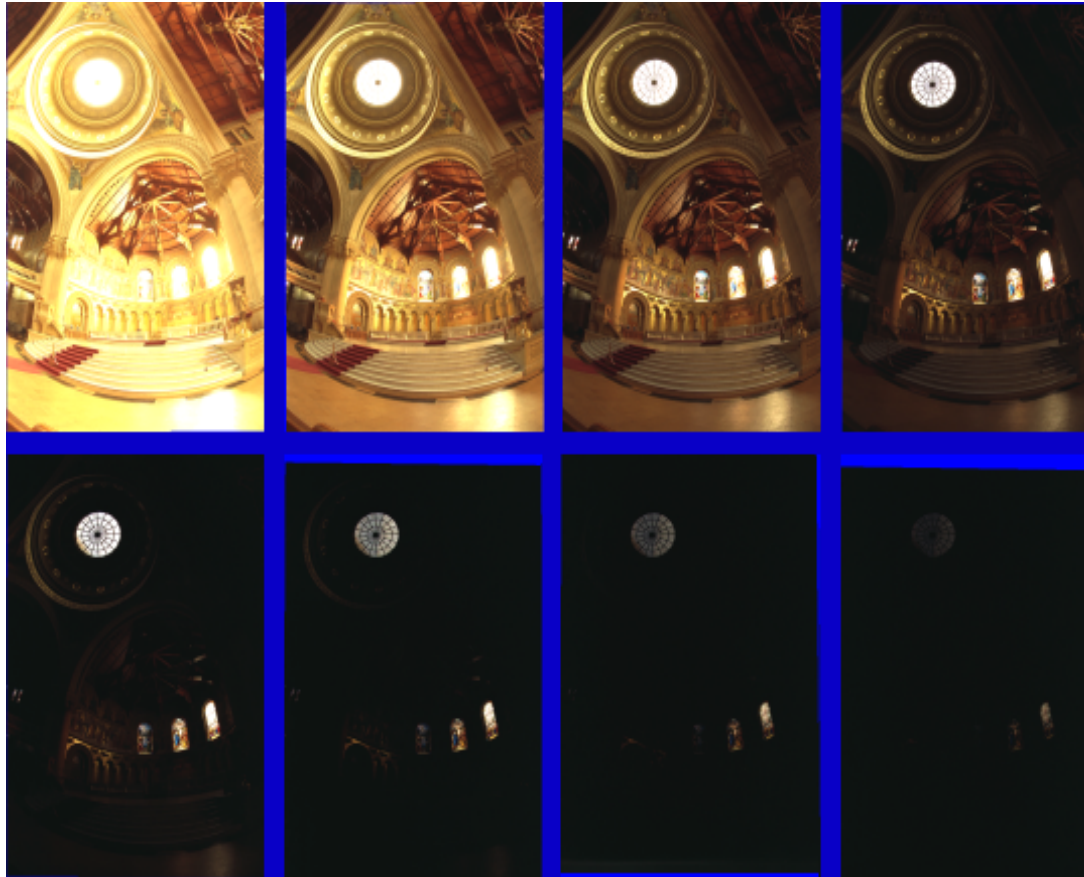
- **Refine objective function:**
- 3. How many samples(pixels) do we need to calculate:

$$\widehat{E_i}, \widehat{g(z)} = \min_{E_i, g(z)} \sum_{i=1}^N \sum_{j=1}^P [\mathbf{g}(Z_{ij}) - \ln E_i - \ln \Delta t_j]^2 + \lambda \sum_{z=0}^{255} g''(z)$$

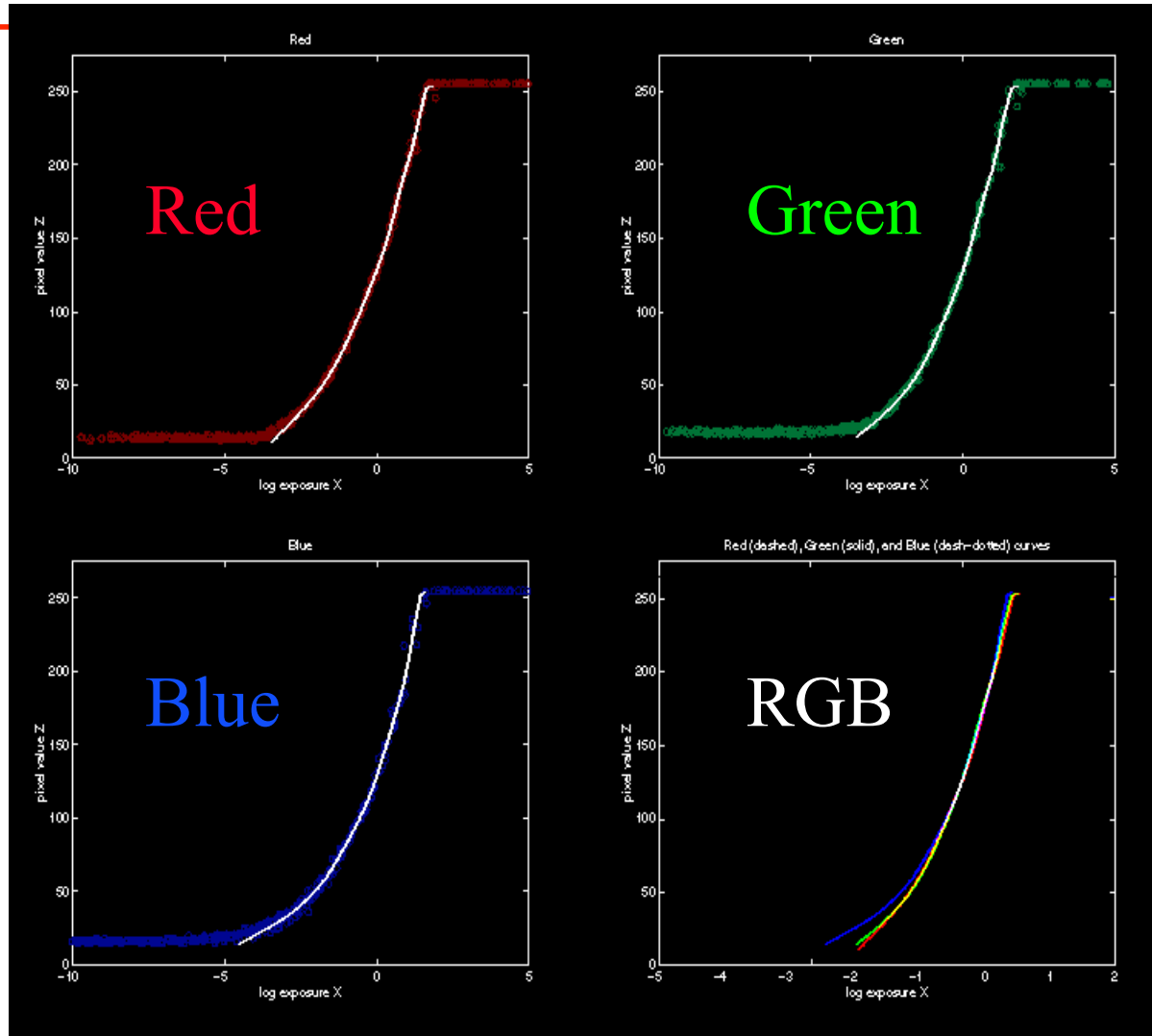
1. Make sure (# of E_i)*(# of Pictures)>256
2. The pixel locations should be chosen so that they have a reasonably even distribution of pixel values.

Results: Color Film

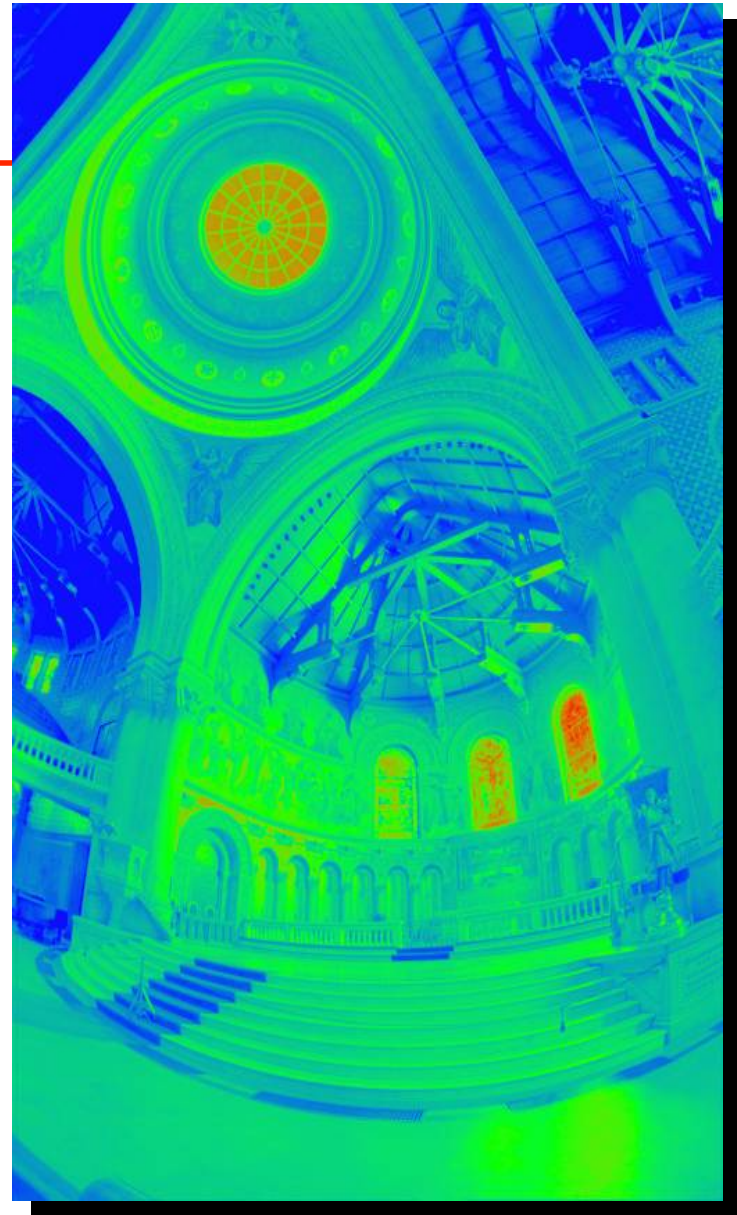
- Kodak Gold ASA 100, PhotoCD



Recovered Response Curves



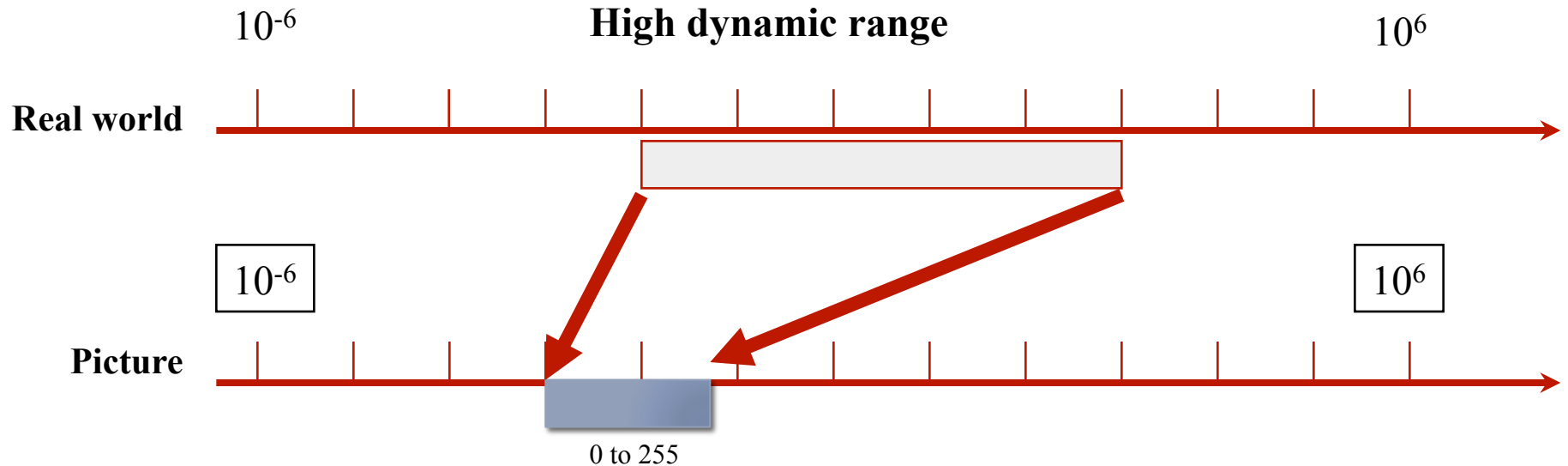
The Radiance Map



Tone-mapping

- Once a radiance map has been computed, it is usually necessary to display it on a lower gamut (i.e., 8-bit) screen or printer

Tone mapping

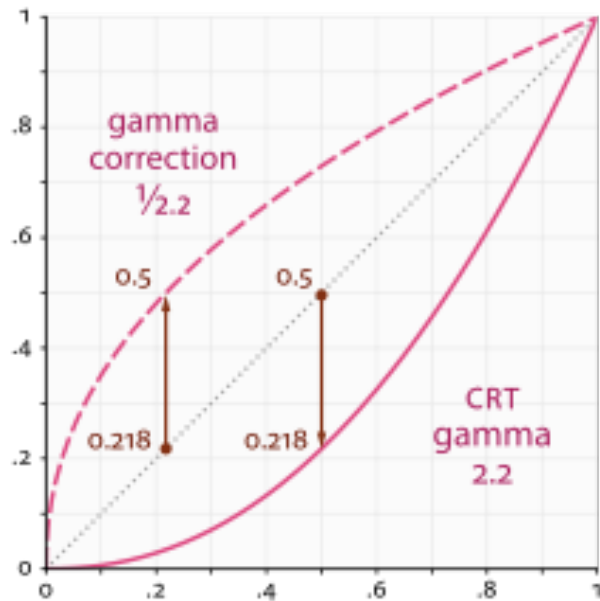


- **Given** radiance map
- **Goal**: build a reasonable mapping function of radiance to pixel values

Tone mapping Methods

- **Simple Gamma tone mapping**

Gamma applied to each color channel independently



Gamma compression



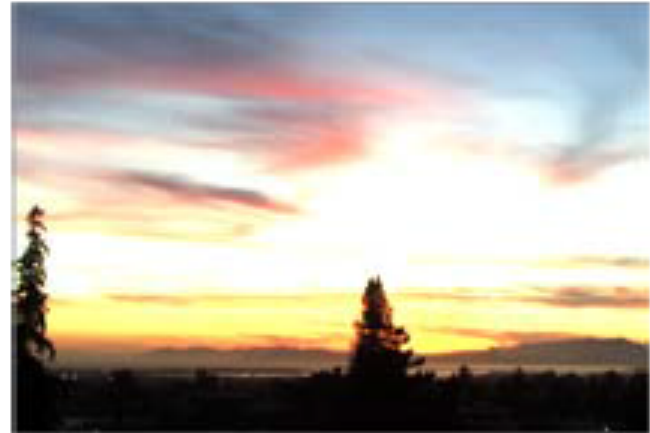
Input Image



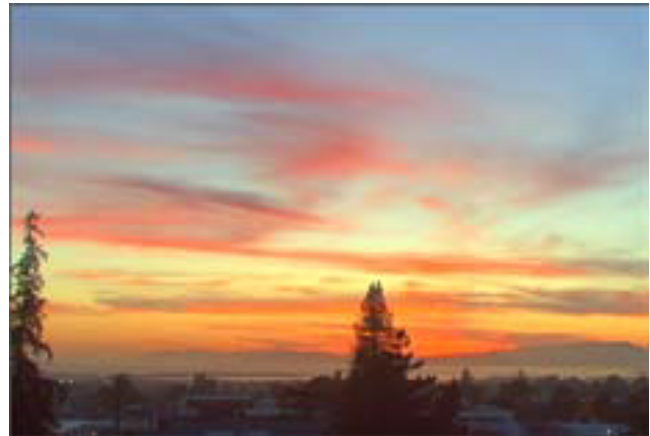
Gamma applied to each channel

Tone mapping Methods

- **Intensity Gamma tone mapping**
- Splitting the image up into luminance and chrominance(L^*a^*b) components, and applying the mapping to the luminance channel



Input Image



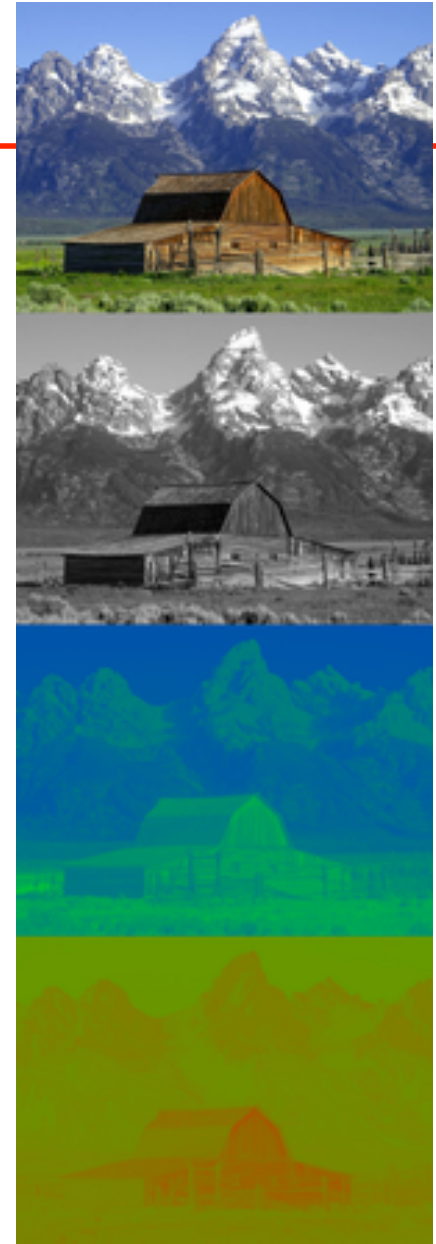
Gamma applied to luminance

Chrominance and luminance

- **YUV** color space

$$\begin{bmatrix} Y' \\ U \\ V \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.14713 & -0.28886 & 0.436 \\ 0.615 & -0.51499 & -0.10001 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1.13983 \\ 1 & -0.39465 & -0.58060 \\ 1 & 2.03211 & 0 \end{bmatrix} \begin{bmatrix} Y' \\ U \\ V \end{bmatrix}$$



Tone mapping Methods

- Advanced mapping method



Figure 10.21 Local tone mapping using linear filters: (a) low-pass and high-pass filtered log luminance images and color (chrominance) image; (b) resulting tone-mapped image (after attenuating the low-pass log luminance image) shows visible halos around the trees. Processed images courtesy of Frédo Durand, MIT 6.815/6.865 course on Computational Photography.

Tone mapping Methods

- Advanced mapping method (using Edge-preserving filter)



Figure 10.22 Local tone mapping using bilateral filter (Durand and Dorsey 2002): (a) low-pass and high-pass bilateral filtered log luminance images and color (chrominance) image; (b) resulting tone-mapped image (after attenuating the low-pass log luminance image) shows no halos. Processed images courtesy of Frédo Durand, MIT 6.815/6.865 course on Computational Photography.

Image matting and compositing



Compositing Equation

$$C = (1 - \alpha)B + \alpha F$$

- B: background image
- F: foreground image
- C: composite image

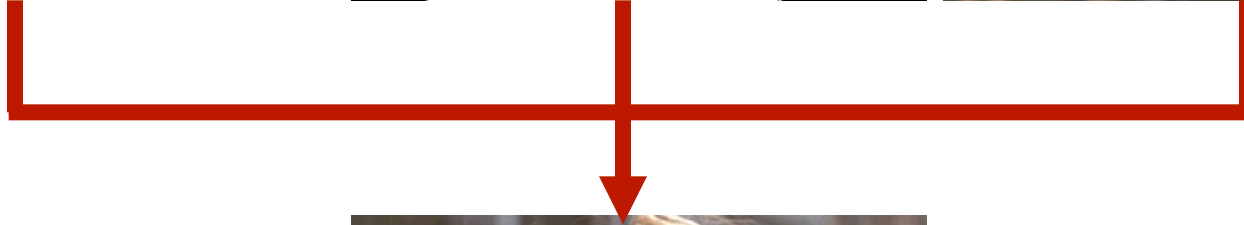
foreground color



alpha matte



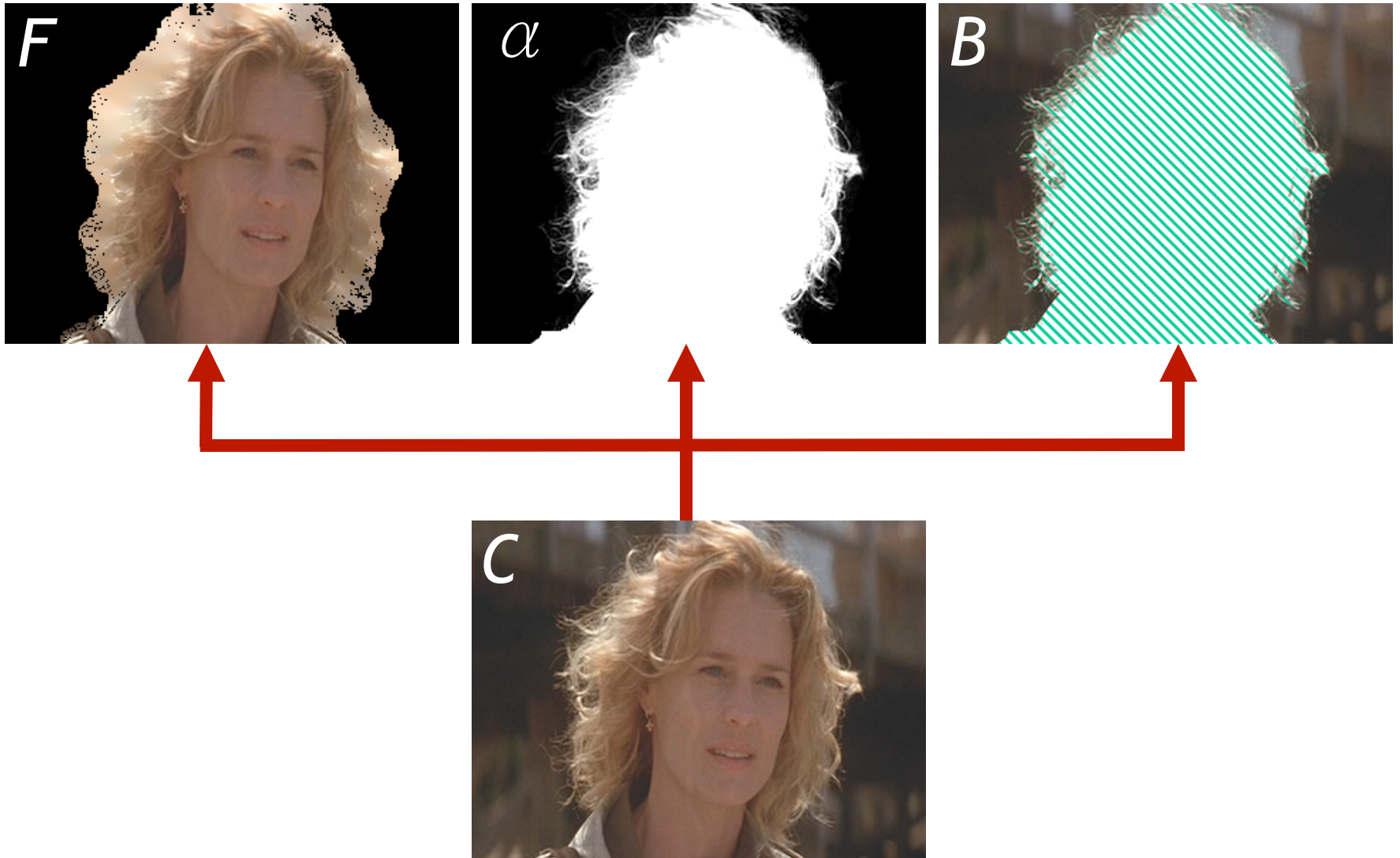
background plate



$$C = (1 - \alpha)B + \alpha F$$

compositing
equation

Matting



Matting ambiguity

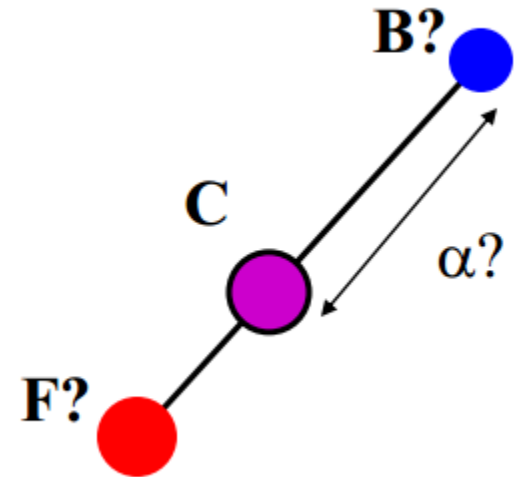
$$C = (1 - \alpha)B + \alpha F$$

Known: C

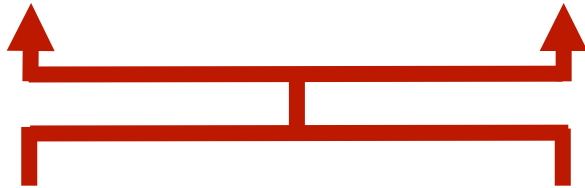
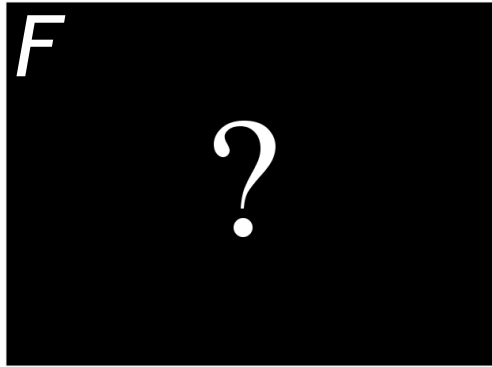
Unknown: α, B, F

7 unknowns: α and triplets for F and B

3 equations, one per color channel



Blue screen matting



$$C = (1 - \alpha)B + \alpha F$$

Known: C, B

Unknown: α, F

4 unknowns: α and

triplets for F

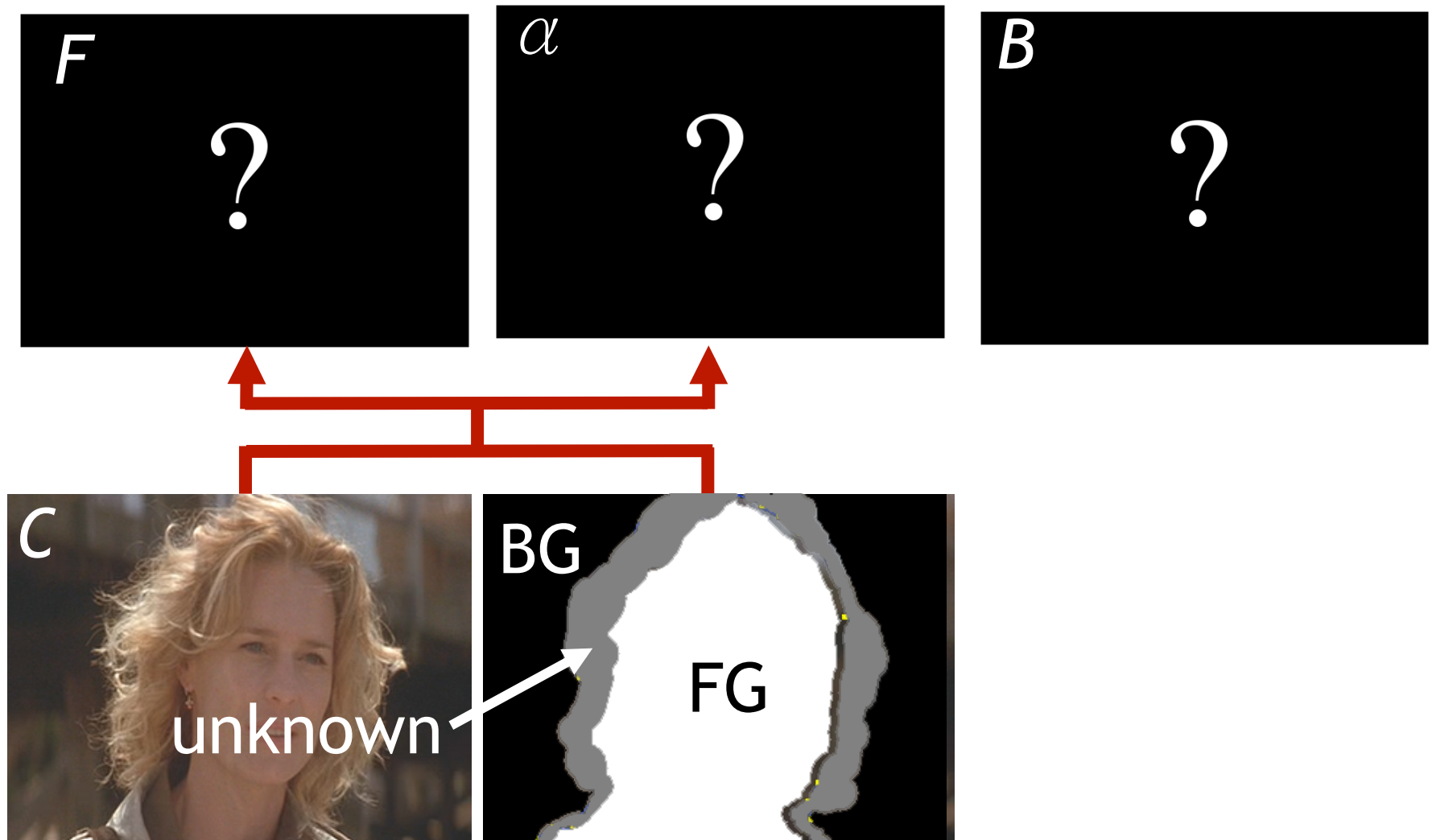
3 equations, one per color
channel

Blue screen matting issues

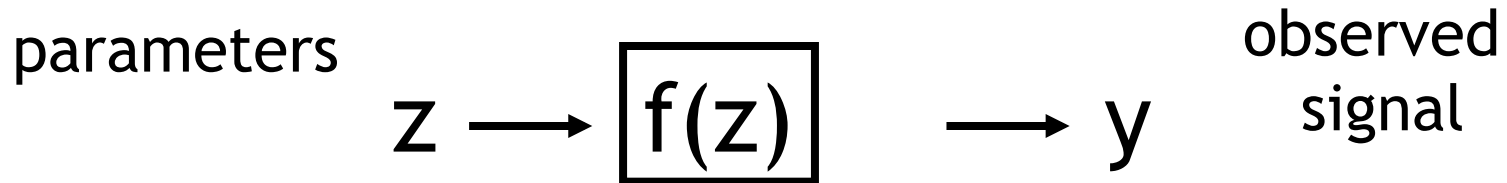
- **Color limitation**
 - – Annoying for blue-eyed people
adapt screen color (in particular green)
- **Shadows**
 - – How to extract shadows cast on background



Natural image matting



Bayesian framework



$$\begin{aligned} z^* &= \max_z P(z \mid y) \\ &= \max_z \frac{P(y \mid z)P(z)}{P(y)} \\ &= \max_z L(y \mid z) + L(z) \end{aligned}$$

Example:
super-resolution
de-blurring
de-blocking
...

Bayesian matting approach(Chuang 2001)



$$P(\mathbf{F}, \mathbf{B}, \alpha | \mathbf{C}) = P(\mathbf{C} | \mathbf{F}, \mathbf{B}, \alpha) P(\mathbf{F}, \mathbf{B}, \alpha) / P(\mathbf{C})$$

↑
**Foreground,
background,
transparency you
want to estimate**

↑
Color you observe

↑
**Likelihood
function**

↑
Prior probability

↑
**Constant w.r.t.
parameters x.**

Bayesian matting approach(Chuang 2001)

- We must try to build a probability distribution for the unknown regions.

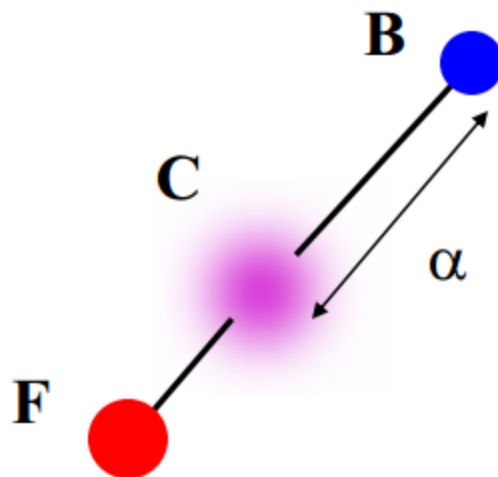
$$\begin{aligned}\mathbf{max} L(F, B, \alpha|C) &= \mathbf{max} L(C|F, B, \alpha) + L(F, B, \alpha) - L(C) \\ &= \mathbf{max} L(C|F, B, \alpha) + L(F, B, \alpha) \\ &= \mathbf{max} L(C|F, B, \alpha) + L(F) + L(B) + L(\alpha)\end{aligned}$$



Bayesian matting approach(Chuang 2001)

- **Log likelihood** $\mathbf{L}(C|F, B, \alpha)$

$$\mathbf{L}(C|F, B, \alpha) = -\|C - \alpha F - (1 - \alpha)B\|^2 / \sigma^2$$



Bayesian matting approach(Chuang 2001)

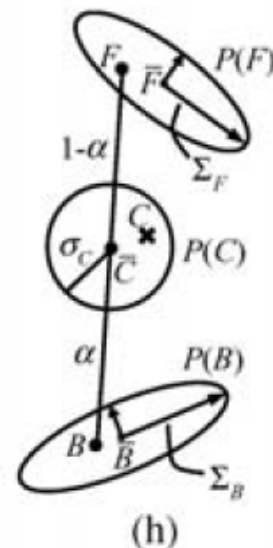
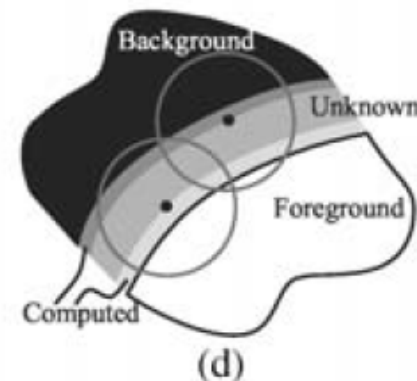
- **Prior probabilities** $L(F), L(B)$

$$\mathbf{L}(F) = -(\mathbf{F} - \bar{\mathbf{F}})^T \Sigma_F^{-1} (\mathbf{F} - \bar{\mathbf{F}})/2$$

$$\bar{\mathbf{F}} = \frac{1}{W} \sum_{i \in N} w_i \mathbf{F}_i$$

$$\Sigma_F = \frac{1}{W} \sum_{i \in N} w_i (\mathbf{F}_i - \bar{\mathbf{F}}) (\mathbf{F}_i - \bar{\mathbf{F}})^T$$

- **SAME for B**



Bayesian matting approach(Chuang 2001)

- **Prior probabilities** $L(\alpha)$
- In this work, we assume that log likelihood for the opacity $L(\alpha)$ is constant.
- Ignort it.

Bayesian matting approach(Chuang 2001)

$$\mathbf{max} L(F, B, \alpha|C) = \mathbf{max} L(C|F, B, \alpha) + L(F) + L(B)$$

$$\mathbf{L}(C|F, B, \alpha) = -\|C - \alpha F - (1 - \alpha)B\|^2 / \sigma^2$$

$$\mathbf{L}(F) = -(F - \bar{F})^T \Sigma_F^{-1} (F - \bar{F}) / 2$$

$$\mathbf{L}(B) = -(B - \bar{B})^T \Sigma_B^{-1} (B - \bar{B}) / 2$$

Bayesian matting approach(Chuang 2001)

- Solve math problem: (for α constant)
- **Derive $L(C|F,B,\alpha) + L(F) + L(B) + L(\alpha)$ wrt F & B , and set to zero gives**

$$\begin{bmatrix} \Sigma_F^{-1} + I\alpha^2/\sigma_C^2 & I\alpha(1-\alpha)/\sigma_C^2 \\ I\alpha(1-\alpha)/\sigma_C^2 & \Sigma_B^{-1} + I(1-\alpha)^2/\sigma_C^2 \end{bmatrix} \begin{bmatrix} F \\ B \end{bmatrix} = \begin{bmatrix} \Sigma_F^{-1}\bar{F} + C\alpha/\sigma_C^2 \\ \Sigma_B^{-1}\bar{B} + C(1-\alpha)/\sigma_C^2 \end{bmatrix},$$

Bayesian matting approach(Chuang 2001)

- Solve math problem: for F & B constant
- **Derive $L(C|F,B,\alpha) + L(F) + L(B) + L(\alpha)$ wrt α , and set to zero gives**

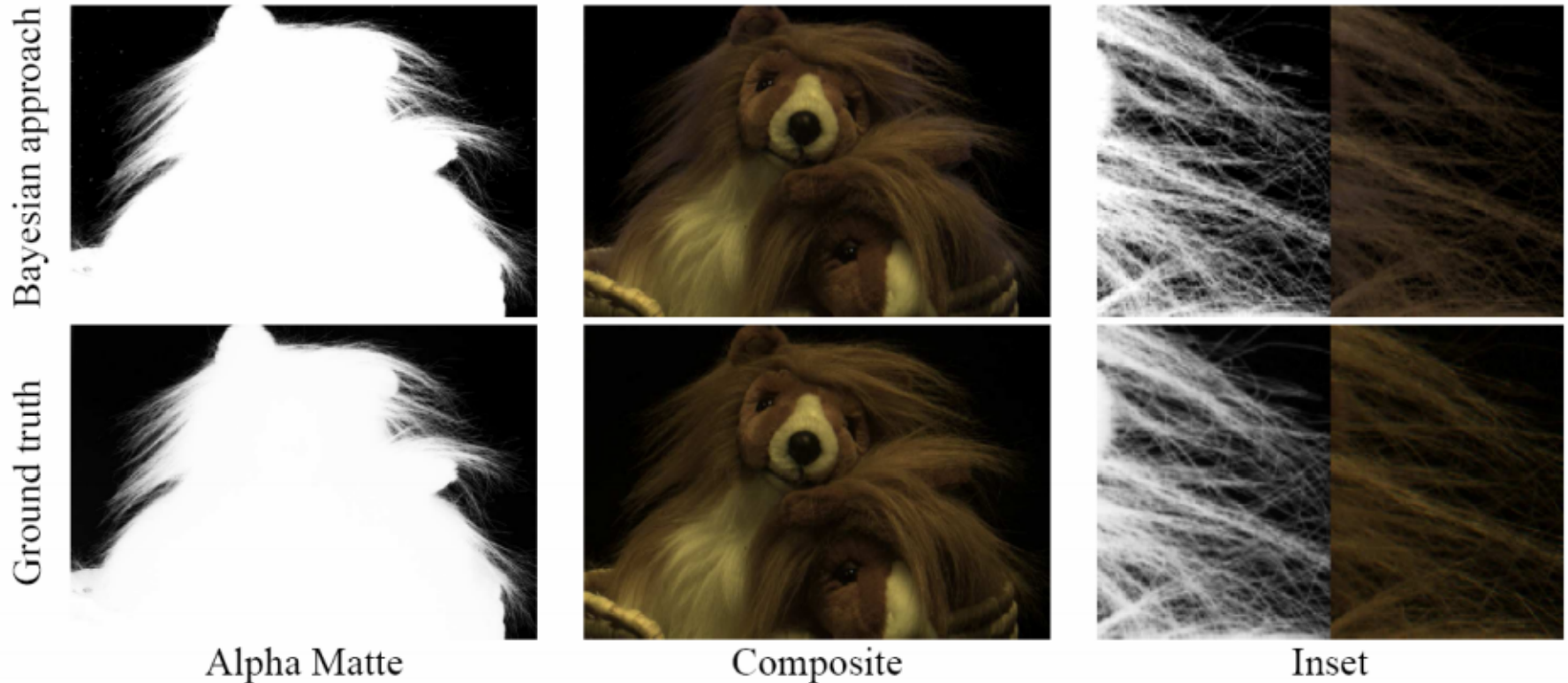
$$\alpha = \frac{(C - B) \cdot (F - B)}{\|F - B\|^2}$$

Bayesian matting approach(Chuang 2001)

- **Solve math problem:**
 - 1. The user **specifies a trimap**
 - 2. **Compute Gaussian** distributions for foreground and background regions
 - 3. **Iterate**
 - – Keep α constant, solve for F & B (for each pixel)
 - – Keep F & B constant, solve for α (for each pixel)
- **Note that pixels are treated independently**

Bayesian matting approach(Chuang 2001)

- Results:



Super-resolution and blur removal



How to increase resolution

- Possible ways for increasing an image resolution:
 - – Reducing pixel size.
 - – Increase the chip-size.
 - – Super-resolution.

How to increase resolution

- **Reduce pixel size:**
 - Increase the number of pixels per unit area.
- Advantage:
 - Increases spatial resolution.
- Disadvantage:
 - Noise introduced.
 - As the pixel size decreases, the amount of light decreases.

How to increase resolution

- **Increase the chip size (HW):**
- Advantage:
 - Enhances spatial resolution.
- Disadvantage:
 - High cost for high precision optics.

How to increase resolution

- **Superresolution (SR):**

- Process of combining multiple low resolution images to form a high resolution image.

- Advantages:

- Cost less than comparable approaches.
- LR imaging systems can still be utilized.

Super resolution

$$o_k(\mathbf{x}) = D\{b(\mathbf{x}) * s(\hat{h}_k(\mathbf{x}))\} + n_k(\mathbf{x})$$

$$\sum_k ||o_k(\mathbf{x}) - D\{b(\mathbf{x}) * s(\hat{h}_k(\mathbf{x}))\}||^2$$

$$\sum_k ||o_k - DB_K W_K s||^2$$

Super-resolution

- Obtaining a HR image from one or multiple LR images .



zoom

apply super-resolution
technique

Super-resolution

